



Fundamental Principles of Mechanical Engineering

Technical Handbook



FLENDER Drives

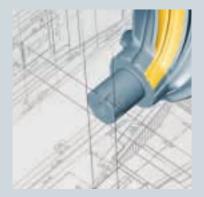
Answers for industry.

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FLENDER Drives

Fundamental Principles of Mechanical Engineering

Technical Handbook



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And discover how you can sustainably enhance your competitive edge with us.

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1. Method of indicating surface texture on drawings acc. to DIN EN ISO 1302

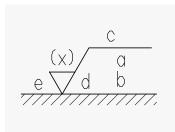
1.1 Symbols for the surface texture					
Graphic symbols	Meaning				
\bigvee	Material removal by machining is required (without requirements).				
preserved	Material removal by machining is required (with additional indication).				
✓	Material removal is prohibited (without requirements).				
non-porous	Material removal is prohibited (with additional indication).				
6.3	Material removal; surface roughness value $Ra = 6.3 \mu m$.				
	Material removal applies to the external contour of the view.				
3 🗸	Machining allowance specified by a numerical value in mm (e.g. 3 mm).				
lead-free 0.4 - 0.8	Material removal (by machining), surface roughness value $\it Ra=0.4$ - 0.8 $\it \mu m$. Requirement for the surface: "lead-free".				

1.2 Definition of the surface parameter Ra

The centre line average height *Ra* of the assessed profile is defined in DIN EN ISO 4287 and

the evaluation length for assessing the roughness in DIN EN ISO 4288.

1.3 Indications added to the graphic symbols



- a = Requirements on the surface appearance
- b = Two or more requirements on the surface appearance
- c = Production method, treatment, coating, or other requirements concerning the manufacturing method, etc.
- d = Surface grooves and their direction
- e = Machining allowance
- (x) = No longer applicable (formerly: indication of Ra)

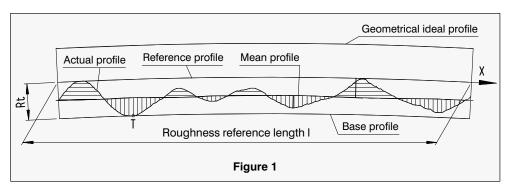
2. Surface roughness parameters

2.1 Peak-to-valley height Rt

The peak-to-valley height Rt in μm acc. to DIN 4762 Part 1 is the distance of the base profile to the reference profile (see figure 1). The base profile is the reference profile displaced to

such an extent perpendicular to the geometrical ideal profile within the roughness reference length, that contacts the point of the actual profile most distant from the reference profile (point T in figure 1).

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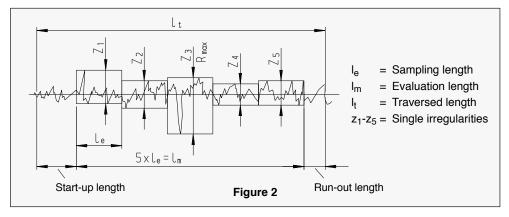


2.2 Mean peak-to-valley height Rz

The mean peak-to-valley height Rz in μm acc. to DIN 4768 is the arithmetic average of the single irregularities of five consecutive sam-

pling lengths (see figure 2).

Note: The definition given for Rz in DIN differs from its definition in ISO.



An exact conversion of the peak-to-valley height Rz into the centre line average height Ra and vice versa can neither be theoretically justified nor empirically proved. For surfaces which are generated by manufacturing methods of the group "metal cutting", a diagram for the conversion from Ra into Rz and vice versa is shown in supplement 1 to DIN 4768, based on comparison measurements. The Ra values assigned to the Rz values are subject to scattering (see table).

2.3 Maximum roughness height Rmax

The maximum roughness height Rmax in μm acc. to DIN 4768 is the largest of the single irregularities Z_1 occurring over the evaluation length I_m (see figure 2). Rmax is applied only in cases where the largest single irregularity ("runaway") is to be recorded for reasons important for function.

2.4 Roughness grade numbers N

In Germany, it is not allowed to use roughness grade numbers (N grades), since they are given in inches.

 Centre line average height Ra and roughness grade numbers in relation to the mean peak-to-valley height Rz 													
Surface rough- ness value	μm	50	25	12.5	6.3	3.2	1.6	0.8	0.4	0.2	0.1	0.05	0.025
Ra	μin	2000	1000	500	250	125	63	32	16	8	4	2	1
Roughness grad	de no.	N 12	N 11	N 10	N 9	N 8	N 7	N 6	N 5	N 4	N 3	N 2	N 1
Surface rough-	from	160	80	40	25	12.5	6.3	3.15	1.6	0.8	0.4	0.25	0.1
ness value Rz in μm	to	250	160	100	63	31.5	20	12.5	6.3	4	2.5	1.6	0.8

Technical Drawings

Geometrical Tolerancing

4. General

4.1 The particulars given are in accordance with the international standard DIN ISO 1101, March 1985 edition.

This standard gives the principles of symbolization and indication on technical drawings of tolerances of form, orientation, location and runout, and establishes the appropriate geometrical definition. The term "geometrical tolerances" is used in this standard as generic term for these tolerances.

4.2 Relationship between tolerances of size, form and position

According to current standards there are <u>two</u> possibilities of making indications on technical drawings in accordance with:

- a) the principle of independence according to DIN ISO 8015 where tolerances of size, form and position must be adhered to <u>independent</u> of each other, i.e. there is no direct relation between them. In this case reference must be made on the drawing to DIN ISO 8015.
- b) the envelope requirements according to DIN 7167, according to which the tolerances of size and form are in direct relation with each other, i.e. that the size tolerances limit the form tolerances.

5. Application; general explanations

- **5.1** Geometrical tolerances shall be specified on drawings only if they are imperative for the functioning and/or economical manufacture of the respective workpiece. Otherwise, the general tolerances according to DIN ISO 2768 apply.
- **5.2** Indicating geometrical tolerances does not necessarily imply the use of any particular method of production, measurement or gauging.
- **5.3** A geometrical tolerance applied to a feature defines the tolerance zone within which the feature (surface, axis, or median plane) is to be contained. According to the characteristic to be toleranced and the manner in which it is dimensioned, the tolerance zone is one of the following:
- the area within a circle;
- the area between two concentric circles:
- the area between two equidistant lines or two parallel straight lines;
- the space within a cylinder;
- the space between two coaxial cylinders;
- the space between two parallel planes;
- the space within a parallelepiped or a sphere.

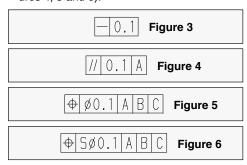
The toleranced feature may be of any form or orientation within this tolerance zone, unless a more restrictive indication is given.

- **5.4** Unless otherwise specified, the tolerance applies to the whole length or surface of the considered feature.
- **5.5** The datum feature is a real feature of a part, which is used to establish the location of a datum.
- **5.6** Geometrical tolerances which are assigned to features referred to a datum do not limit the form deviations of the datum feature itself. The form of a datum feature shall be sufficiently accurate for its purpose and it may therefore be necessary to specify tolerances of form for the datum features (see table on page 8).

5.7 Tolerance frame

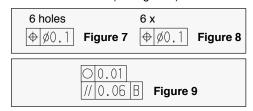
The tolerance requirements are shown in a rectangular frame which is divided into two or more compartments. These compartments contain, from top to bottom, in the following order (see figures 3, 4 and 5):

- the symbol for the characteristic to be toleranced;
- the tolerance value in the unit used for linear dimensions. This value is preceded by the symbol Ø if the tolerance zone is circular or cylindrical; or by the symbol "SØ" if the tolerance zone is spherical;
- if appropriate, the capital letter or letters identifying the datum feature or features (see figures 4, 5 and 6).



Remarks referred to the tolerance, for example "6 holes", "4 surfaces", or "6 x" shall be written above the frame (see figures 7 and 8).

If it is necessary to specify more than one tolerance characteristic for a feature, the tolerance specifications are given in tolerance frames one under the other (see figure 9).



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Table 1: Kinds of tolerances; symbols; included tolerances					
To	olerances	Toleranced characteristics	Included tolerances		
		Straightness		-	
		Flatness		Straightness	
Form	n tolerances	Circularity (Roundness)	\bigcirc	_	
		Cylindricity	\triangleright	Straightness, Parallelism, Circularity	
	Profile	Profile any line		_	
to	lerances	Profile any surface		-	
		Parallelism	//	Flatness	
	Orientation tolerances	Perpendicularity		Flatness	
_		Angularity	_	Flatness	
sition		Position	\oplus	-	
Folerances of position	Location tolerances	Concentricity (for centre points), Coaxiality (for axes)	0	-	
leranc		Symmetry	=	Straightness, Flatness, Parallelism	
ㅂ	Dunout	Circular runout	1	Circularity, Coaxiality, Concentricity	
Runout tolerances		Total runout	11	Concentricity, Coaxiality, Flatness, Parallelism, Perpendicularity	

Table 2: Additional symbols					
	Description		Symbols		
		direct	<i></i>		
Toleranced feature indica	Toleranced feature indications by letter				
Datum feature indication	(by letter only)		A A		
Datum target indication	Ø2 A1				
Theoretically exact dimer	50				
Projected tolerance zone	P				
Maximum material requir Dependent on dimension	(<u>x</u>)				
Least material requireme Dimension describing the					
Free state condition (non	F				
Envelope requirement: T geometrically ideal envel	E				

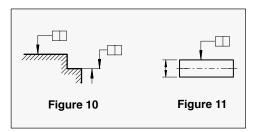
Technical Drawings

Geometrical Tolerancing

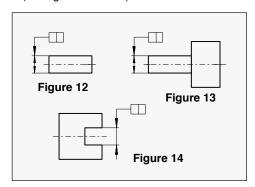
5.8 Toleranced features

The tolerance frame is connected to the toleranced feature by a leader line terminating with an arrow in the following way:

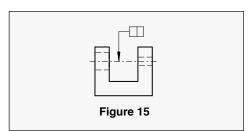
 on the outline of the feature or an extension of the outline (but clearly separated from the dimension line) when the tolerance refers to the line or surface itself (see figures 10 and 11).



 as an extension of a dimension line when the tolerance refers to the axis or median plane defined by the feature so dimensioned (see figures 12 to 14).



 on the axis or the median plane when the tolerance refers to the common axis or median plane of two or more features (see figure 15).

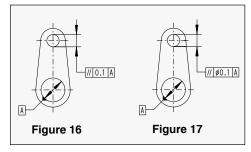


Note:

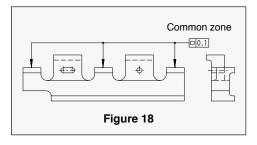
Whether a tolerance should be applied to the contour of a cylindrical or symmetrical feature or to its axis or median plane, depends on the functional requirements.

5.9 Tolerance zones

The tolerance zone is the zone within which all the points of a geometric feature (point, line, surface, median plane) must lie. The width of the tolerance zone is in the direction of the arrow of the leader line joining the tolerance frame to the feature which is toleranced, unless the tolerance value is preceded by the symbol \varnothing (see figures 16 and 17).



Where a <u>common tolerance zone</u> is applied to several separate features, the requirement is indicated by the words "common zone" above the tolerance frame (see figure 18).

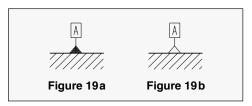


5.10 Datums and datum systems

Datum features are features according to which a workpiece is aligned for recording the toleranced deviations.

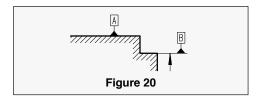
5.10.1 When a toleranced feature is referred to a datum, this is generally shown by datum letters. The same letter which defines the datum is repeated in the tolerance frame.

To identify the datum, a capital letter enclosed in a frame is connected to a datum triangle (see figures 19a and 19b).



The datum triangle with the datum letter is placed:

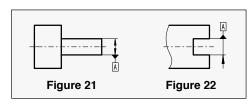
 on the outline of the feature or an extension of the outline (but clearly separated from the dimension line), when the datum feature is the line or surface itself (see figure 20).



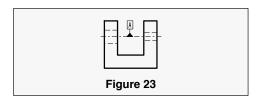
 as an extension of the dimension line when the datum feature is the axis or median plane (see figures 21 and 22).

Note:

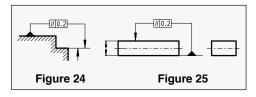
If there is not enough space for two arrows, one of them may be replaced by the datum triangle (see figure 22).



- on the axis or median plane when the datum is:
- a) the axis or median plane of a single feature (for example a cylinder);
- b) the common axis or median plane formed by two features (see figure 23).



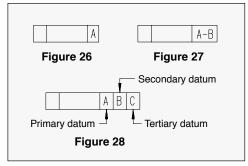
If the tolerance frame can be directly connected with the datum feature by a leader line, the datum letter may be omitted (see figures 24 and 25).



A single datum is identified by a capital letter (see figure 26).

A common datum formed by two datum features is identified by two datum letters separated by a hyphen (see figures 27 and 29).

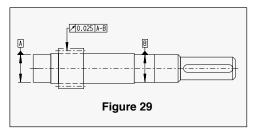
In a datum system (see also 5.10.2) the sequence of two or more datum features is important. The datum letters are to be placed in different compartments, where the sequence from left to right shows the order of priority, and the datum letter placed first should refer to the directional datum feature (see figures 28, 30 and 31).



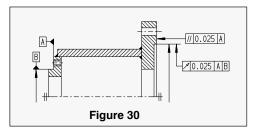
5.10.2 Datum system

A datum system is a group of two or more datums to which one toleranced feature refers in common. A datum system is frequently required because the <u>direction</u> of a <u>short axis</u> cannot be determined alone.

Datum formed by two form features (common datum):



Datum system formed by two datums (directional datum "A" and short axis "B").

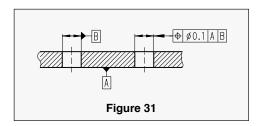


Technical Drawings

Geometrical Tolerancing

Datum system formed by one plane and one perpendicular axis of a cylinder:

Datum "A" is the plane formed by the plane contact surface. Datum "B" is the axis of the largest inscribed cylinder, the axis being at right angles with datum "A" (see figure 31).

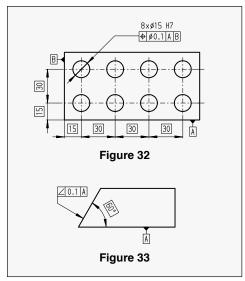


5.11 Theoretically exact dimensions

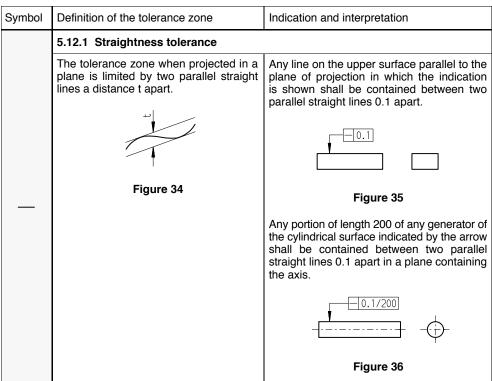
If tolerances of position or angularity are prescribed for a feature, the dimensions determining the theoretically exact position or angle shall not be toleranced.

These dimensions are enclosed, for example 30. The corresponding actual dimensions of the part are subject only to the position tolerance or angu-

larity tolerance specified within the tolerance frame (see figures 32 and 33).



5.12 Definitions of tolerances



Symbol	Definition of the tolerance zone	Indication and interpretation
	The tolerance zone is limited by a parallel- epiped of section $t_1 \cdot t_2$ if the tolerance is specified in two directions perpendicular to each other.	The axis of the bar shall be contained within a parallelepipedic zone of width 0.1 in the vertical and 0.2 in the horizontal direction.
	t ₂	
	Figure 37	Figure 38
	The tolerance zone is limited by a cylinder of diameter t if the tolerance value is preceded by the symbol \varnothing .	The axis of the cylinder to which the tolerance frame is connected shall be contained in a cylindrical zone of diameter 0.08.
	Figure 39	Figure 40
	5.12.2 Flatness tolerance	
	The tolerance zone is limited by two parallel planes a distance t apart.	The surface shall be contained between two parallel planes 0.08 apart.
		0.08
	Figure 41	Figure 42
	5.12.3 Circularity tolerance	
	The tolerance zone in the considered plane is limited by two concentric circles a distance t apart.	The circumference of each cross-section of the outside diameter shall be contained between two co-planar concentric circles 0.03 apart.
		(-(i))
\bigcirc	Figure 43	Figure 44
)		The circumference of each cross-section shall be contained between two co-planar concentric circles 0.1 apart.
		Figure 45

Technical Drawings Geometrical Tolerancing

Symbol	Definition of the tolerance zone	Indication and interpretation				
	5.12.4 Cylindricity tolerance					
\bowtie	The tolerance zone is limited by two coaxial cylinders a distance t apart.	The considered surface area shall be contained between two coaxial cylinders 0.1 apart.				
	Figure 46	Figure 47				
	5.12.5 Parallelism tolerance					
	Parallelism tolerance of a line with referen	nce to a datum line				
	The tolerance zone when projected in a plane is limited by two parallel straight lines a distance t apart and parallel to the datum line, if the tolerance zone is only specified in one direction.	The toleranced axis shall be contained between two straight lines 0.1 apart, which are parallel to the datum axis A and lie in the vertical direction (see figures 49 and 50).				
		Figure 49 Figure 50				
	Figure 48					
//	t	The toleranced axis shall be contained between two straight lines 0.1 apart, which are parallel to the datum axis A and lie in the horizontal direction.				
	Figure 51	Figure 52				
	The tolerance zone is limited by a parallel- epiped of section $\mathbf{t}_1 \cdot \mathbf{t}_2$ and parallel to the datum line if the tolerance is specified in two planes perpendicular to each other.	The toleranced axis shall be contained in a parallelepipedic tolerance zone having a width of 0.2 in the horizontal and 0.1 in the vertical direction and which is parallel to the datum axis A (see figures 54 and 55).				
	t ₂	//0.2A //0.1A //0.1A //0.1A				
	Figure 53	Figure 54 Figure 55				
	2 0000					

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Symbol	Definition of the tolerance zone	Indication and interpretation								
	Parallelism tolerance of a line with referer	nce to a datum line								
	The tolerance zone is limited by a cylinder of diameter t parallel to the datum line if the tolerance value is preceded by the symbol Ø.	The toleranced axis shall be contained in a cylindrical zone of diameter 0.03 parallel to the datum axis A (datum line).								
	Figure 56	∄ Figure 57								
	Parallelism tolerance of a line with referer	nce to a datum surface								
	The tolerance zone is limited by two parallel planes a distance t apart and parallel to the datum surface.	The toleranced axis of the hole shall be contained between two planes 0.01 apart and parallel to the datum surface B.								
		//[0.01]B								
		B								
	Figure 58	Figure 59								
	Parallelism tolerance of a surface with reference to a datum line									
//	The tolerance zone is limited by two parallel planes a distance t apart and parallel to the datum line.	The toleranced surface shall be contained between two planes 0.1 apart and parallel to the datum axis C of the hole.								
		(I)								
	Figure 60	Figure 61								
	Parallelism tolerance of a surface with ref	erence to a datum surface								
	The tolerance zone is limited by two parallel planes a distance t apart and parallel to the datum surface.	The toleranced surface shall be contained between two parallel planes 0.01 apart and parallel to the datum surface D (figure 63).								
		// 0.01 D // 0.01/100 A D A								
		Figure 63 Figure 64								
	Figure 62	All the points of the toleranced surface in a length of 100, placed anywhere on this surface, shall be contained between two parallel planes 0.01 apart and parallel to the datum surface A (figure 64).								

Svmbol Definition of the tolerance zone Indication and interpretation 5.12.6 Perpendicularity tolerance Perpendicularity tolerance of a line with reference to a datum line The tolerance zone when projected in a The toleranced axis of the inclined hole shall plane is limited by two parallel straight be contained between two parallel planes lines a distance t apart and perpendicular 0.06 apart and perpendicular to the axis of to the datum line. the horizontal hole A (datum line). Figure 65 Figure 66 Perpendicularity tolerance of a line with reference to a datum surface The toleranced axis of the cylinder, to which The tolerance zone when projected in a plane is limited by two parallel straight the tolerance frame is connected, shall be contained between two parallel planes 0.1 lines a distance t apart and perpendicular to the datum plane if the tolerance is specapart, perpendicular to the datum surface. ified only in one direction. Figure 67 Figure 68 The tolerance zone is limited by a parallel-The toleranced axis of the cylinder shall be epiped of section $t_1 \cdot t_2$ and perpendicular contained in a parallelepipedic tolerance to the datum surface if the tolerance is zone of 0.1 · 0.2 which is perpendicular to the specified in two directions perpendicular datum surface. to each other. Figure 69 Figure 70 The tolerance zone is limited by a cylinder The toleranced axis of the cylinder to which of diameter t perpendicular to the datum the tolerance frame is connected shall be surface if the tolerance value is preceded contained in a cylindrical zone of diameter 0.01 perpendicular to the datum surface A. by the symbol \emptyset . ⊥|ø0.01|A Figure 71 Figure 72

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Symbol	Definition of the tolerance zone	Indication and interpretation							
	Perpendicularity tolerance of a surface wi	th reference to a datum line							
	The tolerance zone is limited by two parallel planes a distance t apart and perpendicular to the datum line. Figure 73	be contained between two parallel planes 0.08 apart and perpendicular to the axis A (datum line).							
		Figure 74							
	Perpendicularity tolerance of a surface wi								
	The tolerance zone is limited by two parallel planes a distance t apart and perpendicular to the datum surface.	The toleranced surface shall be contained between two parallel planes 0.08 apart and perpendicular to the horizontal datum surface A.							
	Figure 75	Figure 76							
	5.12.7 Angularity tolerance								
	Angularity tolerance of a line with reference to a datum line								
	Line and datum line in the same plane. The tolerance zone when projected in a plane is limited by two parallel straight lines a distance t apart and inclined at the specified angle to the datum line.								
	t of the state of	(a) (b) (c) (c) (d) (d) (d) (d) (d) (d) (d) (d) (d) (d							
	Figure 77	Figure 78							
	Angularity tolerance of a surface with refe	erence to a datum surface							
	The tolerance zone is limited by two parallel planes a distance t apart and inclined at the specified angle to the datum surface.	The toleranced surface shall be contained between two parallel planes 0.08 apart which are inclined at 40° to the datum surface A.							
	t de la constant de l	(0.08 A) (0.08 A)							
	Figure 79	Figure 80							

Technical Drawings

Geometrical Tolerancing

Symbol Definition of the tolerance zone

Indication and interpretation

5.12.8 Positional tolerance

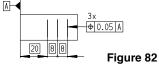
Positional tolerance of a line

The tolerance zone when projected in a plane is limited by two parallel straight lines a distance t apart and disposed symmetrically with respect to the theoretically exact position of the considered line if the tolerance is specified only in one direction.

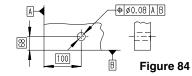


Figure 81

Each of the toleranced lines shall be contained between two parallel straight lines 0.05 apart which are symmetrically disposed about the theoretically exact position of the considered line, with reference to the surface A (datum surface).



The axis of the hole shall be contained within a cylindrical zone of diameter 0.08 the axis of which is in the theoretically exact position of the considered line, with reference to the surfaces A and B (datum surfaces).

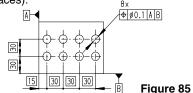


The tolerance zone is limited by a cylinder of diameter t the axis of which is in the theoretically exact position of the considered line if the tolerance value is preceded by the symbol \varnothing .



Figure 83

Each of the axes of the eight holes shall be contained within a cylindrical zone of diameter 0.1 the axis of which is in the theoretically exact position of the considered hole, with reference to the surfaces A and B (datum surfaces).



Positional tolerance of a flat surface or a median plane

The tolerance zone is limited by two parallel planes a distance t apart and disposed symmetrically with respect to the theoretically exact position of the considered surface.

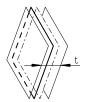


Figure 86

The inclined surface shall be contained between two parallel planes which are 0.05 apart and which are symmetrically disposed with respect to the theoretically exact position of the considered surface with reference to the datum surface A and the axis of the datum cylinder B (datum line).

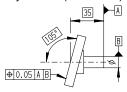


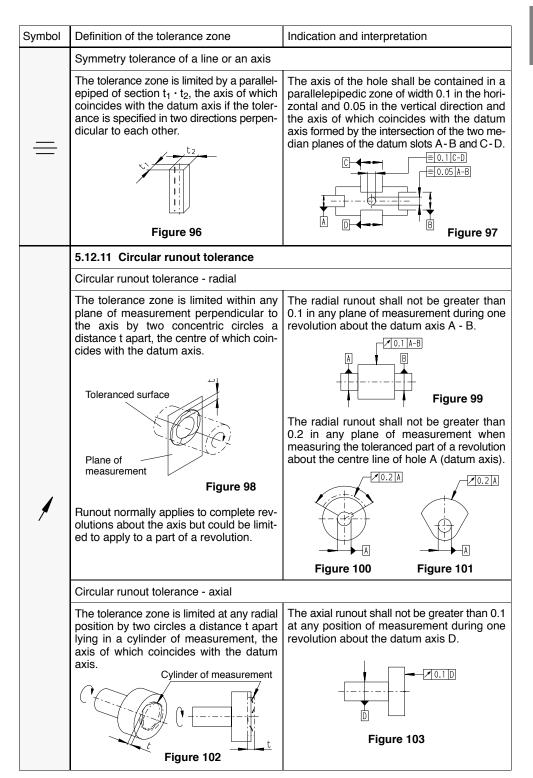
Figure 87

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Symbol Definition of the tolerance zone Indication and interpretation 5.12.9 Concentricity and coaxiality tolerance Concentricity tolerance of a point The tolerance zone is limited by a circle of The centre of the circle, to which the tolerdiameter t the centre of which coincides ance frame is connected, shall be contained with the datum point. in a circle of diameter 0.01 concentric with the centre of the datum circle A. \bigcirc Figure 88 Figure 89 Coaxiality tolerance of an axis The tolerance zone is limited by a cylinder The axis of the cylinder, to which the tolerof diameter t. the axis of which coincides ance frame is connected, shall be contained with the datum axis if the tolerance value in a cylindrical zone of diameter 0.08 coaxial is preceded by the symbol \emptyset . with the datum axis A - B. Figure 90 Figure 91 5.12.10 Symmetry Symmetry tolerance of a median plane The tolerance zone is limited by two paral-The median plane of the slot shall be containlel planes a distance t apart and disposed ed between two parallel planes, which are symmetrically to the median plane with 0.08 apart and symmetrically disposed about respect to the datum axis or datum plane. the median plane with respect to the datum feature A. Figure 92 Figure 93 Symmetry tolerance of a line or an axis The tolerance zone when projected in a The axis of the hole shall be contained beplane is limited by two parallel straight tween two parallel planes which are 0.08 lines a distance t apart and disposed symapart and symmetrically disposed with metrically with respect to the datum axis respect to the actual common median plane (or datum plane) if the tolerance is speciof the datum slots A and B. fied only in one direction. Figure 94 Figure 95

Technical Drawings

Geometrical Tolerancing



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Symbol	Definition of the tolerance zone	Indication and interpretation						
	Circular runout tolerance in any direction							
	The tolerance zone is limited within any cone of measurement, the axis of which coincides with the datum axis by two circles a distance t apart. Unless otherwise specified the measuring direction is normal to the surface. Cone of measurement	arrow shall not be greater than 0.1 in an cone of measurement during one revolution about the datum axis C.						
1	Figure 104							
	Circular runout tolerance in a specified direction							
	The tolerance zone is limited within any cone of measurement of the specified angle, the axis of which coincides with the datum axis by two circles a distance t apart.	The runout in the specified direction shall not be greater than 0.1 in any cone of measurement during one revolution about the datum axis C. Figure 107						
	5.12.12 Total runout tolerance							
	Total radial runout tolerance							
	The tolerance zone is limited by two coaxial cylinders a distance t apart, the axes of which coincide with the datum axis.	during several revolutions about the datum axis A-B, and with relative axial movement between part and measuring instrument.						
11		With relative movement the measuring instrument or the workpiece shall be guided along a line having the theoretically perfect form of the contour and being in correct position to the datum axis.						
	Figure 108	Figure 109						

Technical Drawings Geometrical Tolerancing

Symbol	Definition of the tolerance zone	Indication and interpretation
	Total axial runout tolerance	
1 1	The tolerance zone is limited by two parallel planes a distance t apart and perpendicular to the datum axis. Figure 110	The total axial runout shall not be greater than 0.1 at any point on the specified surface during several revolutions about the datum axis D and with relative radial movement between the measuring instrument and the part. With relative movement the measuring instrument or the workpiece shall be guided along a line having the theoretically perfect form of the contour and being in correct position to the datum axis.

Non-standard Formats

Technical drawings, extract from DIN EN ISO 5457.

6. Sheet sizes

The DIN EN ISO 5457 standard applies to the presentation of drawing forms even if they are

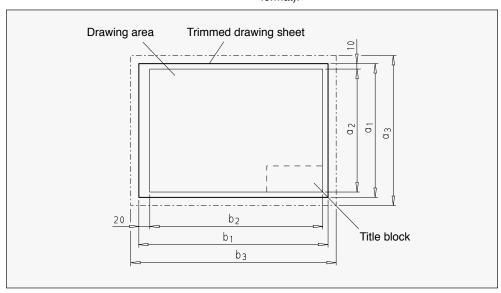
created by CAD. This standard may also be used for other technical documents. The sheet sizes listed below have been taken from DIN EN ISO 5457.

Table 3 Formats of trimmed and untrimmed sheets and of the drawing area										
Sheet sizes acc. to DIN EN ISO 5457, A series	Trimmed sheet a ₁ x b ₁ mm	Drawing area ¹⁾ a ₂ x b ₂ mm	Untrimmed sheet a ₃ x b ₃ mm							
Α0	841 x 1189	821 x 1159	880 x 1230							
A 1	594 x 841	574 x 811	625 x 880							
A 2	420 x 594	400 x 564	450 x 625							
A 3	297 x 420	277 x 390	330 x 450							
A 4	210 x 297	180 x 277	240 x 330							

 The actually available drawing area is reduced by the title block, the filing margin, the possible sectioning margin, etc.

6.1 Title block

Formats \geq A3 are produced in broadside. The title block area is in the bottom right corner of the trimmed sheet. For the A4 format the title block area is at the bottom of the short side (upright format).



6.2 Non-standard formats

Non-standard formats should be avoided. When necessary they should be created using the

dimensions of the short side of an A-format with the long side of a greater A-format.

Technical Drawings

Type Sizes, Lines Lettering Example

7. Type sizes

Table 4: Type sizes for drawing format	ts (h = type h	eight, b = line	width)					
	Paper sizes							
Application range for lettering	A0 ar	nd A1	A2, A3 and A4					
	h	b	Paper sizes A2, A3 and A4 h					
Type, drawing no.	10	1	7	0.7				
Texts and nominal dimensions	5	0.5	3.5	0.35				
Tolerances, roughness values, symbols	3.5	0.35	2.5	0.25				

7.1 The type sizes as assigned to the paper sizes in table 4 MUST be adhered to with regard to their application range. Larger type heights are

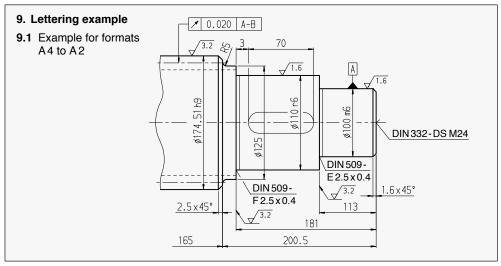
also permissible. Type heights smaller by approx. 20% will be accepted if this is required in a drawing because of restricted circumstances.

8. Lines acc. to DIN ISO 128, Part 20 and Part 24

Table 5: Line groups, line types and line widths										
Line group		0.5	0.7							
Drawing format		A4, A3, A2	A1, A0							
Line type		Line width								
Solid line (thick)		0.5	0.7							
Solid line (thin)		0.25	0.35							
Short dashes (thin) — — — -		0.25	0.35							
Dot-dash line (thick) — -		0.5	0.7							
Dot-dash line (thin)		0.25	0.35							
Dash/double-dot line (thin) ——		0.25	0.35							
Freehand (thin)		0.25	0.35							

8.1 Line groups 0.5 and 0.7 with the pertaining line width according to table 5 may only be used. Assignment to the drawing formats A1 and

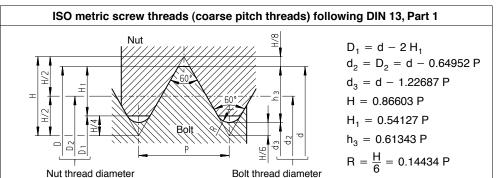
A0 is prescribed. For the A4, A3 and A2 formats, line group 0.7 may be used as well.



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Diameters of series 1 should be preferred to those of series 2, and these again to those of series 3.

Nominal thread diameter			Pitch	Pitch diameter	Core diameter		Depth o	f thread	Round	Tensile stress cross- section
	d = D		Р	$d_2 = D_2$	d_3	D_1	h ₃	H ₁	R	A _s 1)
Series 1	Series 2	Series 3	mm	mm	mm	mm	mm	mm	mm	mm ²
3			0.5	2.675	2.387	2.459	0.307	0.271	0.072	5.03
	3.5		0.6	3.110	2.764	2.850	0.368	0.325	0.087	6.78
4			0.7	3.545	3.141	3.242	0.429	0.379	0.101	8.78
	4.5		0.75	4.013	3.580	3.688	0.460	0.406	0.108	11.3
5			8.0	4.480	4.019	4.134	0.491	0.433	0.115	14.2
6			1	5.350	4.773	4.917	0.613	0.541	0.144	20.1
		7	1	6.350	5.773	5.917	0.613	0.541	0.144	28.9
8			1.25	7.188	6.466	6.647	0.767	0.677	0.180	36.6
		9	1.25	8.188	7.466	7.647	0.767	0.677	0.180 4	48.1
10			1.5	9.026	8.160	8.376	0.920	0.812	0.217	58.0
		11	1.5	10.026	9.160	9.376	0.920	0.812	0.217	72.3
12			1.75	10.863	9.853	10.106	1.074	0.947	0.253	84.3
	14		2	12.701	11.546	11.835	1.227	1.083	0.289	115
16			2	14.701	13.546	13.835	1.227	1.083	0.289	157
	18		2.5	16.376	14.933	15.294	1.534	1.353	0.361	193
20			2.5	18.376	16.933	17.294	1.534	1.353	0.361	245
	22		2.5	20.376	18.933	19.294	1.534	1.353	0.361	303
24			3	22.051	20.319	20.752	1.840	1.624	0.433	353
	27		3	25.051	23.319	23.752	1.840	1.624	0.433	459
30			3.5	27.727	25.706	26.211	2.147	1.894	0.505	561
	33		3.5	30.727	28.706	29.211	2.147	1.894	0.505	694
36			4	33.402	31.093	31.670	2.454	2.165	0.577	817
	39		4	36.402	34.093	34.670	2.454	2.165	0.577	976
42			4.5	39.077	36.479	37.129	2.760	2.436	0.650	1121
	45		4.5	42.077	39.479	40.129	2.760	2.436	0.650	1306
48			5	44.752	41.866	42.587	3.067	2.706	0.722	1473
	52		5	48.752	45.866	46.587	3.067	2.706	0.722	1758
56			5.5	52.428	49.252	50.046	3.374	2.977	0.794	2030
	60		5.5	56.428	53.252	54.046	3.374	2.977	0.794	2362
64			6	60.103	56.639	57.505	3.681	3.248	0.866	2676
	68		6	64.103	60.639	61.505	3.681	3.248	0.866	3055

1) The tensile stress cross-section is calculated acc. to DIN 13 Part 28 with formula

$$A_{s} = \frac{\pi}{4} \cdot \left(\frac{d_2 + d_3}{2}\right)^2$$

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Selection of nominal thread diameters and pitches for coarse and fine pitch threads from 1 mm to 68 mm diameter, following DIN ISO 261

Nominal thread diameter d = D			Coarse pitch	Pitches P for fine pitch threads							
Series 1	Series 2	Series 3	thread	4	3	2	1.5	1.25	1	0.75	0.5
1 1.2	1.4		0.25 0.25 0.3								
1.6 2	1.8		0.35 0.35 0.4								
2.5 3	2.2		0.45 0.45 0.5								
4 5	3.5		0.6 0.7 0.8								0.5 0.5
6 8 10			1 1.25 1.5					1.25	1	0.75 0.75 0.75	0.5 0.5
12	14	15	1.75 2				1.5 1.5 1.5	1.25 1.25	1 1 1		
16	18	17	2 2.5			2	1.5 1.5		1 1 1		
20 24	22		2.5 2.5 3			2 2 2	1.5 1.5 1.5		1 1 1		
	27	25 26	3			2	1.5 1.5 1.5				
30		28 32	3.5			2	1.5 1.5 1.5				
36	33	35	3.5 4		3	2	1.5 1.5 1.5				
	39	38 40	4		3	2	1.5 1.5				
42 48	45		4.5 4.5 5		3 3 3	2 2 2	1.5 1.5 1.5				
	52	50 55	5		3	2 2	1.5 1.5 1.5				
56	60	58	5.5 5.5	4	3	2 2	1.5 1.5 1.5				
64	68	65	6 6	4	3	2 2 2					

	Cylindrical shaft ends								Cylindrical shaft ends						
Acc. to DIN 748/1					FLENDER works standard W 0470				Acc. to DIN 748/1				FLENDER works standard W 0470		
Di me Ser	ter	ISO toler- ance	Leng Long	gth Short	Dia- meter	Length	ISO toler- ance	Di me Ser	ter	ISO toler- ance	Len Long	gth Short	Dia- meter	Length	ISO toler- ance
1	2	zone					zone	1	2	zone					zone
mm 6	mm		mm 16	mm	mm	mm		mm 100	mm		mm 210	mm 165	mm 100	mm	m6
7			16					110			210	165	110	180	
8			20					120	130		210 250	165 200	120 130	210	
9			20					140	100		250	200	140		
10			23	15					150		250	200	150	240	
11 12			23 30	15 18				160	170		300 300	240 240	160 170	270	
14 16			30 40	18 28	14 16	30		180 200	190		300 350 350	240 280 280	180 190 200	310	
19 20 22		k6	40 50 50	28 36 36	19 20 22	35	k6	220			350	280	220	350	
24 25			50 60	36 42	24 25	40		250	240260		410 410 410	330 330 330	240 250 260	400	
28 30			60 80	42 58	28 30	50		280		m6	470	380	280	450	n6
32 35 38			80 80 80	58 58 58	32 35 38	60		320	300	1110	470 470	380 380	300 320	500	
40 42			110 110	82 82	40 42	70		360	340		550 550	450 450	340	550 590	
45 48 50			110 110 110	82 82 82	45 48 50	80	0	400	380 420		550 650 650	450 540 540	380 400 420	650	
55			110	82	55	90	m6		440		650	540	440	690	
60 65			140 140	105 105	60 65	105		450	460		650 650	540 540	450 460	750	
70 75		m6	140 140	105 105	70 75	120		500	480		650 650	540 540	480 500	790	
80 85			170 170	130 130	80 85	140		560	530		800 800	680 680			
90 95			170 170	130 130	90 95	160		630	600		800 800	680 680			

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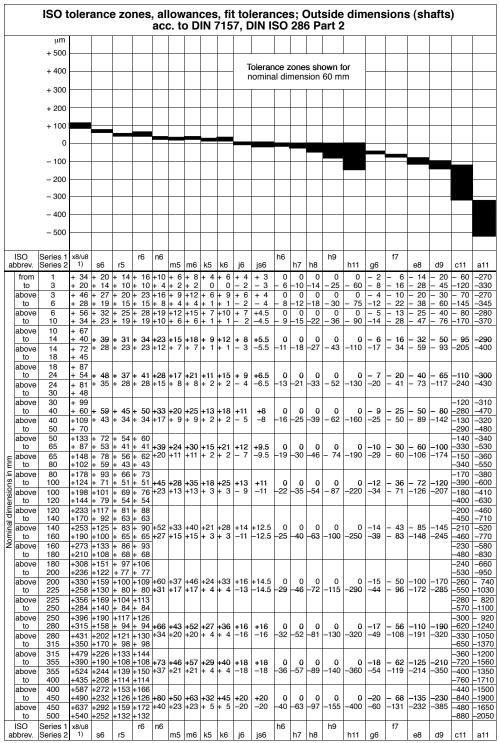
ISO Tolerance Zones, Allowances, Fit Tolerances Inside Dimensions (Holes)

	ISO	toler	ance	zon	es, a acc	llowa . to [ances	s, fit 157,	toler DIN	ance	s; In: 286 P	side art 2	dime	ensio	ns (h	noles)	
	μm							,										
	+ 500											,						
	+ 400						Tolerance zones shown for nominal dimension 60 mm											
	+ 300																	
+ 200																		
	+ 100																	
0 - 100 - 200 - 300																		
	- 400																	
	- 500																	
ISO abbrev.	Series 1 Series 2	P7	N7	N9	M7	K7	J6	J7	H7	Н8	H11	G7	F8	E9	D9	D10	C11	A11
from to	1 3	- 6 -16	- 4 -14	- 4 -29	- 2 -12	0 -10	+ 2	+ 4	+10	+14	+ 60	+12 + 2	+ 20 + 6	+ 39 + 14	+ 45 + 20	+ 60 + 20	+120 + 60	+330 +270
above	3	- 8	- 4	0	0	+ 3	+ 5	+ 6	+12	+18	+ 75	+16	+ 28	+ 50	+ 60	+ 78	+145	+345
to above	6	-20 - 9	-16 - 4	-30 0	-12 0	- 9 + 5	- 3 + 5	- 6 + 8	+15	+22	90	+20	+ 10	+ 20	+ 30	+ 30	+ 70	+270
to above	10 10	-24	-19	-36	-15	-10	- 4	- 7	0	0	0	+ 5	+ 13	+ 25	+ 40	+ 40	+ 80	+280
to above	14 14	-11 -29	- 5 -23	0 -43	0 -18	+ 6 -12	+ 6 - 5	+10 - 8	+18 0	+27 0	+110 0	+24	+ 43 + 16	+ 75 + 32	+ 93 + 50	+120 + 50	+205 + 95	+400 +290
to	18																	
to	24	-14 -35	- 7 -28	0 -52	0 -21	+ 6 -15	+ 8 - 5	+12 - 9	+21 0	+33	+130 0	+28 + 7	+ 53 + 20	+ 92 + 40	+117 + 65	+149 + 65	+240 +110	+430 +300
above to	24 30	-33	-20	-32	-21	-13	- 3	- 3	U	U	U	т /	+ 20	+ 40	+ 03	+ 05		
above to	30 40	-17	- 8	0	0	+ 7	+10	+14	+25	+39	+160	+34	+ 64	+112	+142	+180	+280 +120	+470 +310
above to	40 50	-42	-33	-62	-25	-18	- 6	-11	0	0	0	+ 9	+ 25	+ 50	+ 80	+ 80	+290 +130	+480 +320
above to	50 65	-21	- 9	0	0	+ 9	+13	+18	+30	+46	+190	+40	+ 76	+134	+174	+220	+330 +140	+530 +340
E above E to	65 80	-51	-39	-74	-30	-21	- 6	-12	0	0	0	+10	+ 30	+ 60	+100	+100	+340 +150	+550 +360
above to above to	80 100	-24	-10	0	0	+10	+16	+22	+35	+54	+220	+47	+ 90	+159	+207	+260	+390 +170	+600
above to	100 120	-59	-45	-87	-35	-25	- 6	-13	0	0	0	+12	+ 36	+ 72	+120	+120	+400 +180	+630
	120																+450	+710 +460
above to	140	-28	-12	0	0	+12	+18	+26	+40	+63	+250	+54	+106	+185	+245	+305	+200	+770
above	160	-68	-52	-100	-40	-28	- 7	-14	0	0	0	+14	+ 43	+ 85	+145	+145	+210	+520
to above	180 180																+230	+580
to above	200 200	-33	-14	0	0	+13	+22	+30	+46	+72	+290	+61	+122	+215	+285	+355	+240 +550	+660
to above	225 225	-79	-60	-115	-46	-33	- 7	-16	0	0	0	+15			+170			+ 740
to above	250 250																+280	+ 820
to	280 280	-36 -88	-14 -66	0 -130	0 -52	+16 -36	+25 - 7	+36 -16	+52	+81 0	+320	+69 +17	+137 + 56	+240 +110	+320 +190	+400 +190	+300	
to	315	"	30		32	30							. 55	0			+330	+1050
above to	355	-41	-16	0	0	+17	+29	+39	+57	+89	+360	+75	+151	+265	+350	+440	+360	+1560
above to	400	-98	-73	-140	- 57	-40	- 7	-18	0	0	0	+18	+ 62	+125	+210	+210	+400	+1710 +1350
above to	400 450	- 45	-17	0	0	+18	+33	+43	+63	+97	+400	+83	+165	+290	+385	+480	+840 +440	+1900 +1500
above to		-108	-80	-155	-63	-45	- 7	-20	0	0	0	+20	+ 68	+135	+230	+230	+880 +480	+2050
ISO	Series 1	D-7	NI-	No		1/7	10	17	H7	H8	1122	67	F8	E9	Do	D10	C11	
abbrev.	Series 2	P7	N7	N9	M7	K7	J6	J7	L	L	H11	G7		L	D9			A11

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Standardization

ISO Tolerance Zones, Allowances, Fit Tolerances Outside Dimensions (Shafts)



¹⁾ Up to nominal dimension 24 mm: x8; above nominal dimension 24 mm: u8

Parallel Keys, Taper Keys, and Centre Holes

Dimensions of parallel keys and taper keys											Develled keyes and tener keyes			
Diam	ameter Width		Height	Depth of key- way in shaft	Dept keyw hu	Lengths, see below				Parallel keys and taper keys acc. to DIN 6885 Part 1, 6886 and 6887 Side fitting square and rectangular keys				
d		b	h	t ₁	t ₂	,	Į.	1	l i			l 1		
					DĪ	N		DI	N			William 5		
above	to	1)	2)		6885/1	6886/ 6887 2)	688		68					
mm	mm	mm	mm	mm	mm	mm	from mm	to mm	from mm	to mm		1-		
6	8	2	2	1.2	1.0	0.5	6	20	6	20		<u>d1</u>		
8 10	10 12	3 4	3 4	1.8 2.5	1.4 1.8	0.9 1.2	6 8	36 45	8 10	36 45		Parallel key and keyway acc. to DIN 6885 Part 1		
12	17	5	5	3	2.3	1.7	10	56	12	56		Square and rectangular taper keys		
17	22	6	6	3.5	2.8	2.2	14	70	16	70		- l - b -		
30	30	10	7	4 5	3.3	2.4	18 22	90	20 25	90		15 000 S		
38	44	12	8	5	3.3	2.4	28	140	32	140		1:100		
44	50	14	9	5.5	3.8	2.9	36	160	40	160		+		
50	58	16	10	6	4.3	3.4	45	180	45	180		5		
58 65	65 75	18	11 12	7 7.5	4.4	3.4 3.9	50	200	50 56	200		d = d =		
75	85	20	14	7.5	4.9 5.4	4.4	56 63	220 250	63	220 250		Taper and round-ended sunk key and		
85	95	25	14	9	5.4	4.4	70	280	70	280		keyway acc. to DIN 6886		
95	110	28	16	10	6.4	5.4	80	320	80	320	1)	The tolerance zone for hub keyway width b for		
110	130	32	18	11	7.4	6.4	90	360	90	360		parallel keys with normal fit is ISO JS9 and		
130	150	36	20	12	8.4	7.1	100	400	100	400	i	with close fit ISO P9. The tolerance zone for		
150	170	40	22	13	9.4	8.1	110	400	110	400		shaft keyway width b with normal fit is ISO N9		
170 200	200 230	45 50	25 28	15 17	10.4 11.4	9.1 10.1	125 140	400 400	125 140	400 400		and with close fit ISO P9.		
230	260	56	32	20	12.4	11.1	160	400	140	400		Dimension h of the taper key names the		
260	290	63	32	20	12.4	11.1	180	400				largest height of the key, and dimension t_z the largest depth of the hub keyway. The shaft		
290	330	70	36	22	14.4	13.1	200	400	Leng			keyway and hub keyway dimensions		
330	380	80	40	25	15.4	14.1	220	400	no det			according to DIN 6887 - taper keys with gib		
380	440	90	45	28	17.4	16.1	250	400	min			head - are equal to those of DIN 6886.		
440	500	100	50	31	19.5	18.1	280	400	<u> </u>		32			
	igths I ₁ or I		6 8 10 12 14 16 18 20 22 25 28 90 100 110 125 140 160 180 200 22									2 36 40 45 50 56 63 70 80 250 280 320 360 400		

Dimensions of 60° centre holes in mm												Centre holes
Recommended diameters		Bore diameter			3			Minimum dimensions		in shaft ends (centerings) acc. to DIN 332 Part 1		
d ²⁾ above to		d ₁		a 1) b		(d ₂	d ₃		t		
6	10	1.6	6	5.5	0.5		3.35	5		3.4		
10	25	2 2.5		6.6 8.3	0.6		4.25 6.3 5.3 8			4.3 5.4		5 (5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
25	63	3.15		10 0.			5.7	10		6.8		
		4		12.7	1.2	- 1	3.5	12.5		8.6		Form B
63	100	5 6.3		15.6 20	1.6).6 3.2	16 18		10.8 12.9		DIN 332/1
	mended eters				1	Form	DS			t ₂		
diam d ₆	2)	d ₁	d_2	d_3	d_4	d_5	t ₁	t_2	t_3	t ₄	t ₅	 1 ,
above	to		3)	_			+2	min.	+1	~	~	Keyway t41
7	10	МЗ	2.5		5.3	5.8	9	12	2.6	1.8	0.2	$\frac{1}{2}$
10 13	13 16	M4 M5	3.3 4.2	4.3 5.3	6.7 8.1	7.4 8.8	10 12.5	14 17	3.2 4	2.1	0.3	
16	21	M6	5	6.4		10.5	16	21	5	2.8	0.4	8 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
21	24	M8	6.8		12.2		19	25	6	3.3	0.4	
24	30	M10	_	10.5				30	7.5	3.8		Form DS (with thread)
30 38	38 50	M12 M16	10.2 14	13 17	18.1 23	19.8 25.3	28 36	37 45	9.5 12	4.4 5.2	0.7 1.0	DIN 332/2
50	85	M20	17.5		28.4		42	53	15	6.4	1.3	Cutting-off dimension in case of no centering
85	130	M24	21		34.2		50	63	18	8	1.6	Diameter applies to finished workpiece
130		M30*	26	31	44	48	60	77	17	11	1.9	* Dimensions not acc. to DIN 332 Part 2
225		M36*	31.5	37	55	60 71	74	93	22	15	2.3	Drill diameter for tapping-size holes acc. to DIN 336 Part 1
320	500	M42*	37	43	65	/1	84	105	26	19	2.7	Dire occ i ait i

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Internationally determined prefixes

Decimal multiples and sub-multiples of units are represented with prefixes and symbols. Prefixes and symbols are used only in combination with unit names and unit symbols.

Factor by which the unit is multiplied	Prefix	Symbol	Factor by which the unit is multiplied	Prefix	Symbol
10 ⁻¹⁸	Atto	а	10 ¹	Deka	da
10 ⁻¹⁵	Femto	f	10 ²	Hecto	h
10 ⁻¹²	Pico	р	10 ³	Kilo	k
10 ⁻⁹	Nano	n	10 ⁶	Mega	М
10 ⁻⁶	Micro	μ	10 ⁹	Giga	G
10 ⁻³	Milli	m	10 ¹²	Tera	Т
10 ⁻²	Centi	С	10 ¹⁵	Peta	Р
10 ⁻¹	Deci	d	10 ¹⁸	Exa	Е

 Prefix symbols and unit symbols are written – without blanks and together they form the symbol for a new unit. An exponent on the unit symbol also applies to the prefix symbol.

Example:

1 cm³ = 1 ·
$$(10^{-2}\text{m})^3$$
 = 1 · 10^{-6}m^3
1 μ s = 1 · 10^{-6}s
10⁶s⁻¹ = 10⁶Hz = 1 MHz

 Prefixes are not used with the basic SI unit kilogram (kg) but with the unit gram (g).

Example:

Milligram (mg), NOT microkilogram (µkg).

When giving sizes by using prefix symbols and unit symbols, the prefixes should be chosen in such a way that the numerical values are between 0.1 and 1000.

Example:

12 kN instead of 1.2 · 10⁴N 3.94 mm instead of 0.00394 m 1.401 kPa instead of 1401 Pa 31 ns instead of 3.1 · 10⁻⁸s

 Combinations of prefixes and the following units are not allowed:

Units of angularity: degree, minute, second Units of time: minute, hour, year, day Unit of temperature: degree Celsius

Basic SI units						
Dhysical quantity	Basic SI unit		Physical quantity	Basic SI unit		
Physical quantity	Name	Symbol	Physical quantity Name		Symbol	
Length	Metre	m	Thermodynamic	Kelvin	к	
Mass	Kilogram	kg	temperature	Keivin	K	
Time	Second	S	Amount of substance	Mol	mol	
Electric current	Ampere	Α	Luminous intensity	Candela	cd	

Physics Derived SI Units Legal Units Outside the SI

Derived SI units having special names and special unit symbols					
Physical quantity	SI unit Name		Relation		
Plane angle	Radian	rad	1 rad = 1 m/m		
Solid angle	Steradian	sr	$1 \text{ sr} = 1 \text{ m}^2/\text{m}^2$		
Frequency, cycles per second	Hertz	Hz	1 Hz = 1 s ⁻¹		
Force	Newton	N	1 N = 1 kg·m/s ²		
Pressure, mechanical stress	Pascal	Pa	1 Pa = 1 N/m ² = 1 kg/ (m·s ²)		
Energy; work; quantity of heat	Joule	J	$1 J = 1 N \cdot m = 1 W \cdot s = 1 kg \cdot m^2/s^2$		
Power, heat flow	Watt	W	1 W = 1 J/s = 1 kg \cdot m ² /s ³		
Electric charge	Coulomb	С	1 C = 1 A·s		
Electric potential	Volt	V	$1 \text{ V} = 1 \text{ J/C} = 1 \text{ (kg} \cdot \text{m}^2)/(\text{A} \cdot \text{s}^3)$		
Electric capacitance	Farad	F	$1 F = 1 C/V = 1 (A^2 \cdot s^4)/(kg \cdot m^2)$		
Electric resistance	Ohm	Ω	1 Ω = 1 V/A = 1 (kg·m ²)/A ² ·s ³)		
Electric conductance	Siemens	S	1 S = 1 Ω^{-1} = 1 (A ² · s ³)/(kg · m ²)		
Celsius temperature	degrees Celsius	°C	0 °C = 273.15 K Δ1 °C = Δ1 K		
Inductance	Henry	Н	1 H = 1 V·s/A		

Legal units outside the SI						
Physical quantity	Unit name	Unit symbol	Definition			
Plane angle	Round angle Gon Degree Minute Second	1) gon ° 2) , 2) " 2)	1 perigon = 2π rad 1 gon = $(\pi/200)$ rad 1° = $(\pi/180)$ rad 1' = $(1/60)$ ° 1" = $(1/60)$ '			
Volume	Litre	1	$1 I = 1 dm^3 = (1/1000) m^3$			
Time	Minute Hour Day Year	min ²⁾ h ²⁾ d ²⁾ a ²⁾	1 min = 60 s 1 h = 60 min = 3600 s 1 d = 24 h = 86400 s 1 a = 365 d = 8760 h			
Mass	Ton	t	$1 t = 10^3 kg = 1 Mg$			
Pressure	Bar	bar	1 bar = 10 ⁵ Pa			

- 1) A symbol for the round angle has not been internationally determined
- 2) Do not use with prefixes

	Physical quantities and units of lengths and their powers				
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
I	Length	m (metre)	N.: Basic unit L.U.: μ m; mm; cm; dm; km; etc. N.A.: micron (μ): 1 μ = 1 μ m Ångström (Å): 1 Å = 10 ⁻¹⁰ m		
А	Area	m ² (square metre)	L.U.: mm^2 ; cm^2 ; dm^2 ; km^2 are (a): 1 a = 10^2 m^2 hectare (ha): 1 ha = 10^4 m^2		
V	Volume	m ³ (cubic metre)	L.U.: mm^3 ; cm^3 ; dm^3 litre (l): 1 l = 1 dm^3		
Н	Moment of area	m ³	N.: moment of a force; moment of resistance L.U.: mm ³ ; cm ³		
I	Second moment of area	m ⁴	N.: formerly: geometrical moment of inertia L.U.: mm ⁴ ; cm ⁴		
αβγ	Plane angle	rad (radian)	N.: 1 rad = $\frac{1 \text{ m (arc)}}{1 \text{ m (radius)}} = \frac{1 \text{ m}}{1 \text{ m}} = 1 \text{m/m}$ 1 rad 1 degree = $1^{\circ} = \frac{\pi}{180}$ rad 90° = $\frac{\pi}{2}$ rad L.U.: μ rad, mrad Degree (°): $1^{\circ} = \frac{\pi}{180}$ rad Minute ('): $1' = \frac{1^{\circ}}{60}$ Second (''): $1'' = \frac{1'}{60}$ Gon (gon): 1 gon = $\frac{\pi}{200}$ rad N.A.: Right angle (L): $1L = \frac{\pi}{2}$ rad Centesimal degree (g): $1g = 1$ gon Centesimal minute (°): $1^{\circ} = \frac{1}{100}$ gon Centesimal second (°°): $1^{\circ} = \frac{1}{100}$		
Ω ω	Solid angle	sr (steradian)	N.: 1 sr = $\frac{1 \text{ m}^2 \text{ (spherical surface)}}{1 \text{ m}^2 \text{ (square of spherical radius)}} = 1 \frac{\text{m}^2}{\text{m}^2}$		

PhysicsPhysical Quantities and Units of Time and of Mechanics

	Physical quantities and units of time					
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed			
t	Time, Period, Duration	s (second)	N.: Basic unit L.U.: ns; μs; ms; ks Minute (min): 1 min = 60 s Hour (h): 1 h = 60 min Day (d): 1 d = 24 h Year (a): 1 a = 365 d (Do not use prefixes for decimal multiples and sub-multiples of min; h; d; a)			
f	Frequency, Periodic frequency	Hz (Hertz)	L.U.: kHz; MHz; GHz; THz Hertz (Hz): 1 Hz = 1/s			
n	Rotational frequency (speed)	s ⁻¹	N.: Reciprocal value of the duration of one revolution L.U.: min ⁻¹ = 1/min			
٧	Velocity	m/s	L.U.: cm/s; m/h; km/s; km/h $1 \text{ km/h} = \frac{1}{3.6} \text{ m/s}$			
а	Acceleration, linear	m/s ²	N.: Time-related velocity L.U.: cm/s ²			
g	Gravity	m/s ²	N.: Gravity varies locally. Normal gravity (g_n) : $g_n = 9.80665 \text{ m/s}^2 \approx 9.81 \text{ m/s}^2$			
ω	Angular velocity	rad/s	L.U.: rad/min			
α	Angular acceleration	rad/s ²	L.U.: °/s²			
Ÿ	Volume flow rate	m ³ /s	L.U.: I/s; I/min; dm³/s; I/h; m³/h; etc.			

	Physical quantities and units of mechanics				
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
m	Mass	kg (kilogram)	N.: Basic unit L.U.: μg; mg; g; Mg ton (t): 1 t = 1000 kg		
m'	Mass per unit length	kg/m	N.: m' = m/l L.U.: mg/m; g/km In the textile industry: Tex (tex): 1 tex = 10 ⁻⁶ kg/m = 1 g/km		
m"	Mass in relation to the surface	kg/m²	N.: m" = m/A L.U.: g/mm ² ; g/m ² ; t/m ²		

Physical quantities and units of mechanics (continued)					
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
б	Density	kg/m ³	N.: $\varrho = m/V$ L.U.: g/cm^3 ; kg/dm^3 ; Mg/m^3 ; t/m^3 ; kg/l $1g/cm^3 = 1 kg/dm^3 = 1 Mg/m^3 =$ $1 t/m^3 = 1 kg/l$		
J	Mass moment of inertia; second mass moment	kg ⋅ m²	N.: Instead of the former flywheel effect GD ² $GD^2 \text{ in kpm}^2 \text{ now}: J = \frac{GD^2}{4}$ L.U.: $g \cdot m^2$; $t \cdot m^2$		
ṁ	Rate of mass flow	kg/s	L.U.: kg/h; t/h		
F	Force	N (Newton)	L.U.: μ N; mN; kN; MN; etc.; 1 N = 1 kg m/s ² N.A.: kp (1 kp = 9.80665 N)		
G	Weight	N (Newton)	N.: Weight = mass acceleration due to gravity L.U.: kN; MN; GN; etc.		
M, T	Torque	Nm	L.U.: µNm; mNm; kNm; MNm; etc. N.A.: kpm; pcm; pmm; etc.		
M _b	Bending moment	Nm	L.U.: Nmm; Ncm; kNm; etc. N.A.: kpm; kpcm; kpmm; etc.		
p	Pressure	Pa (Pascal)	N.: 1 Pa = 1 N/m ² L.U.: Bar (bar): 1 bar = 100000 Pa = 10 ⁵ Pa µbar; mbar N.A.: kp/cm ² ; at; ata; atü; mmWS; mmHg; Torr 1kp/cm ² = 1 at = 0.980665 bar 1 atm = 101325 Pa = 1.01325 bar 1 Torr = 101325 Pa = 133.322 Pa 1 mWS = 9806.65 Pa = 9806.65 N/m ² 1 mmHg = 133.322 Pa = 133.322 N/m ²		
p _{abs}	Absolute pressure	Pa (Pascal)			
P _{amb}	Ambient atmospheric pressure	Pa (Pascal)			
p _e	Pressure above atmospheric	Pa (Pascal)	$p_e = p_{abs} - p_{amb}$		
σ	Direct stress (tensile and compressive stress)	N/m²	L.U.: N/mm^2 1 $N/mm^2 = 10^6 N/m^2 = 1 MPa$		
τ	Shearing stress	N/m ²	L.U.: N/mm ²		
ε	Extension	m/m	N.: ΔI / I L.U.: μm/m; cm/m; mm/m		

PhysicsPhysical Quantities and Units of Mechanics,
Thermodynamics and Heat Transfer

	Physical quantities and units of mechanics (continued)				
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
W, A	Work	J	N.: 1 J = 1 Nm = 1 Ws L.U.: mJ; kJ; MJ; GJ; TJ; kWh 1 kWh = 3.6 MJ		
E, W	Energy	(Joule)	N.A.: kpm; cal; kcal 1 cal = 4.1868 J; 860 kcal = 1 kWh		
Р	Power	W (Watt)	L.U.:	N.: 1 W = 1 J/s = 1 Nm/s L.U.: μW; mW; kW; MW; etc. kJ/s; kJ/h; MJ/h; etc. N.A.: PS; kpm/s; kcal/h	
Q	Heat flow		1 PS = 735.49875 W 1 kpm/s = 9.81 W 1 kcal/h = 1.16 W 1 hp = 745.70 W		
η	Dynamic viscosity	Pa·s	N.: 1 Pa·s = 1 Ns/m ² L.U.: dPa·s; mPa·s N.A.: Poise (P): 1 P = 0.1 Pa·s		
v	Kinematic viscosity	m²/s	L.U.: mm ² /s; cm ² /s N.A.: Stokes (St): 1 St = 1/10000 m ² /s 1cSt = 1 mm ² /s		

	Physical quantities and units of thermodynamics and heat transfer				
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
Т	Thermo- dynamic temperature	K (Kelvin)	N.: Basic unit 273.15 K = 0 °C 373.15 K = 100 °C L.U.: mK		
t	Celsius temperature	°C	N.: The degrees Celsius (°C) is a special name for the degrees Kelvin (K) when stating Celsius temperatures. The temperature interval of 1 K equals that of 1 °C.		
Q	Heat, Quantity of heat	J	1 J = 1 Nm = 1 Ws L.U.: mJ; kJ; MJ; GJ; TJ N.A.: cal; kcal		
а	Temperature conductivity	m²/s	$\begin{split} a &= \frac{\lambda}{\varrho \cdot c_p} \\ \lambda \left[W/(m \cdot K) \right] &= \text{ thermal conductivity} \\ \varrho \left[kg/m^3 \right] &= \text{ density of the body} \\ c_p \left[J/(kg \cdot K) \right] &= \text{ specific heat capacity} \\ \text{ at constant pressure} \end{split}$		

PhysicsPhysical Quantities and Units of Thermodynamics,
Heat Transfer and Electrical Engineering

Phy	Physical quantities and units of thermodynamics and heat transfer (continued)					
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed			
Н	Enthalpy (Heat content)	J	N.: Quantity of heat absorbed under certain conditions L.U.: kJ; MJ; etc. N.A.: cal; Mcal; etc.			
S	Entropy	J/K	1 J/K = 1 Ws/K = 1 Nm/K L.U.: kJ/K N.A.: kcal/deg; kcal/°K			
α h	Heat transfer coefficient	W/(m ² ·K)	L.U.: W/(cm ² · K); kJ/(m ² · h · K) N.A.: cal/(cm ² · s · grd) kcal/(m ² · h · grd) $\approx 4.2 \text{ kJ/(m}^2 \cdot h \cdot \text{K)}$			
С	Specific heat capacity	J/(K·kg)	1 J/(K·kg) = W·s/(kg·K) N.: Heat capacity referred to mass N.A.: cal/(g·grd); kcal/(kg·grd); etc.			
α_{I}	Coefficient of linear thermal expansion	K ⁻¹	$ \begin{array}{ll} m/(m\cdot K) = K^{-1} \\ \text{N.:} & \text{Temperature unit/length unit ratio} \\ \text{L.U.:} & \mu m/(m\cdot K); \ cm/(m\cdot K); \ mm/(m\cdot K) \end{array} $			
α_{V} γ	Coefficient of volumetric expansion	K ⁻¹	$m^3/(m^3 \cdot K) = K^{-1}$ N.: Temperature unit/volume ratio N.A.: $m^3/(m^3 \cdot deg)$			

	Physical quantities and units of electrical engineering				
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed		
I	Current strength	A (Ampere)	N.: Basic unit L.U.: pA; nA; μA; mA; kA; etc.		
Q	Electric charge; Quantity of electricity	C (Coulomb)	1 C = 1 A · s 1 Ah = 3600 As L.U.: pC; nC; μC; kC		
U	Electric voltage	V (Volt)	$\begin{array}{l} 1 \text{ V} = 1 \text{ W/A} = 1 \text{ J/(s} \cdot \text{A)} \\ = 1 \text{ A} \cdot \Omega = 1 \text{ N} \cdot \text{m/(s} \cdot \text{A)} \\ \text{L.U.: } \mu \text{V; mV; kV; MV; etc.} \end{array}$		
R	Electric resistance	Ω (Ohm)	1 Ω = 1 V/A = 1 W/A ² 1 J/(s · A ²) = 1 N · m/(s · A ²) L.U.: $\mu\Omega$; m Ω ; k Ω ; etc.		
G	Electric conductance	S (Siemens)	N.: Reciprocal of electric resistance 1 S = 1 Ω^{-1} = 1/ Ω ; G = 1/R L.U.: μ S; mS; kS		
С	Electric capacitance	F (Farad)	$\begin{array}{l} 1 \ F = 1 \ C/V = 1 \ A \cdot s/V \\ = 1 \ A^2 \cdot s/W = 1 \ A^2 \cdot s^2/J \\ = 1 \ A^2 \cdot s^2/(N \cdot m) \\ \text{L.U.:} pF; \ \mu F; \ etc. \end{array}$		

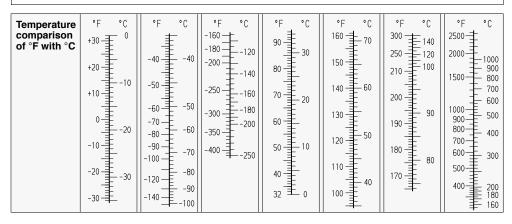
PhysicsPhysical Quantities and Units of Lighting Engineering, Different Measuring Units of Temperature

	Physica	al quantities an	d units of lighting engineering
Symbol	Physical quantity	SI unit Symbol Name	N.: Note L.U.: Further legal units N.A.: Units no longer allowed
I	Luminous intensity	cd (Candela)	N.: Basic unit 1 cd = 1 lm (lumen) / sr (Steradian) L.U.: mcd; kcd
L	Luminous density; Luminance		L.U.: cd/cm ² ; mcd/m ² ; etc. N.A.: Apostilb (asb): $1 \text{ asb} = \frac{1}{\pi} \text{ cd/m}^2$ Nit (nt): $1 \text{ nt} = 1 \text{ cd/m}^2$ Stilb (sb): $1 \text{ sb} = 10^4 \text{ cd/m}^2$
Ф	Luminous flux	lm (Lumen)	1 lm = 1 cd·sr L.U.: klm
Е	Illuminance	lx (Lux)	1 lx = 1 lm/m ²

	Different measuring units of temperature										
Kelvin K T _K	Degrees Celsius °C t _C	Degrees Fahrenheit °F t _F	Degrees Rankine °R T _R								
$T_{K} = 273.15 + t_{C}$	$t_{\rm C} = T_{\rm K} - 273.15$	$t_F = \frac{9}{5} \cdot T_K - 459.67$	$T_R = \frac{9}{5} \cdot T_K$								
$T_{K} = 255.38 + \frac{5}{9} \cdot t_{F}$	$t_C = \frac{5}{9} \left(t_F - 32 \right)$	$t_{F} = 32 + \frac{9}{5} \cdot t_{C}$	$T_R = \frac{9}{5} \ (t_c + 273.15)$								
$T_K = \frac{5}{9} \cdot T_R$	$t_{\rm C} = \frac{5}{9} \ T_{\rm R} - 273.15$	$t_F = T_R - 459.67$	$T_{R} = 459.67 + t_{F}$								

Comparison of some temperatures									
0.00	– 273.15	- 459.67	0.00						
+ 255.37	- 17.78	0.00	+ 459.67						
+ 273.15	0.00	+ 32.00	+ 491.67						
+ 273.16 ¹⁾	+ 0.01 ¹⁾	+ 32.02	+ 491.69						
+ 373.15	+ 100.00	+ 212.00	+ 671.67						

1) The triple point of water is +0.01 °C. The triple point of pure water is the equilibrium point between pure ice, air-free water and water vapour (at 1013.25 hPa).



	Measures of length											
Unit		Inch in	Foot ft	Yard yd	Stat mile	Naut mile	mm	m	km			
1 in 1 ft 1 yd 1 stat mile 1 naut mile	= = = =	1 12 36 63 360 72 960	0.08333 1 3 5280 6080	0.02778 0.3333 1 1760 2027	- - - 1 1.152	- - - 0.8684 1	25.4 304.8 914.4 –	0.0254 0.3048 0.9144 1609.3 1853.2	- - - 1.609 1.853			
1 mm 1 m 1 km	= = =	0.03937 39.37 39.370	3.281 · 10 ⁻³ 3.281 3281	1.094 · 10 ⁻³ 1.094 1094	- - 0.6214	- - 0.5396	1 1000 10 ⁶	0.001 1 1000	10 ⁻⁶ 0.001 1			

- 1 German statute mile = 7500 m
- 1 geograph. mile = 7420.4 m = 4 arc minutes at the equator (1° at the equator = 111.307 km)
- 1 internat. nautical mile
- 1 German nautical mile (sm)
- 1 mille marin (French)

= 1852 m = 1 arc minute at the degree of

longitude (1° at the meridian = 111.121 km)

Astronomical units of measure

- 1 light-second = 300 000 km
- 1 l.y. (light-year) = $9.46 \cdot 10^{12}$ km
- 1 parsec (parallax second, distances to the stars) = 3.26 l.v.
- 1 astronomical unit (mean distance of the earth from the sun) = $1.496 \cdot 10^8$ km
- Typographical unit of measure: 1 point (p) = 0.376 mm

Other measures of length of the Imperial system

- 1 micro-in = 10^{-6} in = 0.0254 um
- 1 mil = 1 thou = 0.001 in = 0.0254 mm
- 1 line = 0.1 in = 2.54 mm
- 1 fathom = 2 yd = 1.829 m
- 1 engineer's chain = 100 eng link = 100 ft = 30.48 m
- 1 rod = 1 perch = 1 pole = 25 surv link = 5.029 m
- 1 surveyor's chain = 100 surv link = 20.12 m
- 1 furlong = 1000 surv link = 201.2 m
- 1 stat league = 3 stat miles = 4.828 km

Other measures of length of the metric system

France:

1 toise = 1.949 m

1 myriametre = 10 000 m

Russia:

1 werschok = 44.45 mm 1 saschen = 2.1336 m

1 werst = 1.0668 km

Japan:

1 arschin = 0.7112 m 1 shaku = 0.3030 m

1 ken = 1.818 m

1 ri = 3.927 km

	Square measures												
Unit		sq in	sq ft	sq yd	sq mile	cm ²	dm ²	m ²	а	ha	km ²		
1 square inch	=	1	_	-	_	6.452	0.06452	_	_	_	_		
1 square foot	=	144	1	0.1111	_	929	9.29	0.0929	_	_	-		
1 square yard	=	1296	9	1	_	8361	83.61	0.8361	_	_	_		
1 square mile	=	-	-	-	1	_	-	_	-	259	2.59		
1 cm ²	=	0.155	_	_	_	1	0.01	_	_	-	_		
1 dm ²	=	15.5	0.1076	0.01196	_	100	1	0.01	_	_	-		
1 m ²	=	1550	10.76	1.196	_	10000	100	1	0.01	_	_		
1 a	=	_	1076	119.6	_	_	10000	100	1	0.01	-		
1 ha	=	_	_	_	-	_	_	10000	100	1	0.01		
1 km ²	=	_	-	-	0.3861	_	_	_	10000	100	1		

Other square measures of the Imperial system

- 1 sq mil = $1 \cdot 10^{-6}$ sq in = 0.0006452 mm²
- 1 sq line = $0.01 \text{ sq in} = 6.452 \text{ mm}^2$
- 1 sq surveyor's link = 0.04047 m_2
- 1 sq rod = 1 sq perch = 1 sq pole = 625 sq surv link = 25.29 m²
- 1 sq chain = 16 sq rod = 4.047 a
- 1 acre = 4 rood = 40.47 a
- 1 township (US) = $36 \text{ sq miles} = 3.24 \text{ km}^2$
- 1 circular in $=\frac{\pi}{4}$ sq in $=5.067 cm^2$ (circular area with 1 in dia.)
- 1 circular mil = $\frac{\pi}{4}$ sq mil = 0.0005067mm² (circular area with 1 mil dia.)

Other square measures of the metric system

Russia:

1 kwadr. archin = 0.5058 m^2

1 kwadr. saschen = 4.5522 m²

= 1.0925 ha 1 dessjatine $= 1.138 \text{ km}^2$ 1 kwadr. werst

Japan:

 $= 3.306 \, \text{m}^2$ 1 tsubo

= 0.9917a1 se

 $= 15.42 \text{ km}^2$ 1 ho-ri

Physics

Cubic Measures and Weights; Energy, Work, Quantity of Heat

	Cubic measures											
Unit		cu in	cu ft	US liquid quart	US gallon	Imp quart	Imp gallon	cm ³	dm ³ (l)	m ³		
1 cu in 1 cu ft 1 cu yd		1 1728 46656	- 1 27	0.01732 29.92 807.9	- 7.481 202	0.01442 24.92 672.8	- 6.229 168.2	16.39 - -	0.01639 28.32 764.6	- 0.02832 0.7646		
1 US liquid quart 1 US gallon	11 11	57.75 231	0.03342 0.1337	1 4	0.25 1	0.8326 3.331	0.2082 0.8326	946.4 3785	0.9464 3.785			
1 Imp quart 1 Imp gallon	11 11	69.36 277.4	0.04014 0.1605	1.201 4.804	0.3002 1.201	1 4	0.25 1	1136 4546	1.136 4.546	-		
1 cm ³ 1 dm ³ (I) 1 m ³	11 11	0.06102 61.02 61023	- 0.03531 35.31	- 1.057 1057	- 0.2642 264.2	- 0.88 880	- 0.22 220	1 1000 10 ⁶	0.001 1 1000	10 ⁶ 0.001 1		

- $1 \text{ US minim} = 0.0616 \text{ cm}^3 \text{ (USA)}$
- 1 US fl dram = 60 minims = 3.696 cm³
- 1 US fl oz = 8 fl drams = 0.02957 l
- 1 US gill = 4 fl oz = 0.1183 l
- 1 US liquid pint = 4 gills = 0.4732 l 1 US liquid quart = 2 liquid pints = 0.9464 l
- 1 US gallon = 4 liquid quarts = 3.785 l
- 1 US dry pint = 0.5506 l
- 1 US dry quart = 2 dry pints = 1.101 l
- 1 US peck = 8 dry quarts = 8.811 I
- 1 US bushel = 4 pecks = 35.24 l
- 1 US liquid barrel = 31.5 gallons = 119.2 l
- 1 US barrel = 42 gallons = 158.8 l (for crude oil)
- 1 US cord = 128 cu ft = 3.625 m³

- 1 Imp minim = 0.0592 cm^3 (GB)
- 1 Imp fl drachm = $60 \text{ minims} = 3.552 \text{ cm}^3$
- 1 $\lim_{x \to 0} f(x) = 8 f(x) = 0.02841 f(x)$
- 1 Imp gill = 5 fl oz = 0.142 l
- 1 Imp pint = 4 gills = 0.5682 I
- 1 Imp quart = 2 pints = 1.1365 I1 Imp gallon = 4 quarts = 4.5461 I
- 1 Imp pottle = 2 quarts = 2.273 I
- 1 Imp peck = 4 pottles = 9.092 I
- 1 Imp bushel = 4 pecks = 36.37 I
- 1 Imp quarter = 8 bushels = 64 gallons = 290.94 l

					Weight	s					
Unit		dram	oz	lb	short cwt	long cwt	short ton	long ton	g	kg	t
1 dram	=	1	0.0625	0.003906	_	-	-	-	1.772	0.00177	-
1 oz (ounce)	=	16	1	0.0625	-	_	_	_	28.35	0.02835	_
1 lb (pound)	=	256	16	1	0.01	0.008929	-	-	453.6	0.4536	-
1 short cwt (US) 1 long cwt (GB/US)	=	25600 28672	1600 1792	100 112	1 1.12	0.8929 1	0.05 0.056	0.04464 0.05	45359 50802	45.36 50.8	0.04536 0.0508
1 short ton (US)	=	_	32000	2000	20	17.87	1	0.8929	-	907.2	0.9072
1 long ton (GB/US)	=	_	35840	2240	22.4	20	1.12	1	-	1016	1.016
1g	=	0.5643	0.03527	0.002205	_	-	_	_	1	0.001	10 ⁻⁶
1kg	=	564.3	35.27	2.205	0.02205	0.01968	_	_	1000	1	0.001
1ť	=	-	35270	2205	22.05	19.68	1.102	0.9842	10 ⁶	1000	1
1 grain = 1 / 7000 l 1 stone = 14 lb = 6)	1 lot = 3	solotnik	dol = 4.26 k = 12.79	78 g		(CIS) (CIS)				

- 1 stone = 14 lb = 6.35 kg
- 1 short quarter = 1/4 short cwt = 11.34 kg
- 1 long quarter = 1/4 long cwt = 12.7 kg
- 1 quintal or 1 cental = 100 lb = 45.36 kg
- 1 quintal = 100 livres = 48.95 kg
- 1 kilopound = 1 kp = 1000 lb = 453.6 kg

- lot = 3 solotnik = 12.7978 g1 funt = 32 lot = 0.409 kg
- 1 pud = 40 funt = 16.38 kg1 berkowetz = 163.8 kg
- 1 kwan = 100 tael = 1000 momme = 10000 fun = 3.75 kg (J) 1 hyaku kin = 1 picul = 16 kwan = 60 kg

(CIS)

(CIS)

(CIS)

tdw = tons dead weight = lading capacity of a cargo vessel (cargo + ballast + fuel + stores), mostly given in long tons, i.e. 1 tdw = 1016 kg

(USA)

(USA)

(ÚSA)

(GB / USA)

Energy, work, quantity of heat												
Work		ft lb	erg	J = Nm = Ws	kpm	PSh	hph	kWh	kcal	Btu		
1 ft lb 1 erg 1 Joule (WS) 1 kpm 1 PSh 1 hph 1 kWh 1 kcal			10 · 10 ⁶ 98.07 · 10 ⁶ 26.48 · 10 ¹² 26.85 · 10 ¹²	$2.685\cdot 10^6$	10.2 · 10 ⁻⁹ 0.102 1		37.25 · 10 ⁻¹⁵ 372.5 · 10 ⁻⁹	277.8 · 10 ⁻⁹		94.84 · 10 ⁻¹² 948.4 · 10 ⁻⁶		
1 Btu	=	778.6	10.55 · 10 ⁹	1055	107.6	398.4 · 10 ⁻⁶	392.9 · 10 ⁻⁶	293 · 10 ⁻⁶	0.252	1		

1 in oz = 0.072 kpcm; 1 in lb = 0.0833ft lb = 0.113 Nm; 1 thermi (French) = 4.1855 · 106 J; 1 therm (English) = 105.51 · 106 J Common in case of piston engines: 1 litre-atmosphere (litre atmosphere) = 98.067 J

Power, Energy Flow, Heat Flow, Pressure and Tension, Velocity

	Power, energy flow, heat flow										
Power		erg/s	W	kpm/s	PS	hp	kW	kcal/s	Btu/s		
1 erg/s	=	1	10 ⁻⁷	0.102 · 10 ⁻⁷	0.136 · 10 ⁻⁹	0.1341 · 10 ⁻⁹	10 ⁻¹⁰	23.9 · 10 ⁻¹²	94.84 · 10 ⁻¹²		
1W	=	10 ⁷	1	0.102	1.36 ·10 ⁻³	1.341 · 10 ⁻³	10 ⁻³	239 · 10 ⁻⁶	948.4 · 10 ⁻⁶		
1 kpm/s	=	$9.807 \cdot 10^{7}$	9.807	1	13.33 · 10 ⁻³	13.15 · 10 ⁻³	9.804 · 10 ⁻³	2.344 · 10 ⁻³	9.296 · 10 ⁻³		
1 PS (ch) 2)	=	$7.355 \cdot 10^9$	735.5	75	1	0.9863	0.7355	0.1758	0.6972		
1hp	=	$7.457 \cdot 10^9$	745.7	76.04	1.014	1	0.7457	0.1782	0.7068		
1 kW	=	10 ¹⁰	1000	102	1.36	1.341	1	0.239	0.9484		
1 kcal/s	=	41.87 · 10 ⁸	4187	426.9	5.692	5.614	4.187	1	3.968		
1 Btu/s	=	10.55 · 10 ⁹	1055	107.6	1.434	1.415	1.055	0.252	1		

¹ poncelet (French) = 980.665 W; flyweel effect: 1 kgm² = 3418 lb in ²

	Pressure and tension													
Unit		μbar = dN/m²	mbar = cN/ cm ²	bar = daN/ cm ²	kp/m ² mm WS	p/cm ²	kp/cm ² = at	kp/ mm ²	Torr = mm QS	atm	lb sq ft	lb sq in	long ton sq in	sh ton sq in
	= [1	0.001	-	0.0102	-	-	_	-	-	-	-	-	-
1 mbar = cN/cm ²	= '	1000	1	0.001	10.2	1.02	_	_	0.7501	-	2.089	0.0145	-	-
1 bar = daN/cm ²	=	10 ⁶	1000	1	10197	1020	1.02	0.0102	750.1	0.9869	2089	14.5	0.0064	0.0072
1 kp/m ² = 1mm WS at 4 °C	= 9	98.07	-	-	1	0.1	0.0001	-	-	-	0.2048	-	-	-
1 p/cm ²	= 9	980.7	0.9807	_	10	1	0.001	_	0.7356	-	2.048	0.0142	-	-
1 kp/cm ² = 1 at (technical atmosphere)	=	-	980.7	0.9807	10000	1000	1	0.01	735.6	0.9678	2048	14.22	_	-
1 kp/mm ²	=	-	98067	98.07	10 ⁶	10 ⁵	100	1	73556	96.78	-	1422	0.635	0.7112
1 Torr = 1 mm QS at 0 °C	=	1333	1.333	0.00133	13.6	1.36	0.00136	-	1	-	2.785	0.01934	-	1
1 atm (pressure of the atmosphere)	=	-	1013	1.013	10332	1033	1.033	-	760	1	2116	14,7	-	-
1 lb/sq ft	= 4	478.8	0.4788	-	4.882	0.4882	-	-	0.3591	-	1	-	-	-
1 lb/sq in = 1 psi	= 6	8948	68.95	0.0689	703.1	70.31	0.0703	-	51.71	0.068	144	1	_	0.0005
1 long ton/sq in (GB)	=	-	-	154.4	-	_	157.5	1.575	_	152.4	-	2240	1	1,12
1 short ton/sq in (US)	=	-	-	137.9	-	-	140.6	1.406	-	136.1	-	2000	0.8929	1

¹ psi = $0.00689 \, \text{N} \, / \, \text{mm}^2$

The specific gravity of mercury is assumed to be 13.595 kg/dm³.

Velocity										
Unit		m/s	m/min	km/h	ft/min	mile/h				
m/s m/min km/h ft/min mile/h	= = = =	1 0.0167 0.278 0.0051 0.447	60 1 16.67 0.305 26.82	3.6 0.06 1 0.0183 1.609	196.72 3.279 54.645 1 87.92	2.237 0.0373 0.622 0.0114 1				

¹ N/m² (Newton/m²) = 10 μ b; 1 barye (French) = 1 μ b; 1 pièce (pz) (French) = 1 sn/m² \approx 102 kp/m²; 1 hpz = 100 pz = 1.02 kp/m^2 ; 1 micron (USA) = 0.001 mm QS = 0.001 Torr.In the USA, "inches Hg" are calculated from the top, i.e. 0 inches Hg = 760 mm QS and 29.92 inches Hg = 0 mm

QS = absolute vacuum.

PhysicsEquations for Linear Motion and Rotary Motion

Deficition	SI	Sym-					
Definition	unit	bol	Linear motion	Rotary motion			
Uniform motion			distance moved divided by time	angular velocity = angle of rotation in radian measure/time			
Velocity	m/s	٧	$v = \frac{s_2 - s_1}{t_2 - t_1} = \frac{\Delta s}{\Delta t} = const.$	$\omega = \frac{\varphi_2 - \varphi_1}{t_2 - t_1} = \frac{\Delta \varphi}{\Delta t} = \text{const.}$			
Angular velocity	rad/s	ω	motion acceler	ated from rest:			
Angle of rotation	rad	φ	$v = \frac{s}{t}$	$\omega = \frac{\varphi}{t}$			
Distance moved	m	s	$s = v \cdot t$	angle of rotation $\varphi = \omega \cdot t$			
Uniformly accelerated motion			acceleration equals change of velocity divided by time	angular acceleration equals change of angular velocity divided by time			
Acceleration	m/s ²	а	$a = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t} = const.$	$\alpha = \frac{\omega_2 - \omega_1}{t_2 - t_1} = \frac{\Delta \omega}{\Delta t} = \text{const.}$			
Angular acceleration	rad/s ²	α	motion acceler	ated from rest:			
association.			$a = \frac{v}{t} = \frac{v^2}{2s} = \frac{2s}{t^2}$	$\alpha = \frac{\omega}{t} = \frac{\omega^2}{2\varphi} = \frac{2\varphi}{t^2}$			
Velocity	m/s	٧	$v = a \cdot t = \sqrt{2 a \cdot s}$	$\omega = \alpha \cdot t$			
Circumferential speed	m/s	v		$v = r \cdot \omega = r \cdot \alpha \cdot t$			
Distance moved	m	s	$s = \frac{v}{2} \cdot t = \frac{a}{2} \cdot t^2 = \frac{v^2}{2a}$	angle of rotation $\varphi = \frac{\omega}{2} \cdot t = \frac{\alpha}{2} \cdot t^2 = \frac{\omega^2}{2\alpha}$			
Uniform motion and constant force or constant torque			force · distance moved	torque · angle of rotation in radian measure			
Work	J	W	$W = F \cdot s$	$W = M \cdot \varphi$			
			work in unit of time = force · velocity	work in unit of time = torque · angular velocity			
Power	W	Р	$P = \frac{W}{t} = F \cdot v$	$P = \frac{W}{t} = M \cdot \omega$			
Non-uniform (accelerated) motion			accelerating force = mass · acceleration	accel. torque = second mass moment · angular acceleration			
Force	N	F	F = m·a	$M = J \cdot \alpha$			
In case of any motion			Momentum (kinetic energy) equals half the mass · second power of velocity	Kinetic energy due to rotation equals half the mass moment of inertia · second power of the angular velocity			
Energie	J	E_k	$E_k = \frac{m}{2} \cdot v^2$	$E_k = \frac{J}{2} \cdot \omega^2$			
Potential energy (due to force of gravity)	J	Ep	$E_{p} \qquad \qquad \text{weight} \cdot \text{height} \\ E_{p} = G \cdot \text{h} = \text{m} \cdot \text{g} \cdot \text{h}$				
Centrifugal force N $F_F = m \cdot r_s \cdot \omega^2$ $(r_s = centre-of-gravity radius)$				entre-of-gravity radius)			

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	A = area	U = circumference	
Square	$A = a^2$	Polygon	
	$a = \sqrt{A}$ $d = a\sqrt{2}$	h ₁	$A = A_1 + A_2 + A_3$ $= \frac{a \cdot h_1 + b \cdot h_2 + b \cdot h_3}{2}$
Rectangle	$A = a \cdot b$ $d = \sqrt{a^2 + b^2}$	Formed area	$A = \frac{r^2}{2} (2\sqrt{3} - \pi)$ $\approx 0.16 \cdot r^2$
Parallelogram	$A = a \cdot h$ $a = \frac{A}{h}$	Circle	$A = \frac{d^2 \cdot \pi}{4} = r^2 \cdot \pi$ $\approx 0.785 \cdot d^2$ $U = 2 \cdot r \cdot \pi = d \cdot \pi$
Trapezium	$A = m \cdot h$ $m = \frac{a + b}{2}$	Circular ring	$A = \frac{\pi}{4} \cdot (D^2 - d^2)$ $= (d + b) b \cdot \pi$ $b = \frac{D - d}{2}$
Triangle	$A = \frac{a \cdot h}{2}$ $a = \frac{2 \cdot A}{h}$	Circular sector	$A = \frac{r^2 \cdot \pi \cdot \alpha^{\circ}}{360^{\circ}}$ $= \frac{b \cdot r}{2}$ $b = \frac{r \cdot \pi \cdot \alpha^{\circ}}{180^{\circ}}$
Equilateral triangle	$A = \frac{a^2}{4}\sqrt{3}$ $d = \frac{a}{2}\sqrt{3}$	Circular segment	$A = \frac{r^2}{2} \left(\frac{\alpha^{\circ} \cdot \pi}{180^{\circ}} - \sin \alpha \right)$ $= \frac{1}{2} [r (b - s) + sh]$ $s = 2 r \sin \frac{\alpha}{2}$ $h = r (1 - \cos \frac{\alpha}{2}) = \frac{s}{2} \tan \frac{\alpha}{4}$
Hexagon	$A = \frac{3 \cdot a^2 \cdot \sqrt{3}}{2}$ $d = 2 \cdot a$ $s = \sqrt{3} \cdot a$	Ellipse	$\hat{\alpha} = \frac{\alpha^{\circ} \cdot \pi}{180^{\circ}}$ $b = r \cdot \hat{\alpha}$ $A = \frac{D \cdot d \cdot \pi}{4} = a \cdot b \cdot \pi$ $U \approx \frac{D + d}{2} \cdot \pi$
Octagon	$A = 2a^{2} (\sqrt{2} + 1)$ $d = a\sqrt{4 + 2\sqrt{2}}$ $s = a(\sqrt{2 + 1})$		$0 \approx \frac{1}{2} \cdot \pi$ $U = \pi (a + b) [1 + \frac{1}{4} \left(\frac{a - b}{a + b}\right)^{2} + \frac{1}{64} \left(\frac{a - b}{a + b}\right)^{4} + \frac{1}{256} \left(\frac{a - b}{a + b}\right)^{6} \dots]$

V = vol	ume O = surface	e M = gener	ated surface
Cube	$V = a^{3}$ $O = 6 \cdot a^{2}$ $d = a\sqrt{3}$	Frustum of cone	$V = \frac{\pi \cdot h}{12} (D^2 + Dd + d^2)$ $M = \frac{\pi \cdot m}{2} (D + d)$ $= 2 \cdot \pi \cdot p \cdot h$ $m = \sqrt{\left(\frac{D - d}{2}\right)^2 + h^2}$
Square prism	$V = a \cdot b \cdot c$ $O = 2 (ab + ac + bc)$ $d = \sqrt{a^2 + b^2 + c^2}$	Sphere	$V = \frac{4}{3} r^3 \pi = \frac{1}{6} \cdot d^3 \pi$ $\approx 4.189 \cdot r^3$ $O = 4 \pi \cdot r^2 = \pi \cdot d^2$
Parallelepiped	V = A · h (Cavalier principle)	Spherical zone	$V = \frac{\pi \cdot h}{6} (3a^2 + 3b^2 + h^2)$ $M = 2 \cdot r \cdot \pi \cdot h$
Pyramid	$V = \frac{A \cdot h}{3}$	Spherical segment	$V = \frac{\pi \cdot h}{6} \left(\frac{3}{4} s^2 + h^2 \right)$ $= \pi h^2 \left(r - \frac{h}{3} \right)$ $M = 2 \cdot r \cdot \pi \cdot h$ $= \frac{\pi}{4} (s^2 + 4h^2)$
Frustum of pyramid	$V = \frac{h}{3} (A_1 + A_2 + \sqrt{A_1 \cdot A_2})$	Spherical sector	$V = \frac{2}{3} \cdot h \cdot r^{2} \cdot \pi$ $O = \frac{\pi \cdot r}{2} (4h + s)$
Cylinder	$V = \frac{d^2 \cdot \pi}{4} h$ $M = 2 \cdot r \cdot \pi \cdot h$ $O = 2 \cdot r \cdot \pi \cdot (r + h)$	Cylindrical ring	$V = \frac{D \cdot \pi^2 \cdot d^2}{4}$ $O = D \cdot d \cdot \pi^2$
Hollow cylinder	$V = \frac{h \cdot \pi}{4} (D^2 - d^2)$	Barrel	$V = \frac{h \cdot \pi}{12} (2D^2 + d^2)$
Cone	$V = \frac{r^2 \cdot \pi \cdot h}{3}$ $M = r \cdot \pi \cdot m$ $O = r \cdot \pi \cdot (r + m)$ $m = \sqrt{h^2 + \left(\frac{d}{2}\right)^2}$	Prismatoid A ₂	$V = \frac{h}{6} (A_1 + A_2 + 4A)$

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Mechanics / Strength of Materials Axial Section Moduli and Axial Second Moments of Area (Moments of Inertia) of Different Profiles

Cross-sectional area	Section modulus	Second moment of area
1 2 1 .c 1 .c 1 1 .	$W_1 = bh^2/6$ $W_2 = hb^2/6$	$I_1 = bh^3/12$ $I_2 = hb^3/12$
	$W_1 = W_2 = a^3/6$	$I_1 = I_2 = a^4/12$
υ 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	$W_1 = bh^2/24 \text{ for } e = \frac{2}{3} h$ $W_2 = hb^2/24$	$I_1 = bh^3/36$ $I_2 = hb^3/48$
2 1 2 R	$W_1 = \frac{5}{8} R^3 = 0.625 R^3$ $W_2 = 0.5413 R^3$	$I_1 = I_2 = \frac{5}{16} \sqrt{3} R^4 = 0.5413 R^4$
b1/2 b1/2	$W_1 = \frac{6b^2 + 6bb_1 + b_1^2}{12(3b + 2b_1)} h^2$ for $e = \frac{1}{3} \frac{3b + 2b_1}{2b + b_1} h$	$I_1 = \frac{6b^2 + 6bb_1 + b_1^2}{36(2b + b_1)} h^3$
1 c 1 1 x c 1 1 x x x x x x x x x x x x	$W_1 = \frac{BH^3 - bh^3}{6H}$	$I_1 = \frac{BH^3 - bh^3}{12}$
1 2 1 2 D	$W_1 = W_2 = \pi D^3 / 32 \approx D^3 / 10$	$I_1 = I_2 = \pi D^4 / 64 \approx D^4 / 20$
2 5 2 1 1 1 1 2 1 2 2 2 2 2 2 2 2 2 2 2	or in case of thin	$I_1 = I_2 = \frac{\pi}{64} (D^4 - d^4)$ wall thickness s: $I_1 = I_2 = \pi s r^3 \left[1 + (s/2r)^2 \right] \approx \pi s r^3$
2 1 1 2 2	$W_1 = \pi a^2 b/4$ $W_2 = \pi b^2 a/4$	$I_1 = \pi a^3 b/4$ $I_2 = \pi b^3 a/4$
5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	$W_1 = I_1/a_1$ or in case of thin $s = a_1 - a_2 = b_1 - b_2 = 0$ $W_1 \approx \frac{\pi}{4} \ a \ (a+3b) \ s$	$I_{1} = \frac{\pi}{4} (a_{1}^{3} b_{1} - a_{2}^{3} b_{2})$ wall thickness s: $= 2 (a - a_{2}) = 2 (b - b_{2})$ $I_{1} \approx \frac{\pi}{4} a^{2} (a + 3b) s$
	w ₁ = I ₁ / e = 0.1908 r ³ with e = r $\left(1 - \frac{4}{3\pi}\right)$ = 0.5756 r axis 1-1 = axis of	$I_1 = [\pi/8 - 8/(9\pi)] r^4 = 0.1098 r^4$

	eflection (mm) $\alpha, \alpha_1, \alpha_2, \alpha_A, \alpha_B$ Angles (°) engths (mm) F, F_A, F_B Forces (N) odulus of elasticity (N/mm²) I Second moment of area (mm⁴) I (moment of inertia)
F 3	$w(x) = \frac{FI^3}{3EI} \left[1 - \frac{3}{2} \cdot \frac{x}{I} + \frac{1}{2} \left(\frac{x}{I} \right)^3 \right] \qquad f = \frac{FI^3}{3EI} \qquad \tan \alpha = \frac{FI^2}{2EI}$ $F_B = F$
L Q F _B	$w(x) = \frac{ql^4}{8EI} \left[1 - \frac{4}{3} \cdot \frac{x}{l} + \frac{1}{3} \left(\frac{x}{l} \right)^4 \right] \qquad f = \frac{ql^4}{8EI} \qquad \tan \alpha = \frac{ql^3}{6EI}$ $F_B = q \cdot l$
U Q F _R	$w(x) = \frac{q_0 I^4}{120EI} \left[4 - 5 \cdot \frac{x}{I} + \left(\frac{x}{I} \right)^5 \right] \qquad f = \frac{q_0 I^4}{30EI} \qquad \tan \alpha = \frac{q_0 I^3}{24EI}$ $F_B = \frac{q_0 \cdot I}{2}$
F _A × L F _B	$w(x) = \frac{Fi^3}{16Ei} \cdot \frac{x}{i} \left[1 - \frac{4}{3} \left(\frac{x}{i} \right)^2 \right] \qquad x \le \frac{1}{2} \qquad f = \frac{Fi^3}{48Ei} \qquad \tan \alpha = \frac{Fi^2}{16Ei}$ $F_A = F_B = \frac{F}{2}$
	$w_{1}(x_{1}) = \frac{Fi^{3}}{6EI} \cdot \frac{a}{i} \left(\frac{b}{i}\right)^{2} \frac{x_{1}}{i} \left(1 + \frac{1}{b} - \frac{x_{1}^{2}}{ab}\right) x_{1} \le a f = \frac{Fi^{3}}{3EI} \left(\frac{a}{i}\right)^{2} \left(\frac{b}{i}\right)^{2} \tan \alpha_{1} = \frac{f}{2a} \left(1 + \frac{1}{b}\right)$ $w_{2}(x_{2}) = \frac{Fi^{3}}{6EI} \cdot \frac{b}{i} \left(\frac{a}{i}\right)^{2} \frac{x_{2}}{i} \left(1 + \frac{1}{a} - \frac{x_{2}^{2}}{ab}\right) x_{2} \le b f_{max} = f \frac{1 + b}{3b} \sqrt{\frac{1 + b}{3a}} \tan \alpha_{2} = \frac{f}{2b} \left(1 + \frac{1}{a}\right)$
$F_{A} = \frac{1}{x_{1max}} = a\sqrt{(1+b)/3a} \text{ for a > b}$ $Change a and b for a < b$	$F_A = F \frac{b}{l}$ $F_B = F \frac{a}{l}$
L/2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	$\begin{split} w(x) &= \frac{Fi^3}{2Ei} \cdot \frac{x}{i} \left[\frac{a}{i} \left(1 - \frac{a}{i} \right) - \frac{1}{3} \left(\frac{x}{i} \right)^2 \right] f = \frac{Fi^3}{2Ei} \left(\frac{a}{i} \right)^2 \left(1 - \frac{4}{3} \cdot \frac{a}{i} \right) \tan \alpha_1 = \frac{Fi^2}{2Ei} \cdot \frac{a}{i} \left(1 - \frac{a}{i} \right) \\ x &= s a < 1/2 \\ w(x) &= \frac{Fi^3}{2Ei} \cdot \frac{a}{i} \left[\frac{x}{i} \left(1 - \frac{x}{i} \right) - \frac{1}{3} \left(\frac{a}{i} \right)^2 \right] f_m = \frac{Fi^3}{8Ei} \cdot \frac{a}{i} \left[1 - \frac{4}{3} \left(\frac{a}{i} \right)^2 \right] \tan \alpha_2 = \frac{Fi^2}{2Ei} \cdot \frac{a}{i} \left(1 - 2 \cdot \frac{a}{i} \right) \\ a &\leq x \leq 1/2 \\ F_A &= F_B = F \end{split}$
1	$\begin{split} w_{1}(x_{1}) &= \frac{Fl^{3}}{2EI} \left[\frac{1}{3} \left(\frac{x_{1}}{l} \right)^{3} - \frac{a}{l} \left(1 + \frac{a}{l} \right) \frac{x_{1}}{l} + \left(\frac{a}{l} \right)^{2} \left(1 + \frac{2}{3} \cdot \frac{a}{l} \right) \right] \\ x_{1} &\leq a \qquad \qquad f = \frac{Fl^{3}}{2EI} \left(\frac{a}{l} \right)^{2} \left(1 + \frac{2}{3} \cdot \frac{a}{l} \right) \qquad \qquad \tan \alpha_{1} = \frac{Fl^{2}}{2EI} \cdot \frac{a}{l} \left(1 + \frac{a}{l} \right) \\ w_{2}(x_{2}) &= \frac{Fl^{3}}{2EI} \cdot \frac{a}{l} \cdot \frac{x_{2}}{l} \left(1 - \frac{x_{2}}{l} \right) \qquad \qquad x_{2} \leq l \qquad \qquad f_{m} = \frac{Fl^{3}}{8EI} \cdot \frac{a}{l} \qquad \tan \alpha_{2} = \frac{Fl^{2}}{2EI} \cdot \frac{a}{l} \\ F_{A} &= F_{B} = F \end{split}$
F	$\begin{split} w_1(x_1) &= \frac{Fi^3}{6EI} \cdot \frac{a}{I} \cdot \frac{x_1}{I} \left[1 - \left(\frac{x_1}{I} \right)^2 \right] x_1 \leq I f = \frac{Fi^3}{3EI} \left(\frac{a}{I} \right)^2 \left(1 + \frac{a}{I} \right) \tan \alpha_A = \frac{Fi^2}{6EI} \cdot \frac{a}{I} \\ w_2(x_2) &= \frac{Fi^3}{6EI} \cdot \frac{x_2}{I} \left[\frac{2a}{I} + \frac{3a}{I} \cdot \frac{x_2}{I} - \left(\frac{x_2}{I} \right)^2 \right] x_2 \leq a f_{max} = \frac{Fi^3}{9\sqrt{3}EI} \cdot \frac{a}{I} \tan \alpha_B = 2 \tan \alpha_A \\ F_A &= F \frac{a}{I} \qquad F_B = F \left(1 + \frac{a}{I} \right) \qquad \tan \alpha = \frac{Fi^2}{6EI} \cdot \frac{a}{I} \left(2 + 3 \frac{a}{I} \right) \end{split}$
The state of the s	$\begin{split} w(x) &= \frac{ql^4}{24El} \cdot \frac{x}{l} \left[1 - 2 \left(\frac{x}{l} \right)^2 + \left(\frac{x}{l} \right)^3 \right] 0 \leq x \leq l f_m = \frac{5ql^4}{384El} \tan \alpha = \frac{ql^3}{24El} \\ F_A &= \frac{q \cdot l}{2} \qquad \qquad F_B = \frac{q \cdot l}{2} \end{split}$

Values for Circular Sections

 $W_a = \frac{\pi \cdot d^3}{32}$ Axial section modulus:

 $W_p = \frac{\pi \cdot d^3}{16}$ Polar section modulus:

Axial second moment of area

 $I_a = \frac{\pi \cdot d^4}{64}$ (axial moment of inertia):

Polar second moment of area $I_p = \frac{\pi \cdot d^4}{32}$ (polar moment of area):

 $A = \frac{\pi \cdot d^2}{4}$ Area:

 $m = \frac{\pi \cdot d^2}{4} \cdot I \cdot \varrho$ Mass:

 $\varrho = 7.85 \; \frac{\text{kg}}{\text{dm}^3}$ Density of steel:

 $J = \frac{\pi \cdot d^4 \cdot I \cdot \varrho}{32}$ Second mass moment of inertia (mass moment of inertia):

(1-											
d	Α	Wa	Ia	Mass/I	J/I	d	Α	Wa	Ia	Mass/I	J/I
mm	cm ²	cm ³	cm ⁴	kg/m	kgm ² /m	mm	cm ²	cm ³	cm ⁴	kg/m	kgm²/m
6	0.293	0.0212	0.0064	0.222	0.000001	115	103.869	149.3116	858.5414	81.537	0.134791
7	0.385	0.0337	0.0118	0.302	0.000002	120	113.097	169.6460	1017.8760	88.781	0.159807
8	0.503 0.636	0.0503	0.0201	0.395 0.499	0.000003	125 130	122.718	191.7476	1198.4225	96.334	0.188152
10	0.636	0.0716 0.0982	0.0322 0.0491	0.499	0.000005 0.000008	135	132.732 143 139	215.6900 241.5468	1401.9848 1630.4406	104.195 112.364	0.220112 0.255979
11	0.950	0.1307	0.0719	0.746	0.000011	140	153.938	269.3916	1895.7410	120.841	0.296061
12	1.131	0.1696	0.1018	0.888	0.000016	145	165.130	299.2981	2169.9109	129.627	0.340676
13	1.327	0.2157	0.1402	1.042	0.000022	150	176.715	331.3398	2485.0489	138.721	0.390153
14	1.539	0.2694	0.1986	1.208	0.000030	155	188.692	365.5906	2833.3269	148.123	0.444832
15 16	1.767 2.011	0.3313 0.4021	0.2485 0.3217	1.387 1.578	0.000039 0.000051	160 165	201.062 213.825	402.1239 441.0133	3216.9909 3638.3601	157.834 167.852	0.505068 0.571223
17	2.270	0.4823	0.4100	1.782	0.000064	170	226.980	482.3326	4099.8275	178.179	0.643673
18	2.545	0.5726	0.5153	1.998	0.000081	175	240.528	526.1554	4603.8598	188.815	0.722806
19	2.835	0.6734	0.6397	2.226	0.000100	180	254.469	572.5553	5152.9973	199.758	0.809021
20	3.142	0.7854	0.7854	2.466	0.000123	185	268.803	621.6058	5749.8539	211.010	0.902727
21 22	3.464 3.801	0.9092 1.0454	0.9547 1.1499	2.719 2.984	0.000150 0.000181	190 195	283.529 298.648	673.3807 727.9537	6397.1171 7097.5481	222.570 234.438	1.004347 1.114315
23	4.155	1.1945	1.3737	3.261	0.000216	200	314.159	785.3982	7853.9816	246.615	1.233075
24	4.524	1.3572	1.6286	3.551	0.000256	210	346.361	909.1965	9546.5638	271.893	1.498811
25	4.909	1.5340	1.9175	3.853	0.000301	220	380.133	1045.3650	11499.0145	298.404	1.805345
26 27	5.309 5.726	1.7255 1.9324	2.2432 2.6087	4.168 4.495	0.000352 0.000410	230 240	415.476 452.389	1194.4924 1357.1680	13736.6629 16286.0163	326.148 355.126	2.156656 2.556905
28	6.158	2.1551	3.0172	4.493	0.000410	250	490.874	1533.9808	19174.7598	385.336	3.010437
29	6.605	2.3944	3.4719	5.185	0.000545	260	530.929	1725.5198	22431.7569	416.779	3.521786
30	7.069	2.6507	3.9761	5.549	0.000624	270	572.555	1932.3740	26087.0491	449.456	4.095667
32	8.042	3.2170	5.1472	6.313	0.000808	280	615.752	2155.1326	30171.8558	483.365	4.736981
34 36	9.079 10.179	3.8587 4.5804	6.5597 8.2448	7.127 7.990	0.001030 0.001294	300 320	706.858 804.248	2650.7188 3216.9909	39760.7820 51471.8540	554.884 631.334	6.242443 8.081081
38	11.341	5.3870	10.2354	8.903	0.001294	340	907.920	3858.6612	65597.2399	712.717	10.298767
40	12.566	6.2832	12.5664	9.865	0.001973	360	1017.876	4580.4421	82447.9575	799.033	12.944329
42	13.854	7.2736	15.2745	10.876	0.002398	380	1134.115	5387.0460	102353.8739	890.280	16.069558
44	15.205	8.3629 9.5559	18.3984 21.9787	11.936 13.046	0.002889 0.003451	400	1256.637	6283.1853	125663.7060	986.460 1087.572	19.729202
46 48	16.619 18.096	10.8573	26.0576	14.205	0.003451	420 440	1385.442 1520.531	7273.5724 8362.9196	152745.0200 183984.2320	1193.617	23.980968 28.885524
50	19.635	12.2718	30.6796	15.413	0.004817	460	1661.903	9555.9364	219786.6072	1304.593	34.506497
52	21.237	13.9042	35.8908	16.671	0.005635	480	1809.557	10857.3442	260576.2608	1420.503	40.910473
54	22.902	15.4590	41.7393	17.978	0.006553	500	1693.495	12271.8463	306796.1572	1541.344	48.166997
56 58	24.630 26.421	17.2411 19.1551	48.2750 55.5497	19.335 20.740	0.007579 0.008721	520 540	2123.717 2290.221	13804.1581 15458.9920	358908.1107 417392.7849	1667.118 1797.824	56.348573 65.530667
60	28.274	21.2058	63.6173	22.195	0.000721	560	2463.009	17241.0605	482749.6930	1933.462	75.791702
62	30.191	23.3978	72.5332	23.700	0.011388	580	2642.079	19155.0758	555497.1978	2074.032	87.213060
64	32.170	25.7359	82.3550	25.253	0.012930	600	2827.433	21205.7504	636172.5116	2219.535	99.879084
66	34.212	28.2249	93.1420	26.856	0.014623	620	3019.071	23397.7967	725331.6994	2369.970	113.877076
68 70	36.317 38.485	30.8693 33.6739	104.9556 117.8588	28.509 30.210	0.016478 0.018504	640 660	3216.991 3421.194	25735.9270 28224.8538	823549.6636 931420.1743	2525.338 2685.638	129.297297 146.232967
72	40.715	36.6435	131.9167	31.961	0.020711	680	3631.681	30869.2894	1049555.8389	2850.870	164.780267
74	43.008	39.7828	147.1963	33.762	0.023110	700	3848.451	33673.9462	1178588.1176	3021.034	185.038334
76	45.365	43.0964	163.7662	35.611	0.025711	720	4071.504	36643.5367	1319167.3201	3196.131	207.109269
78 80	47.784 50.265	46.5890 50.2655	181.6972 201.0619	37.510 39.458	0.028526 0.031567	740 760	4300.840 4536.460	39782.7731 43096.3680	1471962.6056 1637661.9830	3376.160 3561.121	231.098129 257.112931
82	52.810	54.1304	221.9347	41.456	0.031367	780	4778.362	46589.0336	1816972.3105	3751.015	285.264653
84	55.418	58.1886	244.3920	43.503	0.038370	800	5026.548	50265.4824	2010619.2960	3945.840	315.667229
86	58.088	62.4447	268.5120	45.599	0.042156	820	5281.017	54130.4268	2219347.4971	4145.599	348.437557
88	60.821	66.9034	294.3748	47.745	0.046217	840	5541.769	58188.5791	2443920.3207	4350.289	383.695490
90 92	63.617 66.476	71.5694 76.4475	322.0623 351.6586	49.940 52.184	0.050564 0.055210	860 880	5808.805	62444.6517 66903.3571	2685120.0234 2943747.7113	4559.912 4774.467	421.563844 462.168391
95	70.882	84.1726	399.8198	55.643	0.055210	900	6082.123 6361.725	71569.4076	3220623.3401	4993.954	505.637864
100	78.540	98.1748	490.8739	61.654	0.077067	920	6647.610	76447.5155	3516585.7151	5218.374	552.103957
105	86.590	113.6496	596.6602	67.973	0.093676	940	6939.778	81542.3934	3832492.4910	5447.726	601.701321
110	95.033	130.6706	718.6884	74.601	0.112834	960 980	7238.229 7542.964	86858.7536 92401.3084	4169220.1722 4527664.1126	5682.010 5921.227	654.567567 710.843266
						1000	7853.982	98174.7703	4908738.5156	6165.376	770.671947
L			l	l	l						

Diffusion of stress in structural members: loading types



Maximum stress limit:

Mean stress: Minimum stress limit:



dynamic $\sigma_0 = \sigma_{sch}$

$$\sigma_{o} = \sigma_{sch}$$
 $\sigma_{m} = \sigma_{sch}/2$
 $\sigma_{u} = 0$



alternating



Coefficients of

strength

oscillating

$$\begin{array}{l} \sigma_{\text{o}} = \, \sigma_{\text{m}} + \, \sigma_{\text{a}} \\ \sigma_{\text{m}} = \, \sigma_{\text{v}} \, (\text{initial stress}) \\ \sigma_{\text{u}} = \, \sigma_{\text{m}} - \, \sigma_{\text{a}} \end{array}$$

Resistance to deflection σ_A

Fatigue strength diagram acc. to SMITH

Ruling coefficient of strength of material for the calculation of structural members:

Resistance to breaking R_m Yield point Re; Rp0.2

Fatigue strength under fluctuating stresses σ_{Sch}

Example:

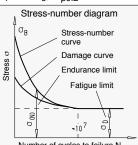
Tension-Compression

Fatigue strength under alternating stresses ow Coefficients of fatigue strength σ_D

Yield point R

Resistance to breaking R_m

Resistance to deflection σ_{Δ}



In case of stresses below the damage curve initial damage will not occur to

Number of cycles to failure N

-atigue strength under alternating stresses Fatigue strength under . †α fluctuating stresses osch Mean stress σ_m ŏ Alternate area/Area of fluctuation

Reduced stress on the member

the material.

Permissible stress

σ_{perm.}

Design strength of the member

 $\sigma_{D} \cdot b_{0} \cdot b_{d}$ $S \cdot \beta_k$

with: σ_D = ruling fatigue strength value of the material

> $b_0 = surface number (\leq 1)$ $b_d = size number (\leq 1)$

 β_k = stress concentration factor (≥ 1)

S = safety (1.2 ... 2)

Reduced stress σ_v

 σ_{v}

For the frequently occurring case of combined bending and torsion, according to the distortion energy theory:

with:

 σ = single axis bending stress

 τ = torsional stress

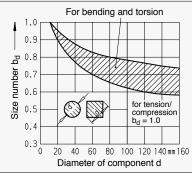
 α_0 = constraint ratio according to Bach

$$\sigma_{\rm v} = \sqrt{\sigma^2 + 3 (\alpha_0 \tau)^2}$$

Alternating bending, dynamic torsion: $\alpha_0 \approx 0.7$ Alternating bending, alternating torsion: $\alpha_0 \approx 1.0$

Static bending, alternating torsion:

 $\alpha_0 \approx 1.6$

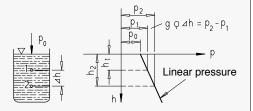


2.5 4 6.3 10 16 25 Surface roughness R_t in μm 0.9 0.8 Surface number b₀ 0.7 40 63 0.6 100 0.5 160 Surfaces with 0.4 rolling skin 400 500 600 700 800 900 1000 1100 1200 N/mm2 Resistance to breaking of the material R_m

Hydraulics	Page
Hydrostatics (Source: K. Gieck, Technische Formelsammlung, 29th edition, Gieck Verlag, Heilbronn)	53
Hydrodynamics (Source: K. Gieck, Technische Formelsammlung, 29th edition, Gieck Verlag, Heilbronn)	54

$$p_1 = p_0 + g \varrho h_1$$

$$P_2 = p_1 + g \varrho (h_2 - h_1) = p_1 + g \varrho \Delta h$$

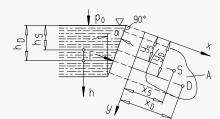


Hydrostatic force of pressure on planes

The hydrostatic force of pressure F is that force which is exerted on the wall by the fluid only - i.e. without consideration of pressure p_0 .

$$F = g \varrho y_s A \cos \alpha = g \varrho h_s A$$

$$y_D = \frac{I_x}{v_s A} = y_s + \frac{I_s}{v_s A}$$
 ; $x_D = \frac{I_{xy}}{v_s A}$ m, mm



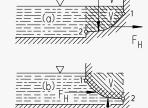
Hydrostatic force of pressure on curved surfaces

The hydrostatic force of pressure on the curved surface 1 - 2 is resolved into a horizontal component F_H and a vertical component F_V.

F_V is equal to the weight of the fluid having a volume V located (a) or thought to be located (b) over the surface 1 - 2. The line of application runs through the centre of gravity.

$$|F_V| = g \varrho V$$
 (N, kN)

F_H is equal to the hydrostatic force of pressure on the projection of surface 1 - 2 perpendicular to F_H.



Buoyance

The buoyant force F_A is equal to the weight of the displaced fluids having densities ϱ and ϱ '.

$$F_A = g \varrho V + g \varrho' V' \qquad (N, kN)$$

If the fluid with density ϱ ' is a gas, the following applies:

$$F_A \approx g \varrho V$$
 (N, kN)

For ϱ_k density of the body applies:

 $\varrho > \varrho_k$ the body floats

 $\varrho = \varrho_k$ the body is suspended

 $\rho < \rho_k$ the body sinks



S = centre of gravity of plane A

= centre of pressure D

 I_x , I_s = moments of inertia

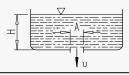
= product of inertia of plane A referred to the x- and y-axes

Discharge of liquids from vessels

Vessel with bottom opening

$$v = \phi \sqrt{2 g H}$$

$$\dot{V} = \phi \epsilon A \sqrt{2 g H}$$



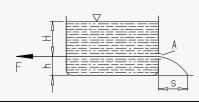
Vessel with small lateral opening

$$v\,=\,\phi\,\sqrt{2\,\,g\,H}$$

$$s = 2\sqrt{H h}$$
 (without any coefficient of friction)

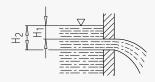
$$\dot{V}\,=\,\phi\;\epsilon\;A\;\sqrt{2\;g\;H}$$

$$F = \varrho \dot{V} v$$



Vessel with wide lateral opening

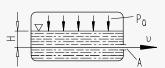
$$\dot{V} = \frac{2}{3} \epsilon b \sqrt{2 g} (H_2^{3/2} - H_1^{3/2})$$



Vessel with excess pressure on liquid level

$$v = \phi \sqrt{2 \left(g H + \frac{p_{\ddot{u}}}{\varrho}\right)}$$

$$\dot{V} \,=\, \phi \,\, \epsilon \,\, A \,\, \sqrt{2 \,\, \left(\, g \,\, H \,\, + \frac{p_{\ddot{u}}}{\varrho} \,\right)} \, \label{eq:Variation}$$



Vessel with excess pressure on outlet

$$v = \varphi \sqrt{2 \frac{p_{\ddot{u}}}{\varrho}}$$

$$\dot{V} = \varphi \; \epsilon \; A \; \sqrt{2 \; \frac{p_{\ddot{u}}}{\varrho}}$$



- v: discharge velocity
- g: gravity
- e: density
- pü: excess pressure compared to external pressure
- φ : coefficient of friction (for water $\varphi = 0.97$)
- ϵ : coefficient of contraction (ϵ = 0.62 for sharp-edged openings)
 - ($\varepsilon = 0.97$ for smooth-rounded openings)
- F: force of reaction
- V: volume flow rate
- b: width of opening

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Types of Protection for Electrical Equipment (Protection Against Water)	60

Ohm	ı's law:			_ γ _	6
U =	$I \cdot R$ $I = \frac{U}{R}$	$R = \frac{U}{x}$	Material		$\left[\frac{\Omega \text{ mm}^2}{\text{m}}\right]$
R . I				$[\Omega \text{ mm}^2]$	L m]
Serie	es connection of resist	tors:	a) Metals		
R =	$R_1 + R_2 + R_3 + + F$	R_{n}	Aluminium	36	0.0278
	total resistance $[\Omega]$		Bismuth	0.83	1.2
	. ,	-1	Lead	4.84	0.2066
$ R_n =$	individual resistance [9	2]	Cadmium	13	0.0769
Ch			Iron wire	6.710	0.150,1
Snui	nt connection of resist	ors:	Gold	43.5 58	0.023 0.01724
$\frac{1}{D} =$	$\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}$	1	Copper Magnesium	22	0.01724
K	H_1 H_2 H_3	⊣ n	Nickel	14.5	0.043
R =	total resistance $[\Omega]$		Platinum	9.35	0.107
_{B-} =	individual resistance [9	\mathbf{O}	Mercury	1.04	0.962
ı'ın –	marriada rosistanos [2	- J	Silver	61	0.0164
Elec	tric power:		Tantalum	7.4	0.135
	Power	Current	Tungsten	18.2	0.055
	rowei	consumption	Zinc	16.5	0.061
t			Tin	8.3	0.12
Direct current					
l nc	$P = U \cdot I$	$I = \frac{P}{II}$	b) Alloys		
ct	$P = 0 \cdot 1$	ı – U	Aldrey (AlMgSi)	30.0	0.033
)ire			Bronze I	48	0.02083
-			Bronze II Bronze III	36 18	0.02778 0.05556
ıt			Constantan (WM 50)	2.0	0.05556
Single-phase alternating current			Manganin	2.32	0.43
as		Б.	Brass	15.9	0.063
-d- βC	$P = U \cdot I \cdot \cos \varphi$	$I = \frac{P}{U \cdot \cos \varphi}$	Nickel silver (WM 30)	3.33	0.30
gle atii	·	U·cos φ	Nickel chromium	0.92	1.09
Sin			Niccolite (WM 43)	2.32	0.43
alt			Platinum rhodium	5.0	0.20
L			Steel wire (WM 13)	7.7	0.13
ent			Wood's metal	1.85	0.54
Three-phase current					
99	D 470 H I 200	, Р	c) Other		
nas	$P = 1.73 \cdot U \cdot I \cdot \cos \varphi$	$1 = \frac{1}{1.73 \cdot U \cdot \cos \varphi}$	conductors Graphite	0.046	22
ld-6			Carbon, homog.	0.046	65
ree			Retort graphite	0.013	70
F			Tiotort grapinio	0.011	, 0
Resi	stance of a conductor	•			
R =	$\frac{1}{\gamma \cdot A} = \frac{1 \cdot \varrho}{A}$				
$R = resistance(\Omega)$					
I = length of conductor (m)					
	electric conductivity (m.				
	cross section of conduc				
	specific electrical resist				
	$(\Omega \text{ mm}^2/\text{m})$				
			1		

56

$$n = \frac{f \cdot 60}{p}$$

 $n = speed (min^{-1})$

f = frequency (Hz)

p = number of pole pairs

Example: f = 50 Hz, p = 2

$$n = \frac{50 \cdot 60}{2} = 1500 \text{ min}^{-1}$$

Efficiency:

$$\eta = \frac{P_{ab}}{P_{zu}} \cdot 100 \left[\%\right]^{1)}$$

Example:

Efficiency and power factor of a four-pole 1.1-kW motor and a 132-kW motor dependent on the load

Power rating:

Output power 1)

Direct current:

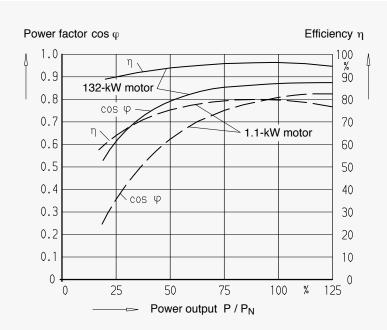
 $P_{ab} = U \cdot I \cdot \eta$

Single-phase alternating current:

 $P_{ab} = U \cdot I \cdot \cos \varphi \cdot \eta$

Three-phase current:

 $\mathsf{P}_{\mathsf{ab}} = 1.73 \cdot \mathsf{U} \cdot \mathsf{I} \cdot \mathsf{cos} \phi \cdot \mathsf{\eta}$



1) P_{ab} = mechanical output power on the motor shaft
 P_{zu} = absorbed electric power

Electrical EngineeringTypes of Construction and Mounting Arrangements of Rotating Electrical Machinery

Types of construction and mounting arrangements of rotating electrical machinery (Extract from DIN EN 50347)									
	Machines with end shields, horizontal arrangement								
	Design			E	xplanation				
Sym- bol	Figure	Bearings	Stator (Housing)	Shaft	General design	Design / Explanation Fastening or Installation			
В3		2 end shields	with feet	free shaft end	-	installation on substructure			
B 5		2 end shields	without feet	free shaft end	mounting flange close to bearing, access from housing side	flanged			
В6		2 end shields	with feet	free shaft end	design B3, if necessary end shields turned through -90°	wall fastening, feet on LH side when looking at input side			
В7		2 end shields	with feet	free shaft end	design B3, if necessary end shields turned through 90°	wall fastening, feet on RH side when looking at input side			
В8	<u> </u>	2 end shields	with feet	free shaft end	design B3, if necessary end shields turned through 180°	fastening on ceiling			
В 35		2 end shields	with feet	free shaft end	mounting flange close to bearing, access from housing side	installation on substructure with additional flange			

Machines with end shields, vertical arrangement								
I	Design			E	xplanation			
Sym- bol	Figure	Bearings	Stator (Housing)	Shaft	Design / Explanation Fastening or Installation			
V 1		2 end shields	without feet	free shaft end at the bottom	mounting flange close to bearing on input side, access from housing side	flanged at the bottom		
V 3		2 end shields	without feet	free shaft end at the top	mounting flange close to bearing on input side, access from housing side	flanged at the top		
V 5		2 end shields	with feet	free shaft end at the bottom	-	fastening to wall or on substructure		
V 6		2 end shields	with feet	free shaft end at the top	-	fastening to wall or on substructure		

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Electrical Engineering

Types of Protection for Electrical Equipment (Protection Against Contact and Foreign Bodies)

Designation DIN number Code letters First type number Second type number An enclosure with this designation is protected against the ingress of solid foreign bodies having a diameter above 1 mm and of splashing water. Degrees of protection for protection against contact and foreign bodies (first type number) Protection against the ingress of solid foreign bodies having a diameter above 50 mm (large foreign bodies) 1) No protection against the ingress of solid foreign bodies having a diameter above 50 mm (large foreign bodies) 1) No protection against intended access, e.g. by hand, however, protection of persons against contact with live parts Protection against the ingress of solid foreign bodies having a diameter above 12 mm (medium-sized foreign bodies) 1) Keeping away of fingers or similar objects Protection against the ingress of solid foreign bodies having a diameter above 2.5 mm (small foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 2.5 mm Protection against the ingress of solid foreign bodies having a diameter above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm Protection against the ingress of solid foreign bodies having a diameter above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm (grain sized foreign bodies) 1) 2) Complete protection against the ingress of dust (dust-tight) Complete protection against the ingress of dust (dust-tight) Complete protection against contact	Types of protection for electrical equipment (Extract from DIN EN 60529)									
DIN number Code letters First type number Second type number An enclosure with this designation is protected against the ingress of solid foreign bodies having a diameter above 1 mm and of splashing water. Degrees of protection for protection against contact and foreign bodies (first type number) First type number Degree of protection (Protection against contact and foreign bodies) No special protection Protection against the ingress of solid foreign bodies having a diameter above 50 mm (large foreign bodies) 1) No protection against intended access, e.g. by hand, however, protection of persons against contact with live parts Protection against the ingress of solid foreign bodies having a diameter above 12 mm (medium-sized foreign bodies) 1) Keeping away of fingers or similar objects Protection against the ingress of solid foreign bodies having a diameter above 2.5 mm (small foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 2.5 mm Protection against the ingress of solid foreign bodies having a diameter above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 2.5 mm Protection against harmful dust covers. The ingress of dust is not entirely prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3) Complete protection against the ingress of dust (dust-tight)	Example of	designation Type of protection DIN EN 60529 IP 4 4								
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50 mm (large foreign bodies) 1) No protection against intended access, e.g. by hand, however, protection of persons against contact with live parts Protection against the ingress of solid foreign bodies having a diameter above 12 mm (medium-sized foreign bodies) 1) Keeping away of fingers or similar objects Protection against the ingress of solid foreign bodies having a diameter above 2.5 mm (small foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 2.5 mm Protection against the ingress of solid foreign bodies having a diameter above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm Protection against harmful dust covers. The ingress of dust is not entirely prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3) Complete protection against contact Protection against the ingress of dust (dust-tight)	0	No special protection								
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2.5 mm (small foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 2.5 mm Protection against the ingress of solid foreign bodies having a diameter above 1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm Protection against harmful dust covers. The ingress of dust is not entirely prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3) Complete protection against contact Protection against the ingress of dust (dust-tight)	2	12 mm (medium-sized foreign bodies) 1)								
1 mm (grain sized foreign bodies) 1) 2) Keeping away tools, wires or similar objects having a thickness above 1 mm Protection against harmful dust covers. The ingress of dust is not entirely prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3) Complete protection against contact Protection against the ingress of dust (dust-tight)	3	2.5 mm (small foreign bodies) 1) 2)								
 prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3) Complete protection against contact Protection against the ingress of dust (dust-tight) 	4	1 mm (grain sized foreign bodies) 1) 2)								
	5	prevented, however, dust may not enter to such an amount that operation of the equipment is impaired (dustproof). 3)								
	6	Protection against the ingress of dust (dust-tight) Complete protection against contact								

- For equipment with degrees of protection from 1 to 4, uniformly or non-uniformly shaped foreign bodies with three dimensions perpendicular to each other and above the corresponding diameter values are prevented from ingress.
- 2) For degrees of protection 3 and 4, the respective expert commission is responsible for the application of this table for equipment with drain holes or cooling air slots.
- 3) For degree of protection 5, the respective expert commission is responsible for the application of this table for equipment with drain holes.

Electrical EngineeringTypes of Protection for Electrical Equipment (Protection Against Water)

Types of protection for electrical equipment (Extract from DIN EN 60529)								
Example of designation Type of protection DIN EN 60529 IP 4 4								
Designation DIN number								
Second type An enclosure	number with this designation is protected against the ingress of solid foreign bodies neter above 1 mm and of splashing water.							
	ees of protection for protection against water (second type number)							
Second type number	Degree of protection (Protection against water)							
0	No special protection							
1	Protection against dripping water falling vertically. It may not have any harmful effect (dripping water).							
2	Protection against dripping water falling vertically. It may not have any harmful effect on equipment (enclosure) inclined by up to 15° relative to its normal position (diagonally falling dripping water).							
3	Protection against water falling at any angle up to 60° relative to the perpendicular. It may not have any harmful effect (spraying water).							
4	Protection against water spraying on the equipment (enclosure) from all directions. It may not have any harmful effect (splashing water).							
5	Protection against a water jet from a nozzle which is directed on the equipment (enclosure) from all directions. It may not have any harmful effect (hose-directed water).							
6	Protection against heavy sea or strong water jet. No harmful quantities of water may enter the equipment (enclosure) (flooding).							
7	Protection against water if the equipment (enclosure) is immersed under determined pressure and time conditions. No harmful quantities of water may enter the equipment (enclosure) (immersion).							
8	The equipment (enclosure) is suitable for permanent submersion under conditions to be described by the manufacturer (submersion). 1)							
	ee of protection is normally for air-tight enclosed equipment. For certain equipment, water may enter provided that it has no harmful effect.							

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8

Materials Conversion of Fatigue Strength Values of Miscellaneous Materials

Conversion of fatigue strength values of miscellaneous materials									
Material	Tensio	on ³⁾	Е	Bending 1)		Torsion 1)			
wateriai	σ_{W}	σ_{Sch}	σ_{bW}	$\sigma_{ extsf{bSch}}$	σ_{bF}	τ_{W}	$ au_{Sch}$	τ_{F}	
Structural steel	0.45 · R _m	1.3 · σ _W	0.49 · R _m	1.5 · σ _{bW}	1.5 · R _e	0.35 · R _m	1.1·τ _W	0.7 · R _e	
Quenched and tempered steel	0.41 · R _m	1.7 · σ _W	0.44 · R _m	1.7 · σ _{bW}	1.4 · R _e	0.30 · R _m	1.6·τ _W	0.7 · R _e	
Case hardening steel	0.40 · R _m	1.6 · σ _W	0.41 · R _m	1.7 · σ _{bW}	1.4 · R _e	0.30 · R _m	1.4·τ _W	0.7 · R _e	
Grey cast iron	0.25 · R _m	1.6 · σw	0.37 · R _m	1.8 · σ _{bW}	-	0.36 · R _m	1.6·τ _W	-	
Light metal	0.30 · R _m	-	0.40 · R _m	_	-	0.25 · R _m	-	-	

- 1) For polished round section test piece of about 10 mm diameter.
- Case-hardened; determined on round section test piece of about 30 mm diameter. R_m and R_e of core material.
- 3) For compression, σ_{Sch} is larger, e.g. for spring steel $\sigma_{dSch}\approx$ 1.3 · σ_{Sch} For grey cast iron $\sigma_{dSch}\approx$ 3 · σ_{Sch}

Ultimate stress values	Type of load						
Offiliate Stress values	Tension	Bending	Torsion				
Tensile strength	R _m	-	_				
Yield point	R _e	σ_{bF}	$ au_{F}$				
Fatigue strength under alternating stresses	σ_{W}	σ _{bW}	τ _W				
Fatigue strength under fluctuating stresses	σ _{Sch}	σ _{bSch}	τ _{Sch}				

Materials Mechanical Properties of Quenched and Tempered Steels

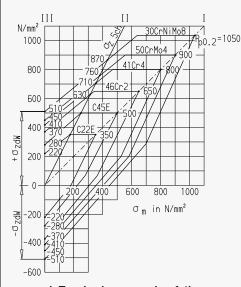
Quenched and tempered steels (Extract from DIN EN 10083) Mechanical properties of steels in quenched and tempered condition Diameter Material above 16 above 40 above 100 above 160 up to 16 mm up to 40 mm up to 100 mm up to 160 mm up to 250 mm Viald Yield Yield Yield Yield point point point point point Tensile Tensile Tensile Tensile Tensile (0.2 (0.2 (0.2 (0.2)(0.2 Numstrength strength strength strength strength Gr) Gr) Gr) Gr) Gr) Symbol N/mm² N/mm² N/mm² N/mm² N/mm² N/mm² N/mm² N/mm² N/mm² N/mm² ber min. min. min. min. R_{m} min. R_{m} R_{m} R_{m} R_{m} R_{e} R_{e} R_{e} R_{e} Re R_{p 0.2} R_{p 0.2} R_{p 0.2} R_{p 0.2} Rn 0 2 C22 1.0402 350 550 - 700 300 500-650 C35 1.0501 430 630 - 780370 600 - 750320 550 - 700 C45 1.0503 500 700 - 850 430 650 - 800370 630 - 780C55 1.0535 550 800 - 950 500 750 - 900 430 700 - 850 C60 1.0601 580 850-1000 520 800 - 950 450 750 - 900 C22E 1 1151 350 550 - 700 300 500 - 650 C35E 1.1181 430 630 - 780370 600 - 750320 550 - 700 1.1180 C35R 430 630 - 780370 600 - 750320 550 - 700 C45E 1.1191 500 700 - 850 430 650 - 800370 630 - 7801.1201 700-850 650 - 800 370 C45R 500 430 630 - 780C55E 1.1203 550 800 - 950 500 750 - 900 430 700 - 850 800-950 C55R 1.1209 550 500 750 - 900 430 700 - 850 1.1221 C60E 580 850-1000 520 800 - 950 450 750 - 900 C60R 1.1223 580 850-1000 520 800 - 950 450 750 - 900 28Mn6 1.1170 590 780 - 930 490 690 - 840 440 640 - 79038Cr2 1.7003 550 800 - 950 450 700-850 350 600 - 75046Cr2 1.7006 650 900-1100 550 800 - 950 400 650 - 8001.7033 900-1100 800 - 950 460 700 - 850 34Cr4 700 590 34CrS4 1.7037 700 900-1100 590 800 - 950 460 700 - 850 37Cr4 1.7034 750 950-1150 630 850-1000 510 750 - 900 37CrS4 1.7038 750 950-1150 630 850-1000 510 750 - 900 41Cr4 1.7035 800 1000-1200 660 900-1100 560 800 - 950 41CrS4 1.7039 800 1000-1200 660 900-1100 560 800 - 950 25CrMo4 1.7218 700 900-1100 600 800 - 950 450 700-850 400 650-800 34CrMo4 1.7220 800 1000-1200 650 900-1100 550 800 - 950500 750-900 450 700-850 34CrMoS4 1.7226 800 1000-1200 650 900-1100 550 800 - 950 500 750- 900 450 700-850 42CrMo4 1.7225 900 1100-1300 750 1000-1200 650 900-1100 550 800- 950 500 750- 900 42CrMoS4 1.7227 900 1100-1300 750 1000-1200 650 900-1100 550 800-950 500 750-900 700 650 50CrMo4 1.7228 900 1100-1300 780 1000-1200 900-1100 850-1000 550 800-950 36CrNiMo4 1.6511 900 1100-1300 800 1000-1200 700 900-1100 600 800- 950 750-900 550 1000 1200-1400 900 1100-1300 800 1000-1200 700 900-1100 800- 950 34CrNiMo6 1.6582 600 30CrNiMo8 1.6580 1050 1250-1450 1050 1250-1450 900 1100-1300 800 700 900-1100 1000-1200 51CrV4 1.8159 900 1100-1300 800 1000-1200 700 900-1100 650 850-1000 600 800-950 30CrMoV9 1.7707 1050 1250-1450 1020 1200-1450 900 1100-1300 800 1000-1200 700 900-1100

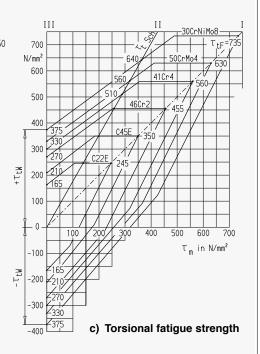
Ш

1400

-600

Fatigue strength diagrams of quenched and tempered steels, DIN EN 10083 (in quenched and tempered condition, test piece diameter d = 10 mm)





a) Tension/compression fatigue strength

П

 N/mm^2 1200 1000 930 800 600 400 MQD+ 200 0 600 800 1000 1200 1400 σ_{m} in N/mm 2 -200 MaD-

b) Bending fatigue strength

Quenched and tempered steels not illustrated may be used as follows:

34CrNiMo6 like 30CrNiMo8 30CrMoV4 like 30CrNiMo8 42CrMo4 like 50CrMo4 36CrNiMo4 like 50CrMo4 51CrV4 like 50CrMo4 34CrMo4 like 41Cr4 28Cr4 like 46Cr2 C45 like C45E C22 like C22E

C60 and C50 lie approximately between C45E and 46Cr2. C40, 32Cr2, C35, C30 and

C40, 32Cr2, C35, C30 and C25 lie approximately between C22E and C45E.

Loading type II: static

Loading type II: dynamic

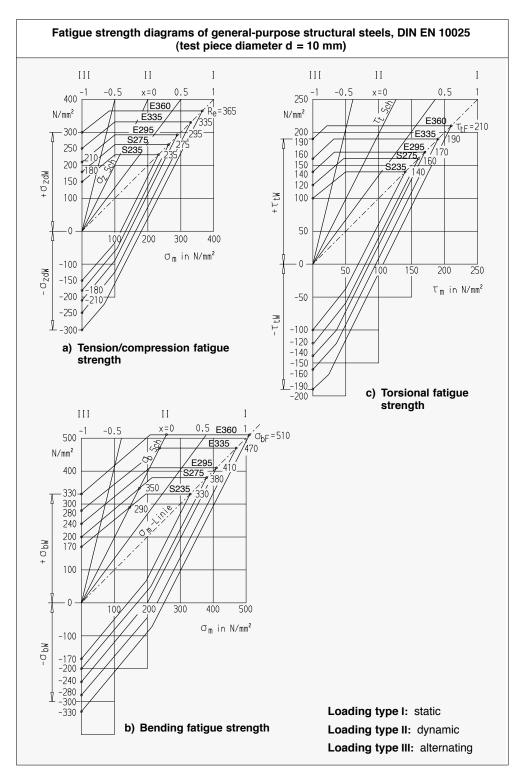
Loading type III: alternating

	General-purpose structural steels (Extract from DIN EN 10025)											
Material		Treat- ment condi-			Upper yield point R _{eH} in N/mm ² (minimum) for product thickness							
Symbol	Num-	Symbol acc. to	tion		in mm	1000		ρic		nm	733	
(in Germany)	ber	DIN EN 10025	1)	<3	≥3 ≤100	>100	≤16	>16 ≤40	>40 ≤63	>63 ≤80	>80 ≤100	>100
St33	1.0035	S185	U, N	310 540	290 510		185	175 2)	-	-	-	
St37-2 USt37-2	1.0037 1.0036	S235JR S235JRG1	U, N U, N				235	225	215	205	195	
RSt37-2 St37-3U St37-3N	1.0038 1.0114 1.0116	S235JRG2 S235JO S235J2G3	U, N, U N	360 510	340 470	uodn p	235	225	215	215	215	uodn p
St44-2 St44-3U St44-3N	1.0044 1.0143 1.0144	S275JR S275JO S275J2G3	U, N U N	430 580	410 560	To be agreed upon	275	265	255	245	235	To be agreed upon
St52-3U St52-3N	1.0553 1.0570	S355JO S355J2G3	U N	510 680	490 630		355	345	335	325	315	
St50-2	1.0050	E295	U, N	490 660	470 610		295	285	275	265	255	
St60-2	1.0060	E335	U, N	590 770	570 710		335	325	315	305	295	
St70-2	1.0070	E360	U, N	690 900	670 830		365	355	345	335	325	

¹⁾ N normalized; U hot-rolled, untreated

²⁾ This value applies to thicknesses up to 25 mm only

Fatigue Strength Diagrams of General-Purpose Structural Steels

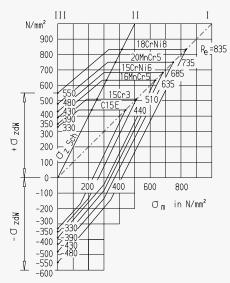


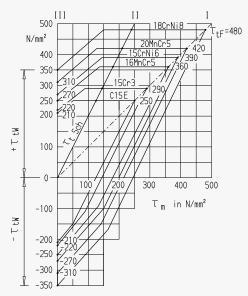
Ca	Case hardening steels; Quality specifications (Extract from DIN EN 10084)									
Material			1)	1) For dia. 11			dia. 30	For dia. 63		
Symbol (in Germany)	Num- ber	Symbol acc. to DIN EN 10084	Treatment condition	Yield point R _e N/mm ² min.	Tensile strength R _m N/mm ²	Yield point R _e N/mm ² min.	Tensile strength R _m N/mm ²	Yield point R _e N/mm ² min.	Tensile strength R _m N/mm ²	
C10 Ck10	1.0301 1.1121	C10 C10E		390 390	640 – 790 640 – 790	295 295	490 – 640 490 – 640	1 1	1 1	
C15 Ck15 Cm15	1.0401 1.1141 1.1140	C15 C15E C15R		440 440 440	740 – 890 740 – 890 740 – 890	355 355 355	590 – 790 590 – 790 590 – 790	- - -	- - -	
15Cr13	1.7015	15Cr13	1008	510	780-1030	440	690- 890	-	-	
16MnCr5 16MnCrS5 20MnCr5 20MnCrS5	1.7131 1.7139 1.7147 1.7149	16MnCr5 16MnCrS5 20MnCr5 20MnCrS5	tails, see DIN EN 10084	635 635 735 735	880-1180 880-1180 1080-1380 1080-1380	590 590 685 685	780-1080 780-1080 980-1280 980-1280	440 440 540 540	640 – 940 640 – 940 780 – 1080 780 – 1080	
20MoCr4 20MoCrS4 25MoCrS4	1.7321 1.7323 1.7325	20MoCr4 20MoCrS4 25MoCrS4	For details,	635 635 735	880 –1180 880 –1180 1080 –1380	590 590 685	780 –1080 780 –1080 980 –1280	- - -	- - -	
15CrNi6 18CrNi8	1.5919 1.5920	15CrNi6 18CrNi8		685 835	960-1280 1230-1480	635 785	880-1180 1180-1430	540 685	780-1080 1080-1330	
17CrNiMo6	1.6587	18CrNiMo7-6		835	1180-1430	785	1080-1330	685	980-1280	

1) Dependent on treatment, the Brinell hardness is different.

Treatment condition	Meaning		
С	treated for shearing load		
G	soft annealed		
BF	treated for strength		
BG	treated for ferrite/pearlite structure		

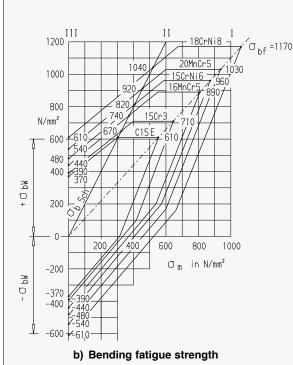
Fatigue strength diagrams of case hardening steels, DIN EN 10084 (Core strength after case hardening, test piece diameter d = 10 mm)





a) Tension/compression fatigue strength

c) Torsional fatigue strength



Case hardening steels not illustrated may be used as follows:

25MoCr4 like 20MnCr5 17CrNiMo6 like 18CrNi8

Loading type II: static
Loading type II: dynamic
Loading type III: alternating

Materials Cold Rolled Steel Strips Cast Steels for General Engineering Purposes

Co	ld rolled steel strips	(Extract from DIN EN 101	132)
	Material		Tensile strength
Symbol (in Germany)	Number	Symbol acc. to DIN EN 10132	R _m ¹⁾ N/mm ² maximum
C55 Ck55	1.0535 1.1203	C55 C55E	610
C60 Ck60	1.0601 1.1221	C60 C60E	620
C67 Ck67	1.0603 1.1231	C67 C67S	640
C75 Ck75	1.0605 1.1248	C75 C75S	640
Ck85 Ck101	1.1269 1.1274	C85S C100S	670 690
71Si7	1.5029	71Si7	800
67SiCr5	1.7103	67SiCr5	800
50CrV4	1.8159	50CrV4	740

1) $R_{\rm m}$ for cold rolled and soft-annealed condition; for strip thicknesses up to 3 mm

Cast steels	for general er	ngineering purp	oses (Extract f	rom DIN 168	1)
Material		Yield point R _{e,} R _{p 0.2}	Tensile strength R _m	(ISO-V-notch	impact work n specimens) A _v > 30 mm
Symbol	Number	N/mm ² min.	N/mm ² min.	Mean v m	J
GS-38 (GE200)	1.0420	200	380	35	35
GS-45 (GE240)	1.0446	230	450	27	27
GS-52 (GE260)	1.0552	260	520	27	22
GS-60 (GE300)	1.0558	300	600	27	20

The mechanical properties apply to specimens which are taken from test pieces with thicknesses up to 100 mm. Furthermore, the yield point values also apply to the casting itself, in so far as the wall thickness is \leq 100 mm.

¹⁾ Determined from three individual values each.

	Round steel wire for springs (Extract from DIN EN 10218)								
Diameter		Grade	of wire						
of wire	A B C D								
mm		Tensile strengtl	h R _m in N/mm ²						
0.07	-	_	-	2800 – 3100					
0.3	-	2370 – 2650	-	2660 – 2940					
1	1720 – 1970	1980 – 2220	-	2230 – 2470					
2	1520 – 1750	1760 – 1970	1980 – 2200	1980 – 2200					
3	1410 – 1620	1630 – 1830	1840 – 2040	1840 – 2040					
4	1320 – 1520	1530 – 1730	1740 – 1930	1740 – 1930					
5	1260 – 1450	1460 – 1650	1660 – 1840	1660 – 1840					
6	1210 – 1390	1400 – 1580	1590 – 1770	1590 – 1770					
7	1160 – 1340	1350 – 1530	1540 – 1710	1540 – 1710					
8	1120 – 1300	1310 – 1480	1490 – 1660	1490 – 1660					
9	1090 – 1260	1270 – 1440	1450 – 1610	1450 – 1610					
10	1060 – 1230	1240 – 1400	1410 – 1570	1410 – 1570					
11	-	1210 – 1370	1380 – 1530	1380 – 1530					
12	-	1180 – 1340	1350 – 1500	1350 – 1500					
13	-	1160 – 1310	1320 – 1470	1320 – 1470					
14	-	1130 – 1280	1290 – 1440	1290 – 1440					
15	-	1110 – 1260	1270 – 1410	1270 – 1410					
16	-	1090 – 1230	1240 – 1390	1240 – 1390					
17	-	1070 – 1210	1220 – 1360	1220 – 1360					
18	-	1050 – 1190	1200 – 1340	1200 – 1340					
19	-	1030 – 1170	1180 – 1320	1180 – 1320					
20	_	1020 – 1150	1160 – 1300	1160 – 1300					

Materials Lamellar Graphite Cast Iron Nodular Graphite Cast Iron

	Lamellar (graphite cas	t iron (E	xtract fro	om DIN EN 1	561)	
	Material		thickn	all lesses mm	Tensile strength ¹⁾ R _m	Brinell hardness	Compressive strength ²⁾
Symbol	Number	Symbol acc. to DIN 1691	above	up to	N/mm ²	HB 30	N/mm ²
EN-GJL-100	EN-JL1010	GG-10	5	40	min. 100 ²⁾	_	_
EN-GJL-150	EN-JL1020	GG-15	10 20 40 80	20 40 80 150	130 110 95 80	225 205 – –	600
EN-GJL-200	EN-JL1030	GG-20	10 20 40 80	20 40 80 150	180 155 130 115	250 235 – –	720
EN-GJL-250	EN-JL1040	GG-25	10 20 40 80	20 40 80 150	225 195 170 155	265 250 – –	840
EN-GJL-300	EN-JL1050	GG-30	10 20 40 80	20 40 80 150	270 240 210 195	285 265 – –	960
EN-GJL-350	EN-JL1060	GG-35	10 20 40 80	20 40 80 150	315 280 250 225	285 275 – –	1080

The values apply to castings which are made in sand moulds or moulds with comparable heat diffusibility.

- 1) These values are reference values.
- 2) Values in the separately cast test piece with 30 mm diameter of the unfinished casting.

N	Nodular graphite cast iron (Extract from DIN EN 1563)									
	Properties in cast-on test pieces									
M	aterial		Wall thickness of casting	Thickness of cast-on test piece	Tensile strength R _m	0.2% proof stress R _{p0.2}				
Symbol	Number	Symbol acc. to DIN 1693	mm	mm	N/mm ²	N/mm ²				
EN-GJS-400-18U-LT	EN-JS1049	GGG-40.3	from 30 up to 60 above 60 up to 200	40 70	390 370	250 240				
EN-GJS-400-15U	EN-JS1072	GGG-40	from 30 up to 60 above 60 up to 200	40 70	390 370	250 240				
EN-GJS-500-7U	EN-JS1082	GGG-50	from 30 up to 60 above 60 up to 200	40 70	450 420	300 290				
EN-GJS-600-3U	EN-JS1092	GGG-60	from 30 up to 60 above 60 up to 200	40 70	600 550	360 340				
EN-GJS-700-2U	EN-JS1102	GGG-70	from 30 up to 60 above 60 up to 200	40 70	700 650	400 380				

MaterialsCopper-Tin and Copper-Zinc-Tin Casting Alloys Copper-Aluminium Casting Alloys

Copper-tin a	and coppe	er-zinc-tin casting	g alloys (Extract from	DIN EN 1982)
N	laterial	Symbol acc.	Condition on delivery	0.2% proof stress ¹⁾ R _{p0.2} min. in	Tensile strength 1) R _m min in
Symbol	Number	to DIN 1705		N/mm ²	N/mm ²
CuSn12-C-GS CuSn12-C-GZ CuSn12-C-GC	CC483K	G-CuSn12 GZ-CuSn12 GC-CuSn12	Sand-mould cast iron Centrifugally cast iron Continuously cast iron	140 150 140	260 280 280
CuSn12Ni-C-GS CuSn12Ni-C-GZ CuSn12Ni-C-GC	CC484K	G-CuSn12Ni GZ-CuSn12Ni GC-CuSn12Ni	Sand-mould cast iron Centrifugally cast iron Continuously cast iron	160 180 170	280 300 300
CuSn12Pb2-C-GS CuSn12Pb2-C-GZ CuSn12Pb2-C-GC	CC482K	G-CuSn12Pb GZ-CuSn12Pb GC-CuSn12Pb	Sand-mould cast iron Centrifugally cast iron Continuously cast iron	140 150 140	260 280 280
CuSn10-Cu-GS	CC480K	G-CuSn10	Sand-mould cast iron	130	270
CuSn7Zn4Pb7-C-GS CuSn7Zn4Pb7-C-GZ CuSn7Zn4Pb7-C-GC	CC493K	G-CuSn7ZnPb GZ-CuSn7ZnPb GC-CuSn7ZnPb	Sand-mould cast iron Centrifugally cast iron Continuously cast iron	120 130 120	240 270 270
CuSn7Zn2Pb3-C-GS	CC492K	G-CuSn6ZnNi	Sand-mould cast iron	140	270
CuSn5Zn5Pb5-C-GS	CC491K	G-CuSn5ZnPb	Sand-mould cast iron	90	220
CuSn3Zn8Pb5-C-GS	CC490K	G-CuSn2ZnPb	Sand-mould cast iron	90	210

1) Material properties in the test bar

Coppe	Copper-aluminium casting alloys (Extract from DIN EN 1982)									
Ma Symbol	Number	Symbol acc. to DIN 1714	Condition on delivery	$\begin{array}{c} 0.2\%\\ \text{proof stress} ^{1)}\\ R_{p0.2}\\ \text{min. in}\\ \text{N/mm}^2 \end{array}$	Tensile strength ¹⁾ R _m min. in N/mm ²					
CuAl10Fe2-C-GS	CC331G	G-CuAl10Fe	Sand-mould cast iron	180	500					
CuAl10Fe2-C-GM		GK-CuAl10Fe	Chilled casting	200	550					
CuAl10Fe2-C-GZ		GZ-CuAl10Fe	Centrifugally cast iron	200	550					
CuAl10Ni3Fe2-C-GS	CC332G	G-CuAl9Ni	Sand-mould cast iron	200	500					
CuAl10Ni3Fe2-C-GK		GK-CuAl9Ni	Chilled casting	230	530					
CuAl10Ni3Fe2-C-GZ		GZ-CuAl9Ni	Centrifugally cast iron	250	600					
CuAl10Fe5Ni5-C-GS	CC333G	G-CuAl10Ni	Sand-mould cast iron	270	600					
CuAl10Fe5Ni5-C-GM		GK-CuAl10Ni	Chilled casting	300	600					
CuAl10Fe5Ni5-C-GZ		GZ-CuAl10Ni	Centrifugally cast iron	300	700					
CuAl10Fe5Ni5-C-GC		GC-CuAl10Ni	Continuously cast iron	300	700					
CuAl11Fe6Ni6-C-GS	CC334G	G-CuAl11Ni	Sand-mould cast iron	320	680					
CuAl11Fe6Ni6-C-GM		GK-CuAl11Ni	Chilled casting	400	680					
CuAl11Fe6Ni6-C-GZ		GZ-CuAl11Ni	Centrifugally cast iron	400	750					

¹⁾ Material properties in the test bar

Aluminium casting alloys (Extract from DIN EN 1706)									
	Material		0.2% proof stress R _{p0.2}	Tensile strength R _m					
Symbol	Number	Symbol acc. to DIN 1725-2	in N/mm ²	in N/mm ²					
AC-AlCu4MgTi	AC-21000	G-AlCu4TiMg	200 up to 220	300 up to 320					
AC-AlCu4Ti	AC-21100	G-AlCu4Ti	180 up to 220	280 up to 330					
AC-AlSi7Mg	AC-42100	G-AlSi7Mg	180 up to 210	230 up to 290					
AC-AlSi10Mg(a)	AC-43000	G-AlSi10Mg	80 up to 220	150 up to 240					
AC-AlSi10Mg(Cu)	AC-43200	G-AlSi10Mg(Cu)	80 up to 200	160 up to 240					
AC-AlSi9Mg	AC-43300	G-AlSi9Mg	180 up to 210	230 up to 290					
AC-AlSi10Mg(Fe)	AC-43400	G-AlSi10Mg	140	240					
AC-AISi11	AC-44000	G-AlSi11	70 up to 80	150 up to 170					
AC-AlSi12(a)	AC-44200	G-AlSi12	70 up to 80	150 up to 170					
AC-AlSi12(Fe)	AC-44300	GD-AlSi12	130	240					
AC-AlSi6Cu4	AC-45000	G-AlSi6Cu4	90 up to 100	150 up to 170					
AC-AlSi9Cu3(Fe)	AC-46000	GD-AlSi9Cu3	140	240					
AC-AlSi8Cu3	AC-46200	G-AlSi9Cu3	90 up to 140	150 up to 240					
AC-AlSi12(Cu)	AC-47000	G-AlSi12(Cu)	80 up to 90	150 up to 170					
AC-AlSi12Cu1(Fe)	AC-47100	GD-AlSi12(Cu)	140	240					
AC-AlMg3(a)	AC-51100	G-AIMg3	70	140 up to 150					
AC-AIMg9	AC-51200	GD-AIMg9	130	200					
AC-AIMg5	AC-51300	G-AIMg5	90 up to 100	160 up to 180					
AC-AIMg5(Si)	AC-51400	G-AIMg5Si	100 up to 110	160 up to 180					

Materials Lead and Tin Casting Alloys for Babbit Sleeve Bearings

Lead and tin cas	Lead and tin casting alloys for babbit sleeve bearings (Extract from DIN ISO 4381)									
Material	Material			ss ¹⁾ 80	0.2% proof stress ¹⁾ R _{p 0.2} in N/mm ²					
Symbol	Number	20 °C	50 °C	120 °C	20 °C	50 °C	100 °C			
PbSb15SnAs	2.3390	18	15	14	39	37	25			
PbSb15Sn10	2.3391	21	16	14	43	32	30			
PbSb14Sn9CuAs	2.3392	22	22	16	46	39	27			
PbSb10Sn6	2.3393	16	16	14	39	32	27			
SnSb12Cu6Pb	2.3790	25	20	12	61	60	36			
SnSb8Cu4	2.3791	22	17	11	47	44	27			
SnSb8Cu4Cd	2.3792	28	25	19	62	44	30			

¹⁾ Material properties in the test bar

Materials Conversion of Hardness Values (DIN EN ISO 18265)

Tensile strength	Vickers hard- ness	Brinell hardness			kwell ness		Tensile strength	Vickers hard- ness	Brinell hardness		ockwe	
N/mm ²	(F≥98N)	$\left(0.102 \cdot \frac{F}{D^2} = 30 \frac{N}{mm^2}\right)$	HRB	HRC	HRA	HRD	N/mm ²	(F≥98N)	$\left(0.102 \cdot \frac{F}{D^2} = 30 \frac{N}{mm^2}\right)$	HRC	HRA	HRD
255 270 285 305 320	80 85 90 95 100	76.0 80.7 85.5 90.2 95.0	41.0 48.0 52.0 56.2				1155 1190 1220 1255 1290	360 370 380 390 400	342 352 361 371 380	36.6 37.7 38.8 39.8 40.8	69.2 69.8	52.8 53.6 54.4 55.3 56.0
335 350 370 385 400	105 110 115 120 125	99.8 105 109 114 119	62.3 66.7				1320 1350 1385 1420 1455	410 420 430 440 450	390 399 409 418 428	41.8 42.7 43.6 44.5 45.3	71.4 71.8 72.3 72.8 73.3	56.8 57.5 58.2 58.8 59.4
415 430 450 465 480	130 135 140 145 150	124 128 133 138 143	71.275.078.7				1485 1520 1555 1595 1630	460 470 480 490 500	437 447 (456) (466) (475)	46.1 46.9 47.7 48.4 49.1	73.6 74.1 74.5 74.9 75.3	60.1 60.7 61.3 61.6 62.2
495 510 530 545 560	155 160 165 170 175	147 152 156 162 166	81.7 85.0				1665 1700 1740 1775 1810	510 520 530 540 550	(485) (494) (504) (513) (523)	49.8 50.5 51.1 51.7 52.3	75.7 76.1 76.4 76.7 77.0	62.9 63.5 63.9 64.5 64.8
575 595 610 625 640	180 185 190 195 200	171 176 181 185 190	87.1 89.5 91.5				1845 1880 1920 1955 1995	560 570 580 590 600	(532) (542) (551) (561) (570)	53.0 53.6 54.1 54.7 55.2	78.4	65.4 65.8 66.2 66.7 67.0
660 675 690 705 720	205 210 215 220 225	195 199 204 209 214	92.5 93.5 94.0 95.0 96.0				2030 2070 2105 2145 2180	610 620 630 640 650	(580) (589) (599) (608) (618)	55.7 56.3 56.8 57.3 57.8	79.2 79.5	67.5 67.9 68.3 68.7 69.0
740 755 770 785 800	230 235 240 245 250	219 223 228 233 238	96.7 98.1 99.5	21.3	60.7 61.2 61.6	40.3 41.1 41.7		660 670 680 690 700		58.3 58.8 59.2 59.7 60.1	80.3 80.6 80.8 81.1 81.3	69.4 69.8 70.1 70.5 70.8
820 835 850 865 880	255 260 265 270 275	242 247 252 257 261	(101) (102)	24.8	62.0 62.4 62.7 63.1 63.5	42.2 43.1 43.7 44.3 44.9		720 740 760 780 800		61.0 61.8 62.5 63.3 64.0	81.8 82.2 82.6 83.0 83.4	71.5 72.1 72.6 73.3 73.8
900 915 930 950 965	280 285 290 295 300	266 271 276 280 285	(104) (105)	27.8	63.8 64.2 64.5 64.8 65.2	45.3 46.0 46.5 47.1 47.5		820 840 860 880 900		64.7 65.3 65.9 66.4 67.0		74.3 74.8 75.3 75.7 76.1
995 1030 1060 1095 1125	310 320 330 340 350	295 304 314 323 333		31.0 32.3 33.3 34.4 35.5	65.8 66.4 67.0 67.6 68.1			920 940		67.5 68.0	85.3 85.6	76.5 76.9

The figures in brackets are hardness values outside the domain of definition of standard hardness test methods which, however, in practice are frequently used as approximate values. Furthermore, the Brinell hardness values in brackets apply only if the test was carried out with a carbide ball.

- 1) Internationally usual, e.g. ASTM E 18-74 (American Society for Testing and Materials)
- 2) Calculated from HB = 0.95 HV (Vickers hardness)

Determination of Rockwell hardness HRA, HRB, HRC, and HRD acc. to DIN EN 10109 Part 1

Determination of Vickers hardness acc. to DIN 50133 Part 1

Determination of Brinell hardness acc. to DIN EN 10003 Part 1

Determination of tensile strength acc. to DIN EN 10002 Part 1 and Part 5

Values of solids and liquids Mean density of the earth = 5.517 g/cm³

Density Density O	Values o	Values of solids and liquids				Mean density of the earth = 5.517 g/cm ³					
Aluminium brorze	Substance (solid)		6	point	conducti- vity λ at 20 °C	Substance (solid)		Q	point	at 20 °C	
Aluminum bronze	Agate		2.52.8	≈1600	11.20	Porcelain		2.22.5	≈1650	≈1	
Ammony	Aluminium	Al	2.7	658	204	Pyranite		3.3	1800	8.14	
Ammony	Aluminium bronze		7.7	1040	128	Quartz-flint		2.52.8	1480	9.89	
Assertic		Sh					Ra				
Asphatum				_							
Asphaltum		710		1300							
Barium Ba 3.59 704							1111				
Basalt natural 27.32 -7 167 Basyllium Ba 1.85 1280 1.85 1.8		B2			0.096		Dh				
Basalt, natural 2.732 - 1.67 Sand.dry 1.41.6 1480 0.58 Service 1.85 1280 1.65 Sand.dry 1.41.6 1480 0.58 Concrete -2 - -1 Sandstone 2.125 -1.000 2.3 Sand.dry Sandstone 2.125 -1.000 2.3 Sandstone 2.125 -1.000 2.3 Sandstone 2.125 -1.000 2.3 Sandstone 2.125 -1.000 -1.5 Sandstone 2.125 -125 Sandstone 2.125 -1.000 -1.5 Sandstone 2.125 -125 -125 -125 -125 Sandstone 2.125 -		Da									
Beyrllium Be 1.85 1280 1.65 Concrete e					1.67		110				
Concrete		Be		1280							
Lead											
Boron (amorph.) B 1.73 2300 -		Pb		327.4							
Borax					-						
Limonite 3.43 1565					_		S				
Bronze					_						
Chlorine calcium		1			64					_	
Chromium nicke Chromium nic		1		774	-		Se	4.4	220	0.2	
Delta metal	Chromium	Cr	7.1		69						
Diamond	Chromium nickel	1				Silicon			1420		
Iron, pure			8.6	950	104.7	Silicon carbide		3.12	-	15.2	
Grease 0.92034 30175 0.209 Gallium Ga 5.9 29.75	Diamond			-	-				1816		
Gallium Ga 5.9 29.75 Stainless 7.9 1450 14.8 Gypsum 2.3 1200 0.45 Glass, window -2.5 -700 0.81 Hard coal 1.35 0.24 Glass, window -2.5 -700 0.81 Hard coal 1.35 0.24 Glass, window -2.5 -700 0.81 Hard coal 1.35 0.24 Glass, window -2.5 -700 0.81 Hard coal 1.35 0.24 Granite 2.6.2.8 3.5 Glod Au 19.29 1063 310 Granite 2.6.2.8 3.5 Graphite 2.6.2.8 3.5 Graphite 2.6.2.8 3.5 Graphite 1.3142 0.34.0.35 Graphite -1.4 0.17 Hard metal R20 1.3142 0.34.0.35 Hard rubber -1.4 0.17 Hard metal R20 14.8 2000 81 Hard rubber -1.4 0.17 Hard metal R20 1.4.8 2000 81 Hard rubber -1.4 0.17 Hard metal R20 1.4.8 2000 81 Hard rubber -1.4 0.17 Hard metal R20 1.4.8 2000 81 Hard rubber -1.4 0.17 Hard metal R20 1.4.8 2000 81 Hard rubber -1.4 0.17 Hard metal R20 0.45035 0.120.17 Hard rubber 1.1.1.8 0.1402 0.3035 Hard rubber 1.1.1.8 0.1402 Hard rubber 1.		Fe									
Germanium Ge 5.32 936 58.615 Non-magnetic B 1450 16.28					0.209						
Glyssum					-						
Glass, window =2.5 =700 0.81 Milea =2.8 =1300 0.35 Strontium Sr 2.54 797 0.23 Strontium Tall 16.6 2990 54 Strontium Tall 16.7 15.5 4.9 Strontium Tall 16.7 16.7 15.5 Strontium Tall 16.7		Ge									
Mica									1450		
Gold Au 19.29 1063 310 Tantalum Ta 16.6 2990 54 4.9 Graphite C 2.6.2.8 -3.5. Graphite C 2.24 -3800 168 Tellurium Th 11.7 -1800 38 Tiantalum Th 4.5 1670 15.5 Tombac Tiantalum Th 4.5 1670 15.5 Tombac Tiantalum Th 4.5 1670 15.5 Tombac Tomba											
Granite											
Graphite C 2.24 ~3800 168 Grey cast iron 7.25 1200 58		Au		1063							
Grey cast iron				-							
Laminated fabric		C									
Hard rubber				1200			- 11				
Hard metal R20											
Woods		-					-11				
Indium											
Iridium		lm.					· ·		1090		
Cadmium									-		
Potassium											
Limestone											
Calcium oxide (lime)		K								130	
Cacicium oxide (lime)		Co			2.2		US		29	00 12	
Caoutchouc, crude		Ca					Co		630	0.91.2	
Cobalt Co 8.8 1490 69.4 Zirconium Sn 7.2 232 65		-								110	
Salt, common		Co									
Coke		- 00			-						
Constantan S.89 1600 23.3 23.3 23.9 23.3 3.9		-		-	0.184	2001		0.0	.000		
Corundum (AL ₂ O ₃) 3.94 2050 1223 Chalk 1.82.6 - 0.92 Copper Cu 8.9 1083 384 Leather, dry 0.91 - 0.15 Lithium Li 0.53 179 71 Magnesium Mg 1.74 657 157 Magnesium, alloyed 1.81.83 650 69.8145.4 Manganese Mn 7.43 1250 30 Marble 2.62.8 1290 2.8 Belazine -0.73 15 25210 0.13 Marble 2.62.8 1290 2.8 Belazine -0.73 15 25210 0.13 Berass 8.5 900 116 Brass 8.5 900 116 Molybdenum Mo 10.2 2600 145 Monel metal 8.8 *1300 19.7 Sodium Na 0.98 97.5 126 Nickel silver Ni 8.9 1452 59 Nickel Ni 8.9 1452 59 Nickel Ni 0.9 52 0.26 Paladium Pd 12 1552 70.9 Phosphorus (white) P 1.83 444 - Plosphorus (white) P 1.83 444 - Platinum Pt 21.5 1770 70 Substance (liquid) Sym-boll Sym-boll at at 1.013mPa (boll at 1.013MPa at 1		1		1600							
Chalk Copper Cu 8.9 1083 384 Copper Substance (liquid) Symbol Density ρ point at at 1.013MPa Thermal conductivity λ at 20 °C Leather, dry 0.91 - 0.15 - 0.15 - 0.15 - 0.15 - 0.15 λ at 20 °C λ at 20 °C λ at 20 °C λ at 20 °C √ W/(mk) λ at 20 °C √ C √ W/(mk) λ at 20 °C √ C <td></td> <td>1</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>		1									
Copper Cu 8.9 1083 384 10.00 2.00 1.00		1	1.82.6	-	0.92			_	D-iii	Thermai	
Leather, dry		Cu		1083			C	Density _Q		conductivity	
Magnesium Mg 1.74 657 157 Magnesium, alloyed 1.81.83 650 69.8145.4 Ether 0.72 20 35 0.14 Manganese Mn 7.43 1250 30 Benzine ≈0.73 15 25210 0.13 Marble 2.62.8 1290 2.8 Benzole, pure 0.83 15 210380 0.15 Brass 8.5 900 116 Glycerine 1.26 20 290 0.29 Molybdenum Mo 10.2 2600 145 Resin oil 0.96 20 150380 0.15 Monel metal 8.8 ≈1300 19.7 Sodium Na 0.98 97.5 126 Linseed oil 0.93 20 316 0.17 Nickel silver 8.7 1020 48 Machinery oil 0.91 15 380400 0.125 Nickel Ni 8.9 1452 59 Methanol 0.8 15 65 0.21 Mineral oil 0.99 22.5 2500 -						Substance (liquid)	Sym-	at		λ	
Magnesium, alloyed 1.81.83 650 69.8145.4 Ether 0.72 20 35 0.14 Manganese Mn 7.43 1250 30 Benzine ~0.73 15 25210 0.13 Red lead oxide 8.69.1 - 0.7 Diesel oil 0.83 15 210380 0.15 Brass 8.5 900 116 Glycerine 1.26 20 290 0.29 Molybdenum Mo 10.2 2600 145 Resin oil 0.96 20 150300 0.15 Monel metal 8.8 *1300 19.7 Resin oil 0.96 20 150300 0.15 Sodium Na 0.98 97.5 126 Linseed oil 0.93 20 316 0.17 Nickel silver Ni 8.9 1452 59 Methyl chloride 0.93 15 380400 0.125 Nickel silver Ni 8.6 2415 54.43 </td <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>DUI</td> <td></td> <td></td> <td></td>							DUI				
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Marble 2.62.8 1290 2.8 Red lead oxide 8.6		1			69.8145.4	Ether	1				
Red lead oxide 8.69.1 - 0.7 Diesel oil 0.83 15 210380 0.15 Brass 8.5 900 116 Glycerine 1.26 20 290 0.29 Molybdenum Mo 10.2 2800 145 Resin oil 0.96 20 150300 0.15 Monel metal 8.8 ~1300 19.7 Fuel oil EL ~0.83 20 >175 0.14 Sodium Na 0.98 97.5 126 Linseed oil 0.93 20 316 0.17 Nickel silver 8.7 1020 48 Machinery oil 0.91 15 380400 0.125 Nickel Ni 8.9 1452 59 Methyl chloride 0.93 15 380400 0.125 Nickel Ni 8.6 2415 54.43 Methyl chloride 0.95 15 24 0.16 Osmium Os 22.5 2500 - Mineral		Mn									
Brass 8.5 900 116 Glycerine 1.26 20 290 0.29 Molybdenum Mo 10.2 2600 145 Resin oil 0.96 20 150300 0.15 Monel metal 8.8 *1300 19.7 Fuel oil EL *0.83 20 >175 0.14 Sodium Na 0.98 97.5 126 Linseed oil 0.93 20 316 0.17 Nickel silver 8.7 1020 48 Machinery oil 0.91 15 380400 0.125 Nickel Nickel Ni 8.9 1452 59 Methyl chloride 0.91 15 380400 0.125 Nickel Silver Nb 8.6 2415 54.43 Methyl chloride 0.95 15 24 0.16 Osmium Os 22.5 2500 - Mineral oil 0.91 20 >360 0.13 Paraffin 0.9 52 0.26 Petrole				1290							
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Monel metal		1									
Sodium Na 0.98 97.5 126 Linseed oil 0.93 20 316 0.17 Nickel silver 8.7 1020 48 Machinery oil 0.91 15 380400 0.125 Nickel Ni 8.9 1452 59 Methanol 0.8 15 65 0.21 Niobium Nb 8.6 2415 54.43 Methyl chloride 0.95 15 24 0.16 Osmium Os 22.5 2500 - Methyl chloride 0.95 15 24 0.16 Paraffin 0.9 52 0.26 Petroleum ether 0.66 20 >40 0.14 Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47		Мо									
Nickel silver 8.7 1020 48 Machinery oil 0.91 15 380400 0.125 Nickel Ni 8.9 1452 59 Methanol 0.8 15 65 0.21 Nickel Ni 8.9 1452 59 Methanol 0.8 15 65 0.21 Methanol 0.9 15 24 0.16 0.9 15 24 0.16 Osmium Os 22.5 2500 - Mineral oil 0.91 20 >360 0.13 Paraffin 0.9 52 0.26 Petroleum ether 0.66 20 >40 0.14 Pitch 1.25 - 0.13 Mercury Hg 13.55 20 357 10 Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong <		L									
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Niobium		L									
Osmium Os 22.5 2500 - Mineral oil 0.91 20 > 360 0.13 Palladium Pd 12 1552 70.9 Petroleum ether 0.66 20 > 40 0.14 Paraffin 0.9 52 0.26 Petroleum ether 0.81 20 > 150 0.13 Pitch 1.25 - 0.13 Mercury Hg 13.55 20 357 10 Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47							Ш.				
Palladium Pd 12 1552 70.9 Petroleum ether 0.66 20 >40 0.14 Paraffin 0.9 52 0.26 Petroleum 0.81 20 >150 0.13 Pitch 1.25 - 0.13 Mercury Hg 13.55 20 357 10 Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47					54.43						
Paraffin 0.9 52 0.26 Petroleum 0.81 20 > 150 0.13 Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47					_						
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Phosphorus (white) P 1.83 44 - Hydrochloric acid 10% 1.05 15 102 0.5 Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47				52			L.,				
Platinum Pt 21.5 1770 70 Sulphuric acid, strong 1.84 15 338 0.47		<u> </u>			0.13		Hg				
					- 70						
rolyamilde A, b 1.13 ≈250 0.34 Silicon fiuld 0.94 20 - 0.22		۲t							338		
	Polyamide A, B	<u> </u>	1.13	≈250	0.34	Silicon fluid	<u> </u>	0.94 20		0.22	

Materials

Coefficient of Linear Expansion;

Iron-Carbon Diagram;

Fatigue Strength Values for Gear Materials

Coefficient of linear expansion $\,\alpha\,$

The coefficient of linear expansion α gives the fractional expansion of the unit of length of a substance per 1 degree K rise in temperature. For the linear expansion of a body applies:

$$\Delta I = I_0 \cdot \alpha \cdot \Delta T$$

where

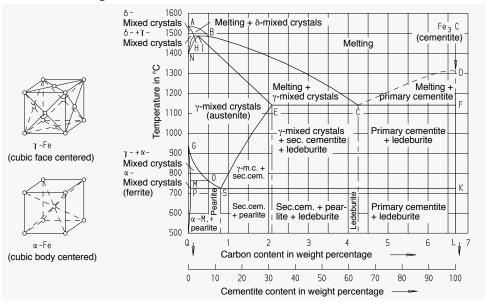
 ΔI : change of length I_0 : original length

α: coefficient of linear expansion

 ΔT : rise of temperature

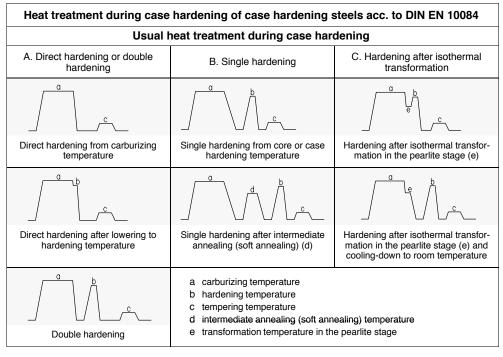
Coefficients of linear expansion of some substances at 0 100 °C							
Substance	lpha [10 ⁻⁶ /K]						
Aluminium alloys	21 24						
Grey cast iron (e.g. GG-20, GG-25) Steel, plain and	10.5						
low-alloy	11.5						
Steel, stainless (18CrNi8)	16						
Steel, rapid machining steel	11.5						
Copper	17						
Brass CuZn37	18.5						
Bronze CuSn8	17.5						

Iron-carbon diagram



Pitting and tooth root fatigue strength of steels											
Grade of steel	Material symbol	Hardness on finished gear HV1	^σ Hlim N/mm²	σ _{Flim} N/mm²							
Case hardening steels, case-hardened	16MnCr5	720	1470	430							
	20MnCr5	680	1470	430							
	18CrNiMo7-6	740	1500	500							
Quenched and tempered steels, quenched and tempered	30CrNiMo8	290	730	300							
	34CrNiMo6	310	770	310							
	42CrMo4	280	740	305							
Quenched and tempered steels, nitrided	34CrNiMo6	630	1000	370							
	42CrMo4	600	1000	370							

Heat Treatment During Case Hardening of Case Hardening Steels



Usual case hardening temperatures											
Material		а	ı	b		С					
Symbol	Number	Carburizing temperature 1) °C	Core hardening temperature 2) °C Case hardening temperature 2) °C		temperature ²⁾ temperature ²⁾		Quenchant	Tempering °C			
C10 C10E C15	1.0301 1.1121 1.0401		880 up to 920		With regard to the properties of						
15Cr3 17Cr3 16MnCr5 16MnCr55 20MnCr5 20MnCr55 20MoCr4 20MoCrS4 20NiCrMo2-2 20NiCrMoS2-2	1,7015 1,7016 1,7131 1,7139 1,7147 1,7149 1,7321 1,7323 1,6523 1,6526	880 up to 980	860 up to 900	780 up to 820	the component, the selection of the quenchant depends on the hardenability or case-hardenability of the steel, the shape and cross section of the work piece to be hardened, as well as on the effect of the	150 up to 200					
15CrNi6 18CrNiMo7-6	1.5919 1.6587		830 up to 870		quenchant.						

- 1) Decisive criteria for the determination of the carburizing temperature are mainly the required time of carburizing, the chosen carburizing agent, and the plant available, the provided course of process, as well as the required structural constitution. For direct hardening, carburizing usually is carried out at temperatures below 950 °C. In special cases, carburizing temperatures up to above 1000 °C are applied.
- 2) In case of direct hardening, quenching is carried out either from the carburizing temperature or any lower temperature. In particular if there is a risk of warping, lower hardening temperatures are preferred.

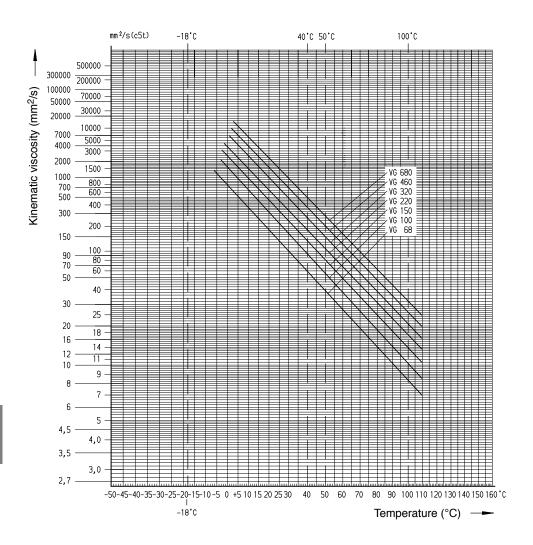
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Viscosity-Temperature-Diagram for Synthetic Oils of Poly- $lpha$ -Olefine Base	81
Viscosity-Temperature-Diagram for Synthetic Oils of Polyglycole Base	82
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Mineral Oils

9

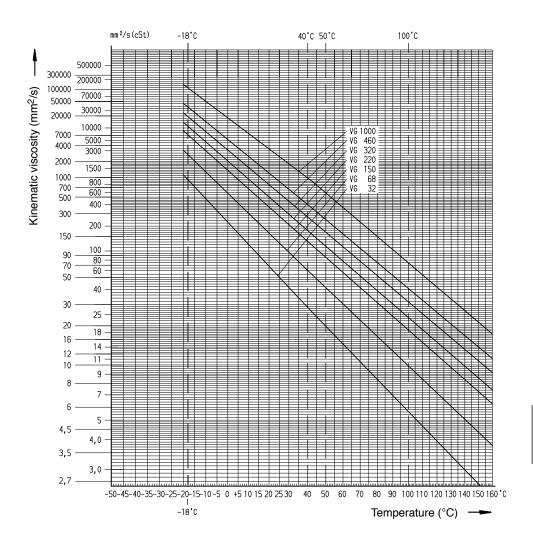
Viscosity-temperature-diagram for mineral oils



Lubricating Oils

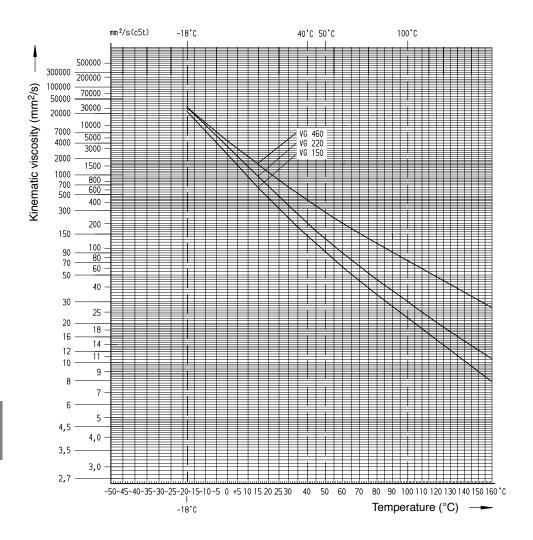
Viscosity-Temperature-Diagram for Synthetic Oils of Poly- α -Olefine Base

Viscosity-temperature-diagram for synthetic oils of poly- α -olefine base



9

Viscosity-temperature-diagram for synthetic oils of polyglycole base



Lubricating Oils

1) T = t + 273.15 [K]

Kinematic Viscosity and Dynamic Viscosity for Mineral Oils at any Temperature

	Kinematic viscosity υ	
Quantities	for the determination of the kinem	natic viscosity
VG grade	W ₄₀ [–]	m [–]
32 46 68	0.18066 0.22278 0.26424	3.7664 3.7231 3.6214
100 150 220	0.30178 0.33813 0.36990	3.5562 3.4610 3.4020
320 460 680	0.39900 0.42540 0.45225	3.3201 3.3151 3.2958
1000 1500	0.47717 0.50192	3.2143 3.1775
,	$V = m (2.49575 - IgT) + W_{40}$	(1)
	$v = 10^{10^{W}} - 0.8$	(2)
	m [-]: slope Γ [K]: thermodynamic tempe N ₄₀ [-]: auxiliary quantity at 40 N [-]: auxiliary quantity D [CSt]: kinematic viscosity	

Dynamic viscosity η

(3) $\eta = \upsilon \cdot \varrho \cdot 0.001$

> $\varrho = \varrho_{15} - (t - 15) \cdot 0.0007$ (4) temperature

Q₁₅ [kg/dm³]: density at 15 °C ο [kg/dm³]: density

t [°C]:

υ [cSt]: kinematic viscosity η [Ns/m²]: dynamic viscosity

Density ϱ_{15} in kg/dm ³ of lubricating oils for gear units $^{2)}$ (Example)												
VG grade	68	100	150	220	320	460	680					
ARAL Degol BG Plus	-	0.888	0.892	0.897	0.895	0.902	0.905					
MOBIL Mobilgear 600 XP	0.880	0.880	0.890	0.890	0.900	0.900	0.910					
MOBIL Mobilgear XMP	-	0.890	0.896	0.900	0.903	0.909	0.917					
CASTROL Optigear BM	0.890	0.893	0.897	0.905	0.915	0.920	0.930					
CASTROL Tribol 1100	0.888	0.892	0.897	0.904	0.908	0.916	0.923					

2) Mineral base gear oils in accordance with designation CLP as per DIN 51517 Part 3. These oils comply with the minimum requirements as specified in DIN 51517 Part 3. They are suitable for operating temperatures from -10 °C up to +90 °C (briefly +100 °C).

ISO-VG	Approx.	Mean vis	viscosit cosities	y (40 °0 s in mm	C) and a ² /s (cSt)	Saybolt universal seconds	AGMA lubricant	Approx. assignment to motor-		
DIN 51519	ment to previous DIN 51502	20 °C	40 °C	40 °C 50 °C 100 °C		(SSU) at 40°C (mean value)	N° at 40 °C 1)	motor oils	car gear oils	
		cSt	cSt	cSt	Engler	cSt	1)		SAE	SAE
5	2	8 (1.7 E)	4.6	4	1.3	1.5				
7	4	12 (2 E)	6.8	5	1.4	2.0				
10	9	21 (3 E)	10	8	1.7	2.5				
15	_	34	15	11	1.9	3.5			5 W	
22	16	55	22	15	2.3	4.5			10 W	70 W
32	25	88	32	21	3	5.5			10 00	75 W
46		137	46	30	4	6.5	214	1 EP	15 W	
68	36	219	68	43	6	8.5	316	2.2 EP	20 W 20	80 W
400	49	0.45	400	0.4			404	0.0.55		
100	68	345	100	61	8	11	464	3.3 EP	30	85 W
150	92	550	150	90	12	15	696	4.4 EP	40	
220	114	865	220	125	16	19	1020	5.5 EP	50	90
	144									
320	169	1340	320	180	24	24	1484	6.6 EP		
460	225	2060	460	250	33	30	2132	7 EP		140
680	324	3270	680	360	47	40	3152	8 EP		
1000		5170	1000	510	67	50				
1500		8400	1500	740	98	65				250
1) Appr	oximate com	nparative	value t	o ISO '	VG grad	es				

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а	mm	Centre distance	n	min ⁻¹	Speed
a _d	mm	Reference centre distance	р	N/mm ²	Pressure; compression
b	mm	Facewidth	р	mm	Pitch on the reference circle
	mm	Bottom clearance between	p _{bt}	mm	Pitch on the base circle
c _p	mm	standard basic rack tooth profile and counter profile	p _e	mm	Normal base pitch
d	mm	Reference diameter	p _{en}	mm	Normal base pitch at a point
da	mm	Tip diameter	p _{et}	mm	Normal transverse pitch
d _b	mm	Base diameter	p _{ex}	mm	Axial pitch
d _f	mm	Root diameter	pt	mm	Transverse base pitch; reference circle pitch
d _w	mm	Pitch diameter			Protuberance value on the
е	mm	Spacewidth on the reference cylinder	pr _{P0}	mm	tool's standard basic rack tooth profile
e _p	mm	Spacewidth on the standard basic rack tooth profile	q	mm	Machining allowance on the cylindrical gear tooth flanks
f	Hz	Frequency	r	mm	Reference circle radius; radius
g_{α}	mm	Length of path of contact	ra	mm	Tip radius
h	mm	Tooth depth	r _b	mm	Base radius
ha	mm	Addendum	10		Radius of the working pitch
h _{aP}	mm	Addendum of the standard basic rack tooth profile	r _w	mm	circle
h _{aP0}	mm	Addendum of the tool's standard basic rack tooth profile	S	mm	Tooth thickness on the reference circle
h _f	mm	Dedendum	s _{an}	mm	Tooth thickness on the tip circle
h _{fP}	mm	Dedendum of the standard basic rack tooth profile	sp	mm	Tooth thickness of the standard basic rack tooth profile
h _{fP0}	mm	Dedendum of the tool's standard basic rack tooth profile	s _{P0}	mm	Tooth thickness of the tool's standard basic rack tooth
hp	mm	Tooth depth of the standard			profile
		basic rack tooth profile Tooth depth of the tool's stand-	u	-	Gear ratio
h _{P0}	mm	ard basic rack tooth profile	V	m/s	Circumferential speed on the reference circle
h _{prP0}	mm	Protuberance height of the tool's standard basic rack	W	N/mm	Line load
··btь0		tooth profile Working depth of the standard	х	_	Addendum modification coefficient
h _{wP}	mm	basic rack tooth profile and the counter profile	ΧE	-	Generating addendum modification coefficient
k	-	Addendum modification factor	z	_	Number of teeth
m	mm	Module	Α	m ²	Gear teeth surface
m _n	mm	Normal module	A _s	mm	Tooth thickness deviation
		Transverse module		N/mm ²	Load value
m _t	mm	Hallsverse module	B_L	14/111111	Loau value

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D	mm	Construction dimension
Fn	N	Load
Ft	N	Nominal peripheral force at the reference circle
G	N	Weight
HV1	-	Vickers hardness at F = 9.81 N
K _A	_	Application factor
K _{Fα}	-	Transverse load factor (for tooth root stress)
K _{Fβ}	-	Face load factor (for tooth root stress)
K _{Hα}	-	Transverse load factor (for contact stress)
Кнβ	-	Face load factor (for contact stress)
K _v	_	Dynamic factor
L _{pA}	dB	Sound pressure level, A-weighted
L _{WA}	dB	Sound power level, A-weighted
Р	kW	Nominal power rating of driven machine
R _Z	μ m	Mean peak-to-valley height
S _F	-	Factor of safety from tooth breakage
S _H	_	Factor of safety from pitting
S	m ²	Enveloping surface
Т	Nm	Torque
Y_{β}	_	Helix angle factor
Y_{ϵ}	1	Contact ratio factor
Y _{FS}	_	Tip factor
Y _R	_	Roughness factor
Y _X	_	Size factor
Z_{β}	_	Helix angle factor
Z_{ϵ}	_	Contact ratio factor
Z _H	_	Zone factor
Z _L	_	Lubricant factor
Z _v	_	Speed factor

Z _X	-	Size factor
α	Degree	Transverse pressure angle at a point; pressure angle
$\widehat{\alpha}$	rad	Angle α in the circular measure $(\widehat{\alpha} = \alpha \cdot \pi / 180)$
α_{at}	Degree	Transverse pressure angle at the tip circle
α_{n}	Degree	Normal pressure angle
αР	Degree	Pressure angle at a point of the standard basic rack tooth profile
αρ0	Degree	Pressure angle at a point of the tool's standard basic rack tooth profile
α_{prP0}	Degree	Protuberance pressure angle at a point
α_{t}	Degree	Transverse pressure angle at the reference circle
α_{wt}	Degree	Working transverse pressure angle at the pitch circle
β	Degree	Helix angle at the reference circle
βb	Degree	Base helix angle
ϵ_{α}	_	Transverse contact ratio
ϵ_{β}	_	Overlap ratio
ϵ_{γ}	_	Total contact ratio
ζ	Degree	Working angle of the involute
η	_	Efficiency
б	mm	Radius of curvature
QaP0	mm	Tip radius of curvature of the tool's standard basic rack tooth profile
QfP0	mm	Root radius of curvature of the tool's standard basic rack tooth profile
σ_{H}	N/mm ²	Effective Hertzian pressure
$\sigma_{ ext{Hlim}}$	N/mm ²	Allowable stress number for contact stress
σ_{HP}	N/mm ²	Allowable Hertzian pressure
σ_{F}	N/mm ²	Effective tooth root stress
σ _{Flim}	N/mm ²	Bending stress number
σ _{FP}	N/mm ²	Allowable tooth root stress
υ ₄₀	mm ² /s	Lubricating oil viscosity at 40 °C

Note: The unit rad (= radian) may be replaced by 1.

1. Cylindrical gear units

1.1 Introduction

In the industry, mainly gear units with case hardened and fine-machined gears are used for torque and speed adaptation of prime movers and driven machines. After carburising and hardening, the tooth flanks are fine-machined by grinding (or removing material by means of shaping or generating tools coated with mechanically resistant material). In comparison with other gear units, which, for example, have quenched and tempered or nitrided gears, gear units with case hardened gears have higher power capacities, i.e. they require less space for the same speeds and torques. Further, gear units have the best efficiencies. Motion is transmitted without slip at constant speed. As a rule, an infinitely variable change-speed gear unit with primary or secondary gear stages presents the most economical solution even in case of variable speed control.

In industrial gear units mainly involute gears are used. Compared with other tooth profiles, the technical and economical advantages are basically:

- Simple manufacture with straight-sided flanked tools;
- The same tool for all numbers of teeth;
- Generating different tooth profiles and centre distances with the same number of teeth by means of the same tool by addendum modification;
- Uniform transmission of motion even in case of centre distance errors from the nominal value:
- The direction of the normal force of teeth remains constant during meshing;
- Advanced stage of development;
- Good availability on the market.

When load sharing gear units are used, output torques can be doubled or tripled in comparison

with gear units without load sharing. Load sharing gear units mostly have one input and one output shaft. Inside the gear unit the load is distributed and then brought together again on the output shaft gear. The uniform sharing of the load between the individual branches is achieved by special design measures.

1.2 Geometry of involute gears

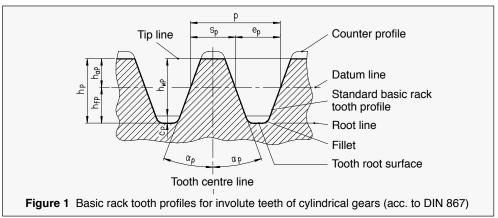
The most important concepts and parameters associated with cylindrical gears and cylindrical gear pairs with involute teeth in accordance with DIN 3960 are represented in sections 1.2.1 to 1.2.4. /1/

1.2.1 Concepts and parameters associated with involute teeth

1.2.1.1 Standard basic rack tooth profile

The standard basic rack tooth profile is the normal section through the teeth of the basic rack which is produced from an external gear tooth system with an infinitely large diameter and an infinitely large number of teeth. From figure 1 follows:

- The flanks of the standard basic rack tooth profile are straight lines and are located symmetrically below the pressure angle at a point α_P to the tooth centre line;
- Between module m and pitch p the relation is p = πm;
- The nominal dimensions of tooth thickness and spacewidth on the datum line are equal, i.e. sp = ep = p/2;
- The bottom clearance c_P between basic rack tooth profile and counter profile is 0.1 m up to 0.4 m;
- The addendum is fixed by h_{aP} = m, the dedendum by h_{fP} = m + c_P and thus, the tooth depth by h_P = 2 m + c_P;
- The working depth of basic rack tooth profile and counter profile is h_{wP} = 2 m.



1.2.1.2 Module

The module m of the standard basic rack tooth profile is the module in the normal section m_{n} of the gear teeth. For a helical gear with helix angle β on the reference circle, the transverse

module in a transverse section is $m_t = m_n/\cos\beta$. For a spur gear $\beta = 0$ and the module is $m = m_n = m_t$. In order to limit the number of the required gear cutting tools, module m has been standardized in preferred series 1 and 2, see table 1.

Table 1 Selection of some modules m in mm (acc. to DIN 780)																
Series 1	1	1.25	1.5	2	2.5	3	4	5	6	8	10	12	16	20	25	32
Series 2	1.75		3.5 4.5			7 9			14	4 1	8 2	2 2	28			

1.2.1.3 Tool reference profile

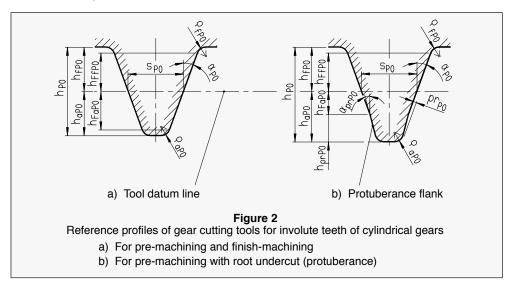
The tool reference profile according to figure 2a is the counter profile of the standard basic rack tooth profile according to figure 1. For industrial gear units, the pressure angle at a point of the tool reference profile $\alpha_{P0}=\alpha_P$ is 20° , as a rule. The tooth thickness s_{P0} of the tool on the tool datum line depends on the stage of machining. The pre-machining tool leaves on both flanks of the teeth a machining allowance q for finish-machining. Therefore, the tooth thickness for pre-machining tools is $s_{P0} < p/2$, and for finish-machining tools $s_{P0} = p/2$.

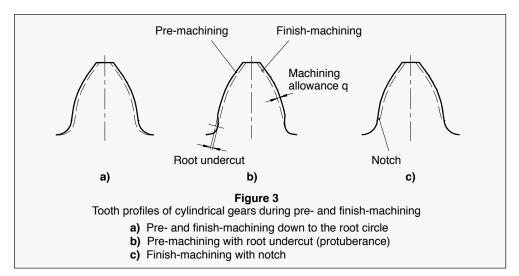
The pre-machining tool generates the root diameter and the fillet on a cylindrical gear. The finish-machining tool removes the machining allowance on the flanks, however, normally it does not touch the root circle – like on the tooth profile in figure 3a.

Between pre- and finish-machining, cylindrical gears are subjected to a heat treatment which, as a rule, leads to warping of the teeth and growing of the root and tip circles.

Especially for cylindrical gears with a relatively large number of teeth or a small module there is a risk of generating a notch in the root on finish-machining. To avoid this, pre-machining tools are provided with protuberance flanks as shown in figure 2b. They generate a root undercut on the gear, see figure 3b. On the tool, protuberance value pr_{P0} , protuberance pressure angle at a point α_{prP0} , as well as the tip radius of curvature ϱ_{aP0} must be so dimensioned that the active tooth profile on the gear will not be reduced and the tooth root will not be weakened too much.

On cylindrical gears with small modules one often accepts on purpose a notch in the root if its distance to the root circle is large enough and thus the tooth root load carrying capacity is not impaired by a notch effect, figure 3c. In order to prevent the tip circle of the mating gear from touching the fillet it is necessary that a check for meshing interferences is carried out on the gear pair. /1/





1.2.1.4 Generating tooth flanks

With the development of the envelope, an envelope line of the base cylinder with the base diameter d_b generates the involute surface of a spur gear.

Å straight line inclined by a base helix angle β_b to the envelope line in the developed envelope is the generator of an involute surface (involute helicoid) of a helical gear, figure 4.

The involute which is always lying in a transverse section, figure 5, is described by the transverse

Base cylinder envelope line Involute of base cylinder Base cylinder Involute helicoid Developed envelope line Generator Developed Involute of base base cylinder cylinder envelope Figure 4 Base cylinder with involute helicoid and generator

pressure angle at a point $\boldsymbol{\alpha}$ and radius \boldsymbol{r} in the equations

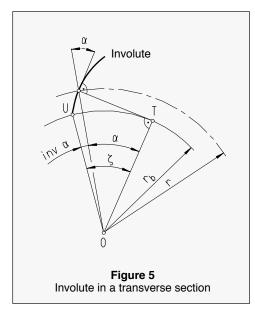
$$inv\alpha = tan\alpha - \widehat{\alpha}$$
 (1)

$$r = r_b / \cos\alpha \tag{2}$$

 $r_b = d_b/2$ is the base radius. The angle inv α is termed involute function, and the angle

$$\zeta = \widehat{\alpha} + \text{inv}\alpha = \tan \alpha$$

 $\tan \alpha$ is termed working angle.



Geometry of Involute Gears

1.2.2 Concepts and parameters associated with cylindrical gears

1.2.2.1 Geometric definitions

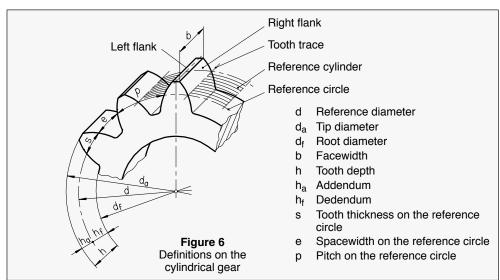
In figure 6 the most important geometric quantities of a cylindrical gear are shown.

The reference circle is the intersection of the reference cylinder with a plane of transverse section. When generating tooth flanks, the straight pitch line of the tool rolls off at the reference circle. Therefore, the reference circle periphery corresponds to the product of pitch p and number of teeth z, i.e. $\pi \cdot d = p \cdot z$. Since $m_t = p/\pi$, the equation for the reference diameter thus is $d = m_t \cdot z$. Many geometric quantities of the cylindrical gear are referred to the reference circle.

For a helical gear, at the point of intersection of the involute with the reference circle, the transverse pressure angle at a point α in the transverse section is termed transverse pressure angle α_t , see figures 5 and 7. If a tangent line is put against the involute surface in the normal section at the point of intersection with the reference circle, the corresponding angle is termed normal pressure angle α_n ; this is equal to the pressure angle α_{P0} of the tool. The interrelationship with the helix angle β at the reference circle is $\tan \alpha_n = \cos \beta \cdot \tan \alpha_t$. On a spur gear $\alpha_n = \alpha_t$.

Between the base helix angle β_b and the helix angle β on the reference circle the relationship is $\sin\!\beta_b = \cos\!\alpha_n \cdot \sin\!\beta$. The base diameter d_b is given by the reference diameter d, by d_b = d $\cdot \cos\!\alpha_t$.

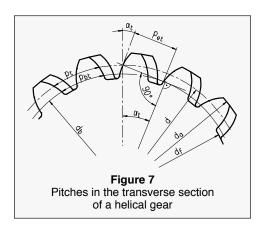
In the case of internal gears, the number of teeth z and thus also the diameters d, d_b, d_a, d_f are negative values.



1.2.2.2 Pitches

The pitch p_t of a helical gear (p in the case of a spur gear) lying in a transverse section is the length of the reference circle arc between two successive right or left flanks, see figures 6 and 7. With the number of teeth z results $p_t = \pi \cdot d/z = \pi \cdot m_t$.

The normal transverse pitch p_{et} of a helical gear is equal to the pitch on the basic circle p_{bt} , thus $p_{et} = p_{bt} = \pi \cdot d_b/z$. Hence, in the normal section the normal base pitch at a point $p_{en} = p_{et}/\cos\beta_b$ is resulting from it, and in the axial section the axial pitch $p_{ex} = p_{et}/\tan\beta_b$, see figure 13.



1.2.2.3 Addendum modification

When generating tooth flanks on a cylindrical gear by means of a tooth-rack-like tool (e.g. a hob), a straight pitch line parallel to the datum line of tool rolls off on the reference circle. The distance $(x \cdot m_n)$ between the straight pitch line and the datum line of tool is the addendum modification, and x is the addendum modification, see figure 8.

An addendum modification is positive, if the datum line of tool is displaced from the reference circle towards the tip, and it is negative if the datum line is displaced towards the root of the gear. This is true for both external and internal gears. In the case of internal gears the tip points to the inside. An addendum modification for external gears should be carried through approximately within the limits as shown in figure 9.

The addendum modification limits x_{min} and x_{max} are represented dependent on the virtual number of teeth $z_n = z / (\cos \beta \cdot \cos^2 \beta_b)$. The upper limit x_{max} takes into account the intersection circle of the teeth and applies to a normal crest width in the normal section of $s_{an} = 0.25 \ m_h$. When falling below the lower limit x_{min} this results in an undercut which shortens the usable involute and weakens the tooth root.

A positive addendum modification results in a greater tooth root width and thus in an increase in the tooth root carrying capacity. In the case of small numbers of teeth this has a considerably stronger effect than in the case of larger ones. One mostly strives for a greater addendum modification on pinions than on gears in order to achieve equal tooth root carrying capacities for both gears, see figure 19.

Further criteria for the determination of addendum modification are contained in /2I, /3I, and /4I. The addendum modification coefficient x refers to gear teeth free of backlash and deviations. In order to take into account tooth thickness deviation $A_{\rm S}$ (for backlash and manufacturing tolerances) and machining allowances q (for premachining), one has to give the following generating addendum modification coefficient for the manufacture of a cylindrical gear:

$$X_E = x + \frac{A_s}{2m_n \cdot \tan \alpha_n} + \frac{q}{m_n \cdot \sin \alpha_n}$$
 (3)

Datum line of tool = straight pitch line

Straight pitch line

b)

Datum line of tool Straight pitch line

c)

Figure 8

Different positions of the datum line of tool in relation to the straight pitch line through pitch point C.

- a) Zero addendum modification; x = 0
- **b)** Negative addendum modification; x < 0
- c) Positive addendum modification; x > 0

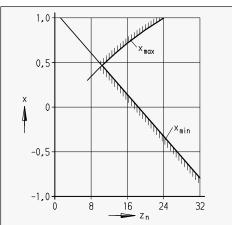


Figure 9

Addendum modification limit x_{max} (intersection circle) and x_{min} (undercut limit) for external gears dependent on the virtual number of teeth z_n (for internal gears, see /1/ and /3/).

Geometry of Involute Gears

1.2.3 Concepts and parameters associated with a cylindrical gear pair

1.2.3.1 Terms

The mating of two external cylindrical gears (external gears) gives an external gear pair. In the case of a helical external gear pair one gear has left-handed and the other one right-handed flank direction.

The mating of an external cylindrical gear with an internal cylindrical gear (internal gear) gives an internal gear pair. In the case of a helical internal gear pair, both gears have the same flank direction, that is either right-handed or left-handed. The subscript 1 is used for the size of the smaller gear (pinion), and the subscript 2 for the larger gear (wheel or internal gear).

In the case of an unmodified gear pair (a zero gear pair), both gears have as addendum modification coefficient $x_1 = x_2 = 0$ (zero gears).

In the case of a gear pair at reference centre distance, both gears have addendum modifications (modified gears), that is with $x_1 + x_2 = 0$, i.e. $x_1 = -x_2$.

For a modified gear pair, the sum is not equal to zero, i.e. $x_1 + x_2 \ne 0$. One of the cylindrical gears in this case may, however, have an addendum modification x = 0.

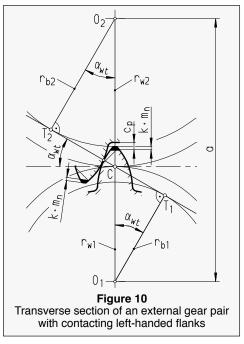
1.2.3.2 Mating quantities

The gear ratio of a gear pair is the ratio of the number of teeth of the gear z_2 to the number of teeth of the pinion z_1 , thus $u=z_2/z_1$. Working pitch circles with diameter $d_w=2\cdot r_w$ are those transverse intersection circles of a cylindrical gear pair, which have the same circumferential speed at their mutual contact point (pitch point C), figure 10. The working pitch circles divide the centre distance $a=r_{w1}+r_{w2}$ in the ratio of the tooth numbers, thus $d_{w1}=2\cdot a/(u+1)$ and $d_{w2}=2\cdot a\cdot u/(u+1)$.

In the case of both an unmodified gear pair and a gear pair at reference centre distance, the centre distance is equal to the zero centre distance $a_d=\left(d_1+d_2\right)/2$, and the pitch circles are simultaneously the reference circles, i.e. $d_w=d$. However, in the case of a modified gear pair, the centre distance is not equal to the zero centre distance, and the pitch circles are not simultaneously the reference circles.

If in the case of modified gear pairs the bottom clearance c_p corresponding to the standard basic rack tooth profile is to be retained (which is not absolutely necessary), then an addendum modification is to be carried out. The addendum modification factor is $k = (a - a_d) / m_n - (x_1 + x_2)$. For unmodified gear pairs and gear pairs at reference centre distance, k = 0. In the case of external gear pairs k < 0, i.e. the tip diameters of both gears become smaller. In the case of

internal gear pairs k > 0, i.e. the tip diameters of both gears become larger (on an internal gear with negative tip diameter the absolute value becomes smaller).

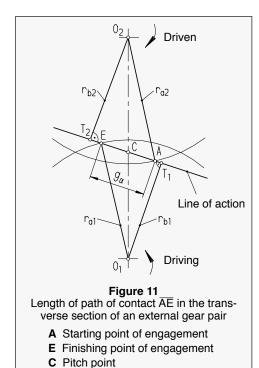


In a cylindrical gear pair either the left or the right flanks of the teeth contact each other on the line of action. Changing the flanks results in a line of action each lying symmetrical in relation to the centre line through O_1 O_2 . The line of action with contacting left flanks in figure 10 is the tangent to the two base circles at points T_1 and T_2 . With the common tangent on the pitch circles it includes the working pressure angle α_{wf} .

The working pressure angle α_{wt} is the transverse pressure angle at a point belonging to the working pitch circle. According to figure 10 it is determined by $\cos \alpha_{wt} = d_{b1} / d_{w1} = d_{b2} / d_{w2}$. In the case of unmodified gear pairs and gear pairs at reference centre distance, the working pressure angle is equal to the transverse pressure angle on the reference circle, i.e. $\alpha_{wt} = \alpha_t$.

The length of path of contact g_{α} is that part of the line of action which is limited by the two tip circles of the cylindrical gears, figure 11.

The starting point A of the length of path of contact is the point at which the line of action intersects the tip circle of the driven gear, and the finishing point E is the point at which the line of action intersects the tip circle of the driving gear.

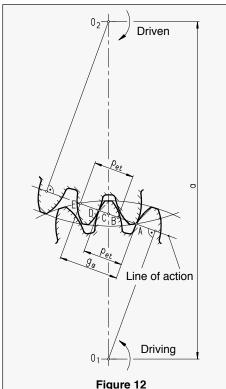


1.2.3.3 Contact ratios

The transverse contact ratio ε_{α} in the transverse section is the ratio of the length of path of contact g_{α} to the normal transverse pitch p_{et} , i.e. $\varepsilon_{\alpha} = g_{\alpha} / p_{et}$, see figure 12.

In the case of spur gear pairs, the transverse contact ratio gives the average number of pairs of teeth meshing during the time of contact of a tooth pair. According to figure 12, the left-hand tooth pair is in the individual point of contact D while the right-hand tooth pair gets into mesh at the starting point of engagement A. The righthand tooth pair is in the individual point of contact B when the left-hand tooth pair leaves the mesh at the finishing point of engagement E. Along the individual length of path of contact BD one tooth pair is in mesh, and along the double lengths of paths of contact AB and DE two pairs of teeth are simultaneously in mesh. In the case of helical gear pairs it is possible to achieve that always two or more pairs of teeth are in mesh simultaneously. The overlap ratio ε_{β} gives the contact ratio, owing to the helix of the teeth, as the ratio of the facewidth b to the axial pitch p_{ex} , i.e. $\varepsilon_{\beta} = b/p_{ex}$, see figure 13.

The total contact ratio ϵ_γ is the sum of transverse contact ratio and overlap ratio, i.e. $\epsilon_\gamma = \epsilon_\alpha + \epsilon_\beta$. With an increasing total contact ratio, the load carrying capacity increases, as a rule, while the generation of noise is reduced.



Single and double contact region in the transverse section of an external gear pair

- B, D Individual points of contact
- A, E Starting and finishing point of engagement, respectively
- C Pitch point

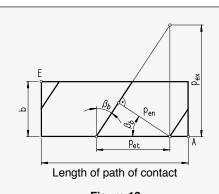


Figure 13
Pitches in the plane of action

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A Starting point of engagementE Finishing point of engagement

Cylindrical Gear Units

Geometry of Involute Gears

1.2.4 Summary of the most important formulae

Tables 2 and 3 contain the most important formulae for the determination of sizes of a cylindrical gear and a cylindrical gear pair, and this for both external and internal gear pairs.

The following rules for signs are to be observed: In the case of internal gear pairs the number of teeth z_2 of the internal gear is a negative quantity. Thus, also the centre distance a or a_d and the gear ratio u as well as the diameters d_2 , d_{a2} , d_{b2} , d_{f2} , d_{w2} and the virtual number of teeth z_{n2} are negative.

When designing a cylindrical gear pair for a gear stage, from the output quantities of tables 2 and 3 only the normal pressure angle α_n and the gear ratio u are given, as a rule. The number of teeth of

the pinion is determined with regard to silent running and a balanced foot and flank load carrying capacity, at approx. $z_1=18\dots 23$. If a high foot load carrying capacity is required, the number may be reduced to $z_1=10$. For the helix angle, $\beta=10$ up to 15 degree is given, in exceptional cases also up to 30 degree. The addendum modification limits as shown in figure 9 are to be observed. On the pinion, the addendum modification coefficient should be within the range of $x_1=0.2$ up to 0.6 and from lul > 2 the width within the range $b_1=(0.35 \text{ to } 0.45)$ a. Centre distance a is determined either by the required power to be transmitted or by the constructional conditions.

Geometry of Involute Gears

Output quantities:

m_n mm normal module

 $\begin{array}{lll} \alpha_{\text{n}} & \text{degree} & \text{normal pressure angle} \\ \beta & \text{degree} & \text{reference helix angle} \\ z & - & \text{number of teeth *)} \end{array}$

x – addendum modification coefficient

x_E – generating addendum modification coefficient, see equation (3)

h_{aP0} mm addendum of the tool

Formula		
$m_t = \frac{m_n}{\cos \beta}$		
$tan\alpha_t = \frac{tan\alpha_n}{cos\beta}$		
$\sin \beta_b = \sin \beta \cdot \cos \alpha_n$		
$d = m_t \cdot z$		
$d_a = d + 2 m_n (1 + x + k)$		
$d_f = d - 2 (h_{aP0} - m_n \cdot x_E)$		
$d_b = d \cdot \cos \alpha_t$		
$p_t = \frac{\pi \cdot d}{z} = \pi \cdot m_t$		
$p_{et} = p_{bt} = \frac{\pi \cdot d_b}{z} = p_t \cdot \cos \alpha_t$		
$\cos \alpha_{at} = \frac{d_b}{d_a}$		
$s_t = m_t \left(\frac{\pi}{2} + 2 \cdot x \cdot \tan \alpha_n \right)$		
$s_n = s_t \cdot \cos \beta$		
$s_{at} = d_a \left(\frac{s_t}{d} + inv\alpha_t - inv\alpha_{at} \right)^{**}$		
$z_n = \frac{z}{\cos\beta \cdot \cos^2\beta_b}$		

^{*)} For an internal gear, z is to be used as a negative quantity. **) For inv α , see equation (1).

Output quantities:

The parameters for pinion and wheel according to table 2 must be given, further the facewidths b_1 and b_2 , as well as either the centre distance a or the sum of the addendum modification coefficients $x_1 + x_2$.

Item	Formula			
Gear ratio	$u = \frac{z_2}{z_1}$			
Working transverse pressure angle ("a" given)	$\cos\alpha_{\text{Wt}} = \frac{m_t}{2 \cdot a} (z_1 + z_2) \cos\alpha_t$			
Sum of the addendum modification coefficients	$x_1 + x_2 = \frac{z_1 + z_2}{2 \cdot \tan \alpha_n} (inv\alpha_{wt} - inv\alpha_t)$			
Working transverse pressure angle (x ₁ + x ₂ given)	$inv\alpha_{wt} = 2 \frac{x_1 + x_2}{z_1 + z_2} tan\alpha_n + inv\alpha_t$			
Centre distance	$a = \frac{m_t}{2} (z_1 + z_2) \frac{\cos \alpha_t}{\cos \alpha_{wt}}$			
Reference centre distance	$a_d = \frac{m_t}{2} (z_1 + z_2) = \frac{d_1 + d_2}{2}$			
Addendum modification factor **)	$k = \frac{a - a_d}{m_n} - (x_1 + x_2)$			
Working pitch circle diameter of the pinion	$d_{w1} = \frac{2 \cdot a}{u+1} = d_1 \frac{\cos \alpha_t}{\cos \alpha_{wt}}$			
Working pitch circle diameter of the gear	$d_{w2} = \frac{2 \cdot a \cdot u}{u+1} = d_2 \frac{\cos \alpha_t}{\cos \alpha_{wt}}$			
Length of path of contact	$g_{\alpha} = \frac{1}{2} \left(\sqrt{d_{a1}^2 - d_{b1}^2} + \frac{u}{ u } \sqrt{d_{a2}^2 - d_{b2}^2} \right) - a \cdot \sin \alpha_{wt}$			
Transverse contact ratio	$\varepsilon_{\alpha} = \frac{g_{\alpha}}{p_{\text{et}}}$			
Overlap ratio	$ \varepsilon_{\beta} = \frac{b \cdot \tan \beta_b}{p_{et}} $ $b = min (b_1, b_2)$			
Total contact ratio	$\varepsilon_{\gamma} = \varepsilon_{\alpha} + \varepsilon_{\beta}$			

^{*)} For internal gear pairs, z₂ and a are to be used as negative quantities.

^{**)} See subsection 1.2.3.2.

1.2.5 Gear teeth modifications

The parameters given in the above subsections 1.2.1 to 1.2.4 refer to non-deviating cylindrical gears. Because of the high-tensile gear materials, however, a high load utilization of the gear units is possible. Noticeable deformations of the elastic gear unit components result from it. The deflection at the tooth tips is, as a rule, a multiple of the manufacturing form errors. This leads to meshing interferences at the entering and leaving sides, see figure 14. There is a negative effect on the load carrying capacity and generation of noise.

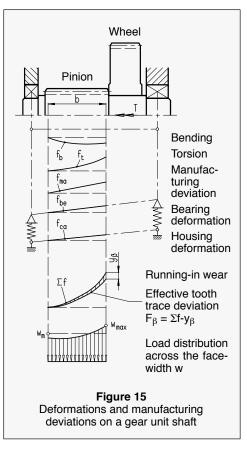
Figure 14
Cylindrical gear pair under load
1 Driven gear
2 Driven gear
a, b Tooth pair being in engagement
c, d Tooth pair getting into engagement

Further, the load causes bending and twisting of pinion and wheel shaft, pinion and wheel body, as well as settling of bearings, and housing deformations. This results in skewing of the tooth flanks which often amounts considerably higher than the tooth trace deviations caused by manufacture, see figure 15. Non-uniform load carrying occurs along the face width which also has a negative effect on the load carrying capacity and generation of noise.

generation of noise. The running-in wear of case hardened gears amounts to a few micrometers only and cannot compensate the mentioned deviations. In order to restore the high load carrying capacity of case hardened gears and reduce the generation of noise, intentional deviations from the involute (profile correction) and from the theoretical tooth trace (longitudinal correction) are produced in order to attain nearly ideal geometries with uniform load distribution under load again. The load-related form corrections are calculated and made for one load only – as a rule for 70 ... 100% of the permanently acting nominal load – /5, 6, 7/. At low partial load, contact patterns

which do not cover the entire tooth depth and

facewidth are achieved. This has to be taken into consideration especially in the case of checks of contact patterns carried out under low loads. Under partial load, however, the local maximum load rise is always lower than the theoretical uniform load distribution under full load. In the case of modified gear teeth, the contact ratio is reduced under partial load because of incomplete carrying portions, making the noise generating levels increase in the lower part load range. With increasing load, the carrying portions and thus the contact ratio increase so that the generating levels drop. Gear pairs which are only slightly loaded do not require any modification.



In figure 16, usual profile and longitudinal corrections are illustrated. In the case of profile correction, the flanks on pinion and wheel are relieved at the tips by an amount equal to the length they are protruding at the entering and leaving sides due to the bending deflection of the teeth. Root relief may be applied instead of tip relief which, however, is much more expensive. Thus, a gradual load increase is achieved on the tooth

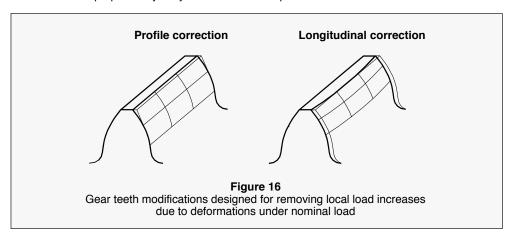
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Cylindrical Gear Units

Geometry of Involute Gears

Load Carrying Capacity of Involute Gears

getting into engagement, and a load reduction on the tooth leaving the engagement. In the case of longitudinal correction, the tooth trace relief often is superposed by a symmetric longitudinal crowning. With it, uniform load carrying along the facewidth and a reduction in load concentration at the tooth ends during axial displacements is attained.



1.3 Load carrying capacity of involute gears

1.3.1 Scope of application and purpose

The calculation of the load carrying capacity of cylindrical gears is generally carried out in accordance with the calculation method according to DIN 3990 /8/ (identical with ISO 6336) which takes into account pitting, tooth root bending stress and scoring as load carrying limits. Because of the relatively large scope of standards, the calculation in accordance with this method may be carried out only by using EDP programs. As a rule, gear unit manufacturers have such a tool at hand. The standard work is the FVA-Stirnradprogramm /9/ which includes further calculation methods, for instance, according to Niemann, AGMA, DNV, LRS, and others.

In DIN 3990, different methods A, B, C ... are suggested for the determination of individual factors, where method A is more exact than method B, etc. The application standard /10/ according to DIN 3990 is based on simplified methods.

Because of its – even though limited – universal validity it still is relatively time-consuming.

The following calculation method for pitting resistance and tooth strength of case-hardened cylindrical gears is a further simplification if compared with the application standard, however, without losing some of its meaning. Certain conditions must be adhered to in order to attain high load carrying capacities which also results in preventing scuffing. Therefore, a calculation of load carrying capacity for scuffing will not be considered in the following.

It has to be expressly emphasized that for the load carrying capacity of gear units the exact calculation method – compared with the simplified one – is always more meaningful and therefore is exclusively decisive in border-line cases.

Design, selection of material, manufacture, heat treatment, and operation of industrial gear units are subject to certain rules which lead to a long service life of the cylindrical gears.

Those rules are:

- Gear teeth geometry acc. to DIN 3960;
- Cylindrical gears out of case-hardened steel;
 Tooth flanks in DIN quality 6 or better, fine machined;
- Quality of material and heat treatment proved by quality inspections acc. to DIN 3990 /11/;
- Effective case depth after carburizing according to instructions /12/ with surface hardnesses of 58 ... 62 HRC;
- Gears with required tooth corrections and without harmful notches in the tooth root;
- Gear unit designed for fatigue strength, i.e. life factors Z_{NT} = Y_{NT} = 1.0;
- − Flank fatigue strength $\sigma_{Hlim} \ge 1200 \text{ N/mm}^2$;
- Subcritical operating range, i.e. pitch circle velocity lower than approx. 35 m/s;
- Sufficient supply of lubricating oil;
- Use of prescribed gear oils of criteria stage 12 acc. to the gear rig test by the FZG-method and sufficient grey staining load capacity;
- Maximum operating temperature 95 °C.

If these requirements are met, a number of factors can be definitely given for the calculation of the load carrying capacity according to DIN 3990, so that the calculation procedure is partly considerably simplified. Non-observance of the above requirements, however, does not necessarily mean that the load carrying capacity is reduced. In case of doubt one should, however, carry out the calculation in accordance with the more exact method.

1.3.2 Basic details

The calculation of the load carrying capacity is

based on the nominal torque of the driven machine. Alternatively, one can also start from the nominal torque of the prime mover if this corresponds with the torque requirement of the driven machine.

In order to be able to carry out the calculation for a cylindrical gear stage, the details listed in table 4 must be given in the units mentioned in the table. The geometric quantities are calculated according to tables 2 and 3. Usually, they are contained in the workshop drawings for cylindrical gears.

Table 4 Basic details				
Abbreviation	Meaning	Unit		
Р	Power rating	kW		
n ₁	Pinion speed	min ⁻¹		
а	Centre distance	mm		
m _n	Normal module	mm		
d _{a1}	Tip diameter of the pinion	mm		
d _{a2}	Tip diameter of the wheel	mm		
b ₁	Facewidth of the pinion	mm		
b ₂	Facewidth of the wheel	mm		
z ₁	Number of teeth of the pinion	-		
z ₂	Number of teeth of the wheel	-		
х ₁	Addendum modification coefficient of the pinion	-		
х ₂	Addendum modification coefficient of the wheel	-		
α_{n}	Normal pressure angle	Degree		
β	Reference helix angle	Degree		
υ ₄₀	Kinematic viscosity of lubricating oil at 40 °C	mm²/s		
R _{z1}	Peak-to-valley height on pinion flank	μ m		
R _{z2}	Peak-to-valley height on wheel flank	μm		

In the further course of the calculation, the quantities listed in table 5 are required. They are derived from the basic details according to table 4.

Table 5 Derived quantities					
Designation	signation Relation				
Gear ratio	$u = z_2/z_1$	-			
Reference diameter of the pinion	$d_1 = z_1 \cdot m_n / \cos \beta$	mm			
Transverse tangential force at pinion reference circle	$F_t = \frac{6 \cdot 10^7}{\pi} \cdot \frac{P}{d_1 \cdot n_1}$	N			
Transverse tangential force at pitch circle	$F_{u} = F_{t} \cdot \frac{d_{1}}{2 \cdot a} (u+1)$	N			
Circumferential speed at reference circle	$v = \pi \cdot d_1 \cdot n_1/60000$	m/s			
Base helix angle	$\beta_b = \arcsin(\cos\alpha_n \cdot \sin\beta)$	Degree			
Virtual number of teeth of the pinion	$z_{n1} = z_1 / (\cos\beta \cdot \cos^2\beta_b)$	_			
Virtual number of teeth of the wheel	$z_{n2} = z_2/(\cos\beta \cdot \cos^2\beta_b)$	-			
Transverse module	$m_t = m_n / \cos \beta$	mm			
Transverse pressure angle	$\alpha_t = \arctan(\tan\alpha_n / \cos\beta)$	Degree			
Working transverse pressure angle	$\alpha_{\text{wt}} = \arccos \left[(z_1 + z_2) m_t \cdot \cos \alpha_t / (2 \cdot a) \right]$	Degree			
Transverse pitch	$p_{et} = \pi \cdot m_t \cdot \cos \alpha_t$	mm			
Base diameter of the pinion	$d_{b1} = z_1 \cdot m_t \cdot \cos \alpha_t$	mm			
Base diameter of the wheel	$d_{b2} = z_2 \cdot m_t \cdot \cos \alpha_t$				
Length of path of contact	$g_{\alpha} = \frac{1}{2} \left(\sqrt{d_{a1}^2 - d_{b1}^2} + \frac{u}{ u } \sqrt{d_{a2}^2 - d_{b2}^2} \right) - a \cdot \sin \alpha_{wt}$	mm			
Transverse contact ratio	$\varepsilon_{\alpha} = g_{\alpha} / p_{et}$	_			
Overlap ratio	$ \varepsilon_{\beta} = b \cdot \tan \beta_b / p_{et} $ $ b = \min (b_1, b_2) $	_			

1.3.3 General factors

1.3.3.1 Application factor

With the application factor K_A , all additional forces acting on the gears from external sources are taken into consideration. It is dependent on the characteristics of the driving and driven machines, as well as the couplings, the masses and stiffness of the system, and the operating conditions.

The application factor is determined by the service classification of the individual gear. If possible, the factor K_A should be determined by means of a careful measurement or a comprehensive analysis of the system. Since very often it is not possible to carry out the one or other method without great expenditure, reference values are given in table 6 which equally apply to all gears in a gear unit.

Table 6 Application factor K _A						
Working mode of prime mover		Working mode of t	he driven machine			
	Uniform	Moderate shock loads	Average shock loads	Heavy shock loads		
Uniform	1.00	1.25	1.50	1.75		
Moderate shock loads	1.10	1.35	1.60	1.85		
Average shock loads	1.25	1.50	1.75	2.00 or higher		
Heavy shock loads	1.50	1.75	2.00	2.25 or higher		

1.3.3.2 Dynamic factor

With the dynamic factor K_{ν} , additional internal dynamic forces caused in the meshing are taken into consideration. Taking z_1 , ν and u from tables 4 and 5, it is calculated from

$$K_{v} = 1 + 0.0003 \cdot z_{1} \cdot v \sqrt{\frac{u^{2}}{1 + u^{2}}}$$
 (4)

1.3.3.3 Face load factor

The face load factor $K_{H\beta}$ takes into account the increase in the load on the tooth flanks caused by non-uniform load distribution over the facewidth. According to /8/, it can be determined by means of different methods. Exact methods based on comprehensive measurements or calculations or on a combination of both are very expensive. Simple methods, however, are not exact, as a consequence of which estimations made to be on the safe side mostly result in higher factors. For normal cylindrical gear teeth without longitudinal correction, the face load factor can be calculated according to method D in accordance with /8/ dependent on facewidth b and reference diameter d₁ of the pinion, as follows:

$$K_{H\beta} = 1.15 + 0.18 (b/d_1)^2 + 0.0003 \cdot b$$
 (5)

with b = min (b₁, b₂). As a rule, the gear unit manufacturer carries out an analysis of the load distribution over the facewidth in accordance with an exact calculation method /13/. If required, he makes longitudinal corrections in order to

attain uniform load carrying over the facewidth, see subsection 1.2.5. Under such conditions, the face load factor lies within the range of $K_{H\beta}$ = 1.1 ... 1.25. As a rough rule applies: A sensibly selected crowning symmetrical in length reduces the amount of $K_{H\beta}$ lying above 1.0 by approx. 40 to 50%, and a directly made longitudinal correction by approx. 60 to 70%.

In the case of slim shafts with gears arranged on one side, or in the case of lateral forces or moments acting on the shafts from external sources, for the face load factors for gears without longitudinal correction the values may lie between 1.5 and 2.0 and in extreme cases even at 2.5.

Face load factor $K_{F\beta}$ for the determination of increased tooth root stress can approximately be deduced from face load factor $K_{H\beta}$ according to the relation

$$\mathsf{K}_{\mathsf{F}\beta} = \left(\mathsf{K}_{\mathsf{H}\beta}\right)^{0.9} \tag{6}$$

1.3.3.4 Transverse load factors

The transverse load factors $K_{H\alpha}$ and $K_{F\alpha}$ take into account the effect of the non-uniform distribution of load between several pairs of simultaneously contacting gear teeth. Under the conditions as laid down in subsection 1.3.1, the result for surface stress and for tooth root stress according to method B in accordance with /8/ is

$$K_{H\alpha} = K_{F\alpha} = 1.0 \tag{7}$$

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1.3.4 Tooth flank load carrying capacity

The calculation of surface durability against pitting is based on the Hertzian pressure at the pitch circle. For pinion and wheel the same effective Hertzian pressure σ_H is assumed. It must not exceed the permissible Hertzian pressure σ_{HP} , i.e. $\sigma_H \leq \sigma_{HP}$.

1.3.4.1 Effective Hertzian pressure

The effective Hertzian pressure is dependent on the load, and for pinion and wheel is equally derived from the equation

$$\sigma_{H} = Z_{E} Z_{H} Z_{\beta} Z_{\epsilon} \sqrt{K_{A} K_{V} K_{H\alpha} K_{H\beta} \frac{u+1}{u} \frac{F_{t}}{d_{1} \cdot b}}$$
 (8)

3,0

2,8

2,6

2,4

2,2

2,0

1,8

1,6

see table 4.

Zμ

-0,01

0,005

0,005

0.01

0,02

0.03

0,04

0.06

0,08

10

 σ_H Effective Hertzian pressure in N/mm²

Further:

b Common facewidth of pinion and wheel

Ft, u, d1 acc. to table 5

K_A Application factor acc. to table 6

K_v Dynamic factor acc. to equation (4)

K_{H6} Face load factor acc. to eq (5)

 $K_{H\alpha}$ Transverse load factor acc. to eq. (7)

 Z_E Elasticity factor; $Z_E = 190 \sqrt{N/mm^2}$ for gears out of steel

Z_H Zone factor acc. to figure 17

 Z_{β} Helix angle factor acc. to eq (9)

 Z_{ϵ} Contact ratio factor acc. to eq. (10) or (11)

With ß according to table 4 applies:

$$Z_{\beta} = \sqrt{\cos\beta}$$
 (9)

With ϵ_{α} and ϵ_{β} according to table 5 applies:

$$Z_{\epsilon} = \sqrt{\frac{4 - \epsilon_{\alpha}}{3} (1 - \epsilon_{\beta}) + \frac{\epsilon_{\beta}}{\epsilon_{\alpha}}} \text{ for } \epsilon_{\beta} < 1 \quad (10)$$

$$Z_{\epsilon} = \sqrt{\frac{1}{\epsilon_{\alpha}}} \qquad \text{for } \epsilon_{\beta} \geqq 1 \tag{11}$$

pinion and wheel and are determined in the following.

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Zone factor Z_H depending on helix angle β as well as on the numbers of teeth z_1 , z_2 , and

addendum modification coefficients x1, x2;

— β
Figure 17

30

40°

The lubricant factor is computed from the lubricating oil viscosity υ_{40} according to table 4 using the following formula:

$$Z_{L} = 0.91 + \frac{0.25}{\left(1 + \frac{112}{v_{40}}\right)^{2}}$$
 (13)

1.3.4.2 Permissible Hertzian pressure

The permissible Hertzian pressure is determined by

$$\sigma_{HP} = Z_L Z_v Z_X Z_R Z_W \frac{\sigma_{Hlim}}{S_H}$$
 (12)

 σ_{HP} permissible Hertzian pressure in N/mm². It is of different size for pinion and wheel if the strengths of materials σ_{Hlim} are different. Factors $Z_L,\,Z_V,\,Z_R,\,Z_W$ and Z_X are the same for



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For the speed factor, the following applies using the circumferential speed v according to table 5:

$$Z_{V} = 0.93 + \frac{0.157}{\sqrt{1 + \frac{40}{V}}}$$
 (14)

The roughness factor can be determined as a function of the mean peak-to-valley height $R_Z = (R_{Z1} + R_{Z2})/2$ of the gear pair as well as the gear ratio u and the reference diameter d_1 of the pinion, see tables 4 and 5, from

$$Z_{R} = \left[\frac{0.513}{R_{z}}\sqrt[3]{(1 + |u|) d_{1}}\right]^{0.08}$$
 (15)

For a gear pair with the same tooth flank hardness on pinion and wheel, the work hardening factor is

$$Z_W = 1.0$$
 (16)

The size factor is computed from module m_{n} according to table 4 using the following formula:

$$Z_X = 1.05 - 0.005 \,\mathrm{m_n}$$
 (17)

with the restriction $0.9 \le Z_X \le 1$.

σ_{Hlim} Endurance strength of the gear material. For gears made out of case hardening steel, case hardened, figure 18 shows a range from 1300 ... 1650 N/mm² depending on the surface hardness of the tooth flanks and the quality of the material. Under the conditions as described in subsection 1.3.1, material quality MQ may be selected for pinion and wheel, see table on page 77.

S_H Required safety factor against pitting, see subsection 1.3.6.

1.3.5 Tooth strength

The maximum load in the root fillet at the 30-degree tangent is the basis for rating the tooth strength. For pinion and wheel it shall be shown separately that the effective tooth root stress σ_F does not exceed the permissible tooth root stress σ_{FP} , i.e. $\sigma_F < \sigma_{FP}$.

1.3.5.1 Effective tooth root stress

As a rule, the load-dependent tooth root stresses for pinion and wheel are different. They are calculated from the following equation:

$$\sigma_{F} = K_{A} K_{V} K_{F\alpha} K_{F\beta} \cdot \frac{F_{t}}{b \cdot m_{n}} \cdot Y_{FS} Y_{\beta} Y_{\epsilon} \quad (18)$$

σ_E Effective tooth root stress in N/mm²

The following factors are of equal size for pinion and wheel:

m_n, F_t acc. to tables 4 and 5

K_A Application factor acc. to table 6

K_v Dynamic factor acc. to equation (4)

K_{F6} Face load factor acc. to equation (6)

K_{Eq} Transverse load factor acc. to eq (7)

Y_ε Contact ratio factor acc. to eq (19)

 Y_{β} Helix angle factor acc. to eq (20)

The following factors are of different size for pinion and wheel:

b₁, b₂ Facewidths of pinion and wheel acc. to table 4. If the facewidths of pinion and wheel are different, it may be assumed that the load bearing width of the wider facewidth is equal to the smaller facewidth plus such extension of the wider that does not exceed one times the module at each end of the teeth.

Y_{FS1}, Tip factors acc. to figure 19. They account Y_{FS2} for the complex stress condition inclusive of the notch effect in the root fillet.

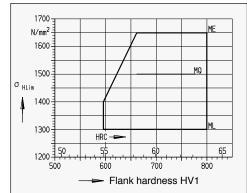
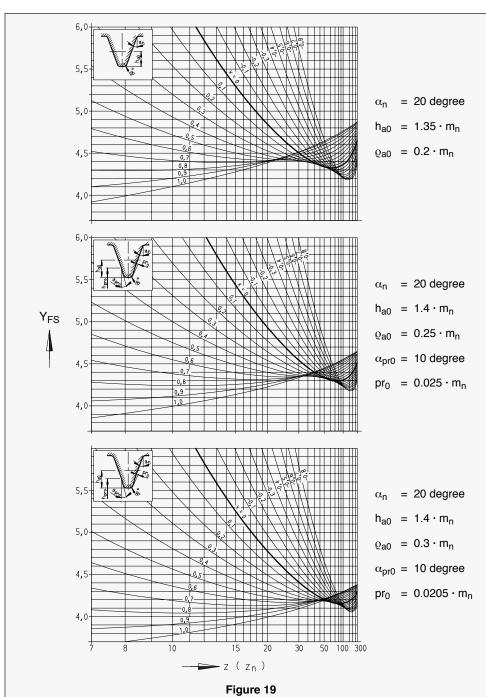


Figure 18

Allowable stress number for contact stress σ_{Hlim} of alloyed case hardening steels, case hardened, depending on the surface hardness HV1 of the tooth flanks and the material quality.

ML modest demands on the material quality MQ normal demands on the material quality ME high demands on the material quality, see /11/



Tip factor Y_{FS} for external gears with standard basic rack tooth profile acc. to DIN 867 depending on the number of teeth z (or z_n in case of helical gears) and addendum modification coefficient x, see tables 4 and 5. The following only approximately applies to internal gears: $Y_{FS} = Y_{FS\infty}$ (\approx value for x = 1.0 and z = 300).

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With the helix angle β acc. to table 4 and the overlap ratio ϵ_{β} acc. to table 5 follows:

$$Y_{\varepsilon} = 0.25 + \frac{0.75}{\varepsilon_{\alpha}} \cdot \cos^2 \beta \tag{19}$$

with the restriction $0.625 \le Y_{\epsilon} \le 1$

$$Y_{\beta} = 1 - \varepsilon_{\beta} \cdot \frac{\beta}{120^{\circ}}$$
 (20)

with the restriction

$$Y_{\beta} \ge \text{max.} [(1 - 0.25 \varepsilon_{\beta}); (1 - \beta/120)].$$

1.3.5.2 Permissible tooth root stress

The permissible tooth root stress for pinion and wheel is determined by

$$\sigma_{FP} = Y_{ST} Y_{\delta relT} Y_{RrelT} Y_{X} \frac{\sigma_{Flim}}{(S_F)}$$
 (21)

 σ_{FP} permissible tooth root stress in N/mm². It is not equal for pinion and wheel if the material strengths σ_{Flim} are not equal. Factors $Y_{ST},\,Y_{\delta relT},\,Y_{RrelT}$ and Y_X may be approximately equal for pinion and wheel.

 \dot{Y}_{ST} is the stress correction factor of the reference test gears for the determination of the bending stress number σ_{Flim} . For standard reference test gears, \dot{Y}_{ST} = 2.0 has been fixed in the standard.

 $Y_{\delta relT}$ is the relative sensitivity factor (notch sensitivity of the material) referring to the standard reference test gear. By approximation $Y_{\delta relT} = 1.0$.

For the relative surface factor (surface roughness factor of the tooth root fillet) referring to the standard reference test gear the following applies by approximation, depending on module m_n:

$$Y_{RrelT} = 1.00 \text{ for}$$
 $m_n \le 8 \text{ mm}$
= 0.98 for 8 mm < $m_n \le 16 \text{ mm}$ (22)
= 0.96 for $m_n > 16 \text{ mm}$

and for the size factor

$$Y_X = 1.05 - 0.01 \text{ m}_n$$
 (23)

with the restriction $0.8 \le Y_X \le 1$.

σ_{Flim} Bending stress number of the gear material. For gears out of case hardening steel, case hardened, a range from 310 ... 520 N/mm² is shown in figure 20 depending on the surface hardness of the tooth flanks and the material quality. Under the conditions according to subsection 1.3.1, a strength pertaining to quality MQ may be used as a basis for pinion and wheel, see table on page 77.

S_F Safety factor required against tooth breakage, see subsection 1.3.6.

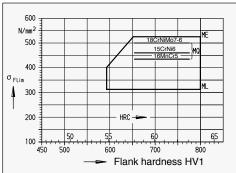


Figure 20

Bending stress number σ_{Flim} of alloyed case hardening steel, case hardened, depending on the surface hardness HV1 of the tooth flanks and the material quality.

ML modest demands on the material quality MQ normal demands on the material quality ME high demands on the material quality, see /11/

1.3.6 Safety factors

The minimum required safety factors according to DIN are:

against pitting $S_H = 1.0$ against tooth breakage $S_F = 1.3$.

In practice, higher safety factors are usual. For multistage gear units, the safety factors are determined about 10 to 20% higher for the expensive final stages, and in most cases even higher for the cheaper preliminary stages.

Also for risky applications a higher safety factor is given.

1.3.7 Calculation example

An electric motor drives a coal mill via a multistage cylindrical gear unit. The low speed gear stage is to be calculated.

Given: Nominal power rating P = 3300 kW; pinion speed n_1 = 141 min⁻¹; centre distance a = 815 mm; normal module m_n = 22 mm; tip diameter d_{a1} = 615.5 mm and d_{a2} = 1100 mm; pinion and wheel widths b_1 = 360 mm and b_2 = 350 mm; numbers of teeth z_1 = 25 and z_2 = 47; addendum modification coefficients x_1 = 0.310 and x_2 = 0.203; normal pressure angle α_n = 20 degree; helix angle β = 10 degree; kinematic viscosity of the lubricating oil v_{40} = 320 cSt; mean peak-to-valley roughness R_{z1} = R_{z2} = 4.8 μ m.

The cylindrical gears are made out of the material 18CrNiMo7-6. They are case hardened and ground with profile corrections and width-symmetrical crowning.

Cylindrical Gear Units

Load Carrying Capacity of Involute Gears Gear Unit Types

Calculation (values partly rounded):

Gear ratio u = 1.88; reference diameter of the pinion d $_1$ = 558.485 mm; nominal circumferential force on the reference circle F_t = 800425 N; circumferential speed on the reference circle v = 4.123 m/s; base helix angle β_b = 9.391 degree; virtual numbers of teeth z_{n1} = 26.08 and z_{n2} = 49.03; transverse module m_t = 22.339 mm; transverse pressure angle α_t = 20.284 degree; working transverse pressure angle α_{wt} = 22.244 degree; normal transverse pitch p_{et} = 65.829 mm; base diameters d_{b1} = 523.852 mm and d_{b2} = 984.842 mm; length of path of contact g_{α} = 98.041 mm; transverse contact ratio ϵ_{α} = 1.489; overlap ratio ϵ_{β} = 0.879.

Application factor $K_A=1.50$ (electric motor with uniform mode of operation, coal mill with medium shock load); dynamic factor $K_V=1.027$; face load factor $K_{H\beta}=1.20$ [acc. to equation (5) follows $K_{H\beta}=1.326$, however, because of symmetrical crowning the calculation may be made with a smaller value]; $K_{F\beta}=1.178$; $K_{H\alpha}=K_{F\alpha}=1.0$.

Load carrying capacity of the tooth flanks:

Elasticity factor $Z_E=190~\sqrt{N/mm^2}$; zone factor $Z_H=2.342$; helix angle factor $Z_\beta=0.992$; contact ratio factor $Z_\epsilon=0.832$. According to equation (8), the Hertzian pressure for pinion and wheel is $\sigma_H=1251~N/mm^2$.

Lubricant factor Z_L = 1.047; speed factor Z_V = 0.978; roughness factor Z_R = 1.018; work hardening factor Z_W = 1.0; size factor Z_X = 0.94. With the allowable stress number for contact stress (pitting) σ_{Hlim} = 1500 N/mm², first the permissible Hertzian pressure σ_{HP} = 1470 N/mm² is determined from equation (12) without taking into account the safety factor.

The safety factor against pitting is found by $S_H = \sigma_{HP}/\sigma_H = 1470/1251 = 1.18$. The safety factor referring to the torque is $S_H^2 = 1.38$.

Load carrying capacity of the tooth root:

Contact ratio factor $Y_{\epsilon}=0.738$; helix angle factor $Y_{\beta}=0.927$; tip factors $Y_{FS1}=4.28$ and $Y_{FS2}=4.18$ (for $h_{a0}=1.4$ m_n; $\varrho_{a0}=0.3$ m_n; $\alpha_{pr0}=10$ degree; pr₀ = 0.0205 m_n). The effective tooth root stresses $\sigma_{F1}=537$ N/mm² for the pinion and $\sigma_{F2}=540$ N/mm² for the wheel can be obtained from equation (18).

Stress correction factor $Y_{ST}=2.0$; relative sensitivity factor $Y_{\delta relT}=1.0$; relative surface factor $Y_{RrelT}=0.96$; size factor $Y_{X}=0.83$. Without taking into consideration the safety factor, the permissible tooth root stresses for pinion and wheel $\sigma_{FP1}=\sigma_{FP2}=797$ N/mm² can be obtained from equation (21) with the bending stress number $\sigma_{Flim}=500$ N/mm².

The safety factors against tooth breakage referring to the torque are $S_F = \sigma_{FP}/\sigma_F$: for the pinion $S_{F1} = 797/537 = 1.48$ and for the wheel $S_{F2} = 797/540 = 1.48$.

1.4 Gear unit types

1.4.1 Standard designs

In the industrial practice, different types of gear units are used. Preferably, standard helical and bevel-helical gear units with fixed transmission ratio and size gradation are applied. These single-stage to four-stage gear units according to the modular construction system cover a wide range of speeds and torques required by the driven machines. Combined with a standard electric motor such gear units are, as a rule, the most economical drive solution.

But there are also cases where no standard drives are used. Among others, this is true for high torques above the range of standard gear units. In such cases, special design gear units are used, load sharing gear units playing an important role there.

1.4.2 Load sharing gear units

In principle, the highest output torques of gear units are limited by the manufacturing facilities, since gear cutting machines can make gears up to a maximum diameter only. Then, the output torque can be increased further only by means of load sharing in the gear unit. Load sharing gear units are, however, also widely used for lower torques as they provide certain advantages in spite of the larger number of internal components, among others they are also used in standard design. Some typical features of the one or other type are described in the following.

1.4.3 Comparisons

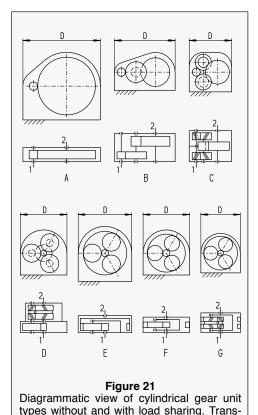
In the following, single-stage and two-stage gear units up to a ratio of i=16 are examined. For common gear units the last or the last and the last but one gear stage usually come to approx. 70 to 80% of the total weight and also of the manufacturing expenditure. Adding further gear stages in order to achieve higher transmission ratios thus does not change anything about the following fundamental description.

In figure 21, gear units without and with load sharing are shown, shaft 1 each being the HSS and shaft 2 being the LSS. With speeds n_1 and n_2 , the transmission ratio can be obtained from the formula

$$i = n_1 / n_2$$
 (24)

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The diameter ratios of the gears shown in figure 21 correspond to the transmission ratio i=7. The gear units have the same output torques, so that in figure 21 a size comparison to scale is illustrated. Gear units A, B, and C are with offset shaft arrangement, and gear units D, E, F, and G with coaxial shaft arrangement



Gear unit A has one stage, gear unit B has two stages. Both gear units are without load sharing. Gear units C, D, E, F, and G have two stages and are load sharing. The idler gears in gear units C and D have different diameters. In gear units E, F, and G the idler gears of one shaft have been joined to one gear so that they are also considered to be single-stage gear units.

mission ratio i = 7. Size comparison to scale of gear units with the same output torque.

Gear unit C has double load sharing. Uniform load distribution is achieved in the high-speed gear stage by double helical teeth and the axial movability of shaft 1.

In gear unit D the load of the high-speed gear stage is equally shared between three gears which is achieved by the radial movability of the sun gear on shaft 1. In the low-speed gear stage the load is shared six times altogether by means of the double helical teeth and the axial movability of the intermediate shaft.

In order to achieve equal load distribution between the three intermediate gears of gear units E, F, and G the sun gear on shaft 1 mostly is radially movable. The large internal gear is an annulus gear which in the case of gear unit E is connected with shaft 2, and in the case of gear units F and G with the housing. In gear units F and G, web and shaft 2 form an integrated whole. The idler gears rotate as planets around the central axle. In gear unit G, double helical teeth and axial movability of the idler gears guarantee equal load distribution between six branches.

1.4.3.1 Load value

By means of load value B_L , it is possible to compare cylindrical gear units with different ultimate stress values of the gear materials with each other in the following examinations.

According to /14/, the load value is the tooth peripheral force F_u referred to the pinion pitch diameter d_w and the carrying facewidth b, i.e.

$$B_{L} = \frac{F_{u}}{b \cdot d_{w}}$$
 (25)

The permissible load values of the meshings of the cylindrical gear units can be computed from the pitting resistance by approximation, as shown in /15/ (see section 1.3.4), using the following formula:

$$B_L \approx 7 \cdot 10^{-6} \frac{u}{u+1} \frac{\sigma^2_{Hlim}}{K_A \cdot S_H^2}$$
 (26)

with B_L in N/mm² and allowable stress number for contact stress (pitting) σ_{Hlim} in N/mm² as well as gear ratio u, application factor K_A and factor of safety from pitting S_H . The value of the gear ratio u is always greater than 1, and is negative for internal gear pairs (see table 3).

Load value B_L is a specific quantity and independent of the size of the cylindrical gear unit. The following applies for practically executed gear units: cylindrical gears out of case hardening steel $B_L = 4 \dots 6 \ N/mm^2$; cylindrical gears out of quenched and tempered steel $B_L = 1 \dots 1.5 \ N/mm^2$; planetary gear stages with annulus gears out of quenched and tempered steel, planet gears and sun gears out of case hardening steel $B_L = 2.0 \dots 3.5 \ N/mm^2$.

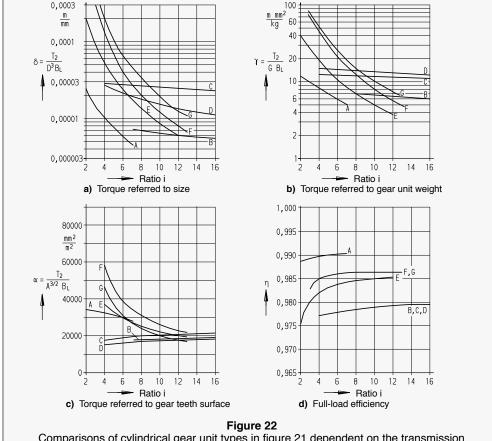
Gear Unit Types

1.4.3.2 Referred torques

In figure 22, referred torques for the gear units shown in figure 21 are represented, dependent on the transmission ratio i. Further explanations are given in table 7. The torque T_2 is referred to the construction dimension D when comparing the sizes, to the weight of the gear unit G when

comparing the weights, and to the generated surface A of the pitch circle cylinders when comparing the gear teeth surfaces. Gear unit weight G and gear teeth surface A (= generated surface) are measures for the manufacturing cost. The higher a curve, in figure 22, the better the respective gear unit in comparison with the others.

Table 7 Referred Torques				
Comparison criteria	Definition	Dimension	Units of the basic details	
Size	$\delta = \frac{T_2}{D^3 \; B_L}$	<u>m</u> 	T ₂ in Nm B ₁ in N/mm ²	
Weight	$\gamma = \frac{T_2}{G B_L}$	m mm ² kg	D in mm	
Gear teeth surface	$\alpha = \frac{T_2}{A^{3/2} \; B_L}$	mm ² m ²	G in kg A in m ²	



Comparisons of cylindrical gear unit types in figure 21 dependent on the transmission ratio i. Explanations are given in table 7 as well as in the text.

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Gear Unit Types

For all gear units explained in figures 21 and 22, the same prerequisites are valid. For all gear units, the construction dimension D is larger than the sum of the pitch diameters by the factor 1.15. Similar definitions are valid for gear unit height and width. Also the wall thickness of the housing is in a fixed relation to the construction dimension D /15/.

With a given torque T_2 and with a load value B_L computed according to equation (26), the construction dimension D, the gear unit weight G, and the gear teeth surface A can be determined by approximation by figure 22 for a given transmission ratio i. However, the weights of modular-type gear units are usually higher, since the housing dimensions are determined according to different points of view.

Referred to size and weight, planetary gear units F and G have the highest torques at small ratios i. For ratios i < 4, the planet gear becomes the pinion instead of the sun gear. Space requirement and load carrying capacity of the planet gear bearings decrease considerably. Usually, the planet gear bearings are arranged in the planet carrier for ratio i < 4.5.

Gear units C and D, which have only external gears, have the highest torque referred to size and weight for ratios above i \approx 7. For planetary gear units, the torque referred to the gear teeth surface is more favourable only in case of small ratios, if compared with other gear units. It is to be taken into consideration, however, that internal gears require higher manufacturing expenditure than external gears for the same quality of manufacture.

The comparisons show that there is no optimal gear unit available which combines all advantages over the entire transmission ratio range. Thus, the output torque referred to size and weight is the most favourable for the planetary gear unit, and this all the more, the smaller the transmission ratio in the planetary gear stage. With increasing ratio, however, the referred torque decreases considerably. For ratios above i = 8, load sharing gear units having external gears only are more favourable because with increasing ratio the referred torque decreases only slightly.

With regard to the gear teeth surface, planetary gear units do not have such big advantages if compared to load sharing gear units having external gears only.

1.4.3.3 Efficiencies

When comparing the efficiencies, figure 22d, only the power losses in the meshings are taken into consideration. Under full load, they come to approx. 85% of the total power loss for common

cylindrical gear units with rolling bearings. The efficiency as a quantity of energy losses results from the following relation with the input power at shaft 1 and the torques T_1 and T_2

$$\eta = \left| \frac{1}{i} \frac{T_2}{T_1} \right| \tag{27}$$

All gear units shown in figure 21 are based on the same coefficient of friction of tooth profile $\mu_Z=0.06$. Furthermore, gears without addendum modification and numbers of teeth of the pinion z=17 are uniformly assumed for all gear units /15/, so that a comparison is possible.

The single stage gear unit A has the best efficiency. The efficiencies of the two stage gear units B, C, D, E, F, and G are lower because the power flow passes two meshings. The internal gear pairs in gear units E, F, and G show better efficiencies owing to lower sliding velocities in the meshings compared to gear units B, C, and D which only have external gear pairs.

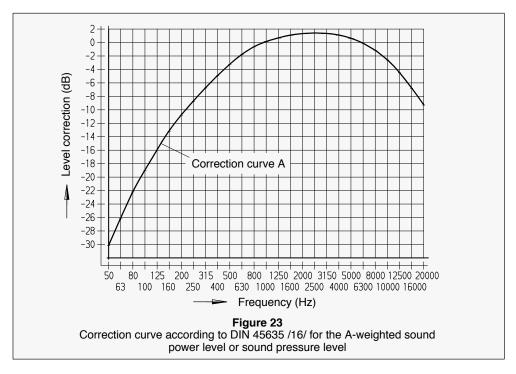
The lossfree coupling performance of planetary gear units F and G results in a further improvement of the efficiency. It is therefore higher than that of other comparable load sharing gear units. For higher transmission ratios, however, more planetary gear stages are to be arranged in series so that the advantage of a better efficiency compared to gear units B, C, and D is lost.

1.4.3.4 Example

Given: Two planetary gear stages of type F arranged in series, total transmission ratio i = 20, output torque $T_2 = 3 \cdot 10^6$ Nm, load value $B_L = 2.3$ N/mm². A minimum of weight is approximately achieved by a transmission ratio division of i = $5 \cdot 4$ of the HS and LS stage. At $\gamma_1 = 30$ m mm²/kg and $\gamma_2 = 45$ m mm²/kg according to figure 22 b, the weight for the HS stage is approximately 10.9 t and for the LS stage approximately 30 t, which is a total 40.9 t. The total efficiency according to figure 22 d is $\eta = 0.986 \cdot 0.985 = 0.971$.

In comparison to a gear unit of type D with the same transmission ratio i = 20 and the same output torque $T_2=3\cdot 10^6$ Nm, however, with a better load value $B_L=4$ N/mm² this gear unit has a weight of 68.2 t according to figure 22 with $\gamma=11$ m mm²/kg and is thus heavier by 67%. The advantage is a better efficiency of $\eta=0.98.$ The two planetary gear stages of type F together have a power loss which is by 45% higher than that of the gear unit type D. In addition, there is not enough space for the rolling bearings of the planet gears in the stage with i = 4.

Noise Emitted by Gear Units



1.5 Noise emitted by gear units

1.5.1 Definitions

Noise emitted by a gear unit – like all other noises – is composed of tones having different frequencies f.

Measure of intensity is the sound pressure p which is the difference between the highest (or lowest) and the mean pressure in a sound wave detected by the human ear.

The sound pressure can be determined for a single frequency or – as a combination – for a frequency range (single-number rating). It is dependent on the distance to the source of sound.

In general, no absolute values are used but amplification or level quantities in bel (B) or decibel (dB).

Conversion of the absolute values is made for the sound pressure using equation

$$L_p = 20 \cdot \log(p/p_0) [dB]$$
 (28)

and for the sound power using equation

$$L_W = 10 \cdot \log(P/P_0) [dB]$$
 (29)

The reference values (e.g. p_0 and P_0) have been determined in DIN EN ISO 1683. For the sound pressure, the threshold of audibility of the human ear at 2 kHz has been taken as reference value ($p_0 = 2 \cdot 10^{-5}$ Pa). For the conversion of the sound power applies ($P_0 = 10^{-12}$ W).

In order to take into consideration the different sensitivities of the human ear at different frequencies, the physical sound pressure value at the different frequencies is corrected according to rating curve A, see figure 23.

A-weighted quantities are marked by subscript "A" (e.g. sound pressure L_p ; A-weighted sound pressure L_{DA}).

Apart from sound pressures at certain places, sound powers and sound intensities of a whole system can be determined.

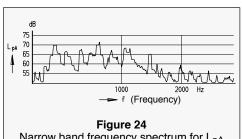
From the gear unit power a very small part is turned into sound power. This mainly occurs in the meshings, but also on bearings, fan blades, or by oil movements. The sound power is transmitted from the sources to the outside gear unit surfaces mainly by structure-borne noise (material vibrations). From the outside surfaces, air borne noise is emitted.

The sound power L_{WA} is the A-weighted sound power emitted from the source of sound and thus a quantity independent of the distance. The sound power can be converted to an average sound pressure for a certain place. The sound pressure decreases with increasing distance from the source of sound.

The sound intensity is the flux of sound power through a unit area normal to the direction of propagation. For a point source of sound it results from the sound power LW divided by the spherical enveloping surface $4 \cdot \pi \cdot r^2$, concentrically enveloping the source of sound. Like the sound pressure, the sound intensity is dependent on the distance to the source of sound, however, unlike the sound pressure it is a directional quantity.

The recording instrument stores the sound pressure or sound intensity over a certain period of time and writes the dB values in frequency ranges (bands) into the spectrum (system of coordinates).

Very small frequency ranges, e.g. 10 Hz or 1/12 octaves are termed narrow bands, see figure 24.



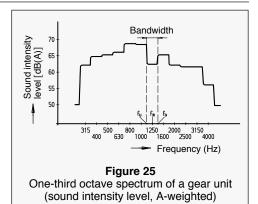
Narrow band frequency spectrum for L_{DA} (A-weighted sound pressure level) at a distance of 1 m from a gear unit.

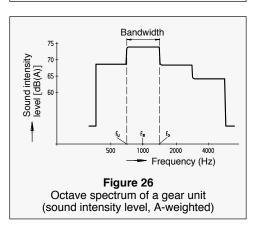
Histograms occur in the one-third octave spectrum and in the octave spectrum, see figures 25 and 26. In the one-third octave spectrum (spectrum with 1/3 octaves), the bandwidth results from

$$f_0 / f_u = \sqrt[3]{2}$$
, i.e. $f_0 / f_u = 1.26$,
 $f_0 = f_m \cdot 1.12$ and $f_u = f_m / 1.12$;

f_m = mean band frequency, f_o = upper band frequency, f_u = lower band frequency. In case of octaves, the upper frequency is twice as big as the lower one, or

$$f_0 = f_m \cdot 1.41$$
 and $f_u = f_m / 1.41$.





The total level (resulting from logarithmic addition of individual levels of the recorded frequency range) is a single-number rating. The total level is the common logical value for gear unit noises. The sound pressure level is valid for a certain distance, in general 1 m from the housing surface as an ideal parallelepiped.

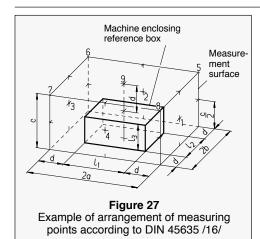
1.5.2 Measurements

The main noise emission parameter is the sound power level.

1.5.2.1 Determination via sound pressure

DIN 45635 Part 1 and Part 23 describe how to determine the sound power levels of a given gear unit /16/. For this purpose, sound pressure levels L_{DA} are measured at fixed points surrounding the gear unit and converted into sound power levels L_{WA}. The measurement surface ratio L_S is an auxiliary quantity which is dependent on the sum of the measurement surfaces. When the gear unit is placed on a reverberant base, the bottom is not taken into consideration, see example in figure 27.

Noise Emitted by Gear Units



In order to really detect the noise radiated by the gear unit alone, corrections for background noise and environmental influences are to be made. They are estimated by measuring background noises (caused by noise radiating machines in the vicinity) and the characteristics of the room (reverberation time, resonances in the room) and are used as correction values in the sound power calculation. If the background noises are too loud (limit values of correction factors are achieved), this method can no longer be used because of insufficient accuracy.

1.5.2.2 Determination via sound intensity

The gear unit surface is scanned manually all around at a distance of, for instance, 10 cm, by means of a special measuring device containing two opposing microphones. The mean of the levels is taken via the specified time, e.g. two minutes. The sound intensity determined in this way is the average sound energy flow penetrating the scanned surface. The sound power can be determined by multiplying the sound intensity by the scanned surface area.

This method has been standardized in DIN EN ISO 9614-2. Because of the special property of the measuring device – to determine the direction of sound incidence – it is very easy to eliminate background noises.

The results correspond to the values as determined in accordance with DIN 45635. As a rule, the sound intensity method is more accurate (less measurement uncertainty) because it is less insensitive to noises and can also be used in case of loud background noises (e.g. in industrial plants).

1.5.3 Prediction

It is not possible to exactly calculate in advance the sound power level of a gear unit to be made. However, one can base the calculations on experience. In the VDI guidelines 2159 /17/, for example, reference values are given. Gear unit manufacturers, too, mostly have own records.

The VDI guidelines are based on measurements carried out on a large number of industrial gear units. Main influence parameters for gear unit noises are gear unit type, transmitted power, manufacturing quality, and speed. In VDI 2159, a distinction is made between cylindrical gear units with rolling bearings, see figure 28, cylindrical gear units with sliding bearings (highspeed gear units), bevel gear and bevel-helical gear units, planetary gear units, and worm gear units. Furthermore, information on speed variators can be found in the guidelines.

Figure 28 exemplary illustrates a characteristic diagram of emissions for cylindrical gear units. Similar characteristic diagrams are also available for the other gear unit types mentioned. Within the characteristic diagrams, 50%- and 80%-lines are drawn. The 80%-line means, for example, that 80% of the recorded industrial gear units radiate lower noises.

The lines are determined by mathematical equations. For the 80%-lines, the equations according to VDI 2159 are:

Gear units	Total sound power level L _{WA}
Cylindrical gear units (rolling bearings)	77.1 + 12.3 · log P / kW (dB)
Cylindrical gear units (sliding bearings)	85.6 + 6.4 · log P / kW (dB)
Bevel gear and bevel-helical gear units	71.7 + 15.9 · log P / kW (dB)
Planetary gear units	87.7 + 4.4 · log P / kW (dB)
Worm gear units	65.0 + 15.9 · log P / kW (dB)

For restrictions, see VDI 2159.

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Type: Cylindrical gear units with external teeth mainly (> 80%) having the following characteristic

features:

Housing: Cast iron housing

Bearing arrangement: Rolling bearings

Lubrication: Dip lubrication

Installation:

Rigid on steel or concrete

Power rating: 0.7 up to 2400 kW Input speed (= max. speed):

1000 up to 5000 min⁻¹ (mostly 1500 min⁻¹)

Max. circumferential speed:

1 up to 20 ms⁻¹
Output torque:

100 up to 200 000 Nm

No. of gear stages: 1 to 3

Information on gear teeth: HS gear stage with helical teeth ($\beta = 10^{\circ}$ up to 30°), hardened, fine-machined, DIN quality 5 to 8

dR 130 Logarithmic regression $L_{WA} = 77.1 + 12.3 \times log P/kW dB$ 120 Sound power level L_{WA} (80%-line) Certainty rate $r^2 = 0.83$ 110 Probability 90% 100 90 80 80% 70 50% 0,1 2 5 10 100 1000 10000 kW Mechanical power rating P

Figure 28

Characteristic diagram of emissions for cylindrical gear units (industrial gear units) acc. to VDI 2159 /17/

To calculate a sound pressure level from the given sound power values a measuring method is used comparable with that described in DIN 45635. It is assumed that the sound energy is uniquely radiated from the object in all directions and can propagate undisturbed (free sound propagation). This assumption results in the so-called measurement surface sound pressure level, the average sound pressure at a determined distance to the gear unit.

The measurement surface sound pressure level L_{pA} at a distance of 1 m is calculated from the total sound power level

$$L_{pA} = L_{WA} - L_{s} (dB)$$
 (30)

$$L_{S} = 10 \cdot log S (dB)$$
 (31)

S = Sum of the hypothetical surfaces (m²) enveloping the gear unit at a distance of 1 m (ideal parallelepiped)

Example of information for P = 100 kW in a twostage cylindrical gear unit of size 200 (centre distance in the 2nd gear stage in mm), with rolling bearings, of standard quality:

"The sound power level, determined in accordance with DIN 45635 (sound pressure measurement) or according to the sound intensity measurement method, is 102 ± 3 dB (A). Room and connection influences have not been taken into consideration. If it is agreed that measurements are to be made they will be carried out on the manufacturer's test stand."

Note:

For this example, a measurement surface sound pressure level of $102 - 13.2 \approx 89$ dB (A), tolerance \pm 3 dB, is calculated at a distance of 1 m with a measurement surface S = 21 m² and a measurement surface ratio L_S = 13.2 dB. (Error of measurement according to DIN EN ISO 9614-2 for measurements in the industrial area with accuracy grade 2.)

Individual levels in a frequency spectrum cannot safely be predicted for gear units because of the multitude of influence parameters.

1.5.4 Possibilities of influencing

With the selection of other than standard geometries and with special tooth modifications (see section 1.2.5), gear unit noises can be positively influenced. In some cases, such a procedure results in a reduction in the performance (e.g. module reduction) for the same size, in any case, however, in special design and manufacturing expenditure. Housing design, distribution of masses, type of rolling bearing, lubrication and cooling are also important.

Sometimes, the only way is to enclose the gear units which makes possible that the total level is reduced by 10 to 25 dB, dependent on the conditions.

Attention has to be paid to it, that no structureborne noise is radiated via coupled elements (couplings, connections) to other places from where then airborne noise will be emitted.

A sound screen does not only hinder the propagation of airborne noise but also the heat dissipation of a gear unit, and it requires more space.

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2. Shaft couplings

2.1 General fundamental principles

In mechanical equipment, drives are consisting of components like prime mover, gear unit, shafts, and driven machine. Such components are connected by couplings which have the following tasks:

- · Transmitting motion of rotation and torques;
- Compensating shaft misalignments (radial, axial, angular);
- Reducing the torsional vibration load, influencing and displacing the resonant ranges;

- · Damping torque and speed impulses;
- Interrupting the motion of rotation (clutches);
- · Limiting the torque (torque limiters);
- · Sound isolation;
- Electrical insulation.

The diversity of possible coupling variants is shown in the overview in figure 29. A distinction is made between the two main groups: couplings and clutches.

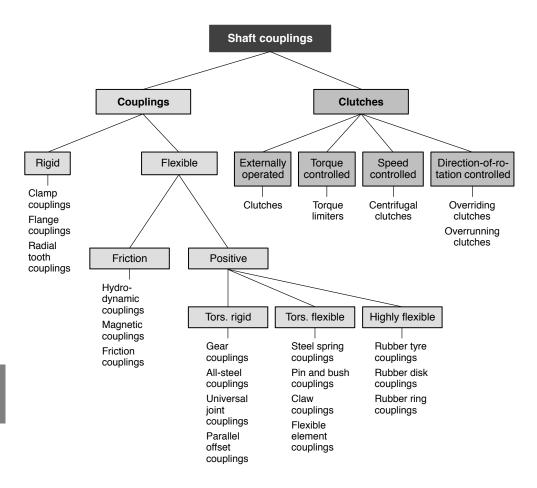


Figure 29
Overview of possible shaft coupling designs

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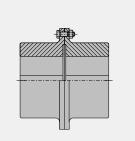
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Flange couplings

Torsionally rigid couplings

Connect two shafts ends torsionally rigid and exactly centered to each other • designed for heavily stressed shafts • not subject to wear and require no maintenance • suitable for both directions of rotation

Nominal torque: 1 300 ... 180 000 Nm



on request

N-EUPEX

Flexible pin couplings

Universally applicable coupling for compensating shaft displacements • maximum operational reliability owing to fail-safe device • suitable for plugin assembly and simplified assembly of the design consisting of three parts

Nominal torque: 19 ... 62 000 Nm

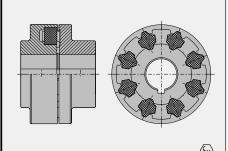
Brochure MD 10.1

N-EUPEX-DS

Flexible pin couplings

Disconnecting driving and driven machines upon failure of flexible elements (without fail-safe device) • universally applicable since combination with all parts of the N-EUPEX product range is possible

Nominal torque: 19 ... 21 200 Nm



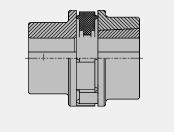
Brochure MD10.1

BIPEX

Flexible claw couplings

Fail-safe universal coupling • very compact design, high power capacity • very well suitable for plug-in assembly and assembly into bell housing • also with Taper bush for easy assembly and bore adaptation

Nominal torque: 13.5 ... 3 700 Nm



Brochure MD 10.1

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Shaft Couplings

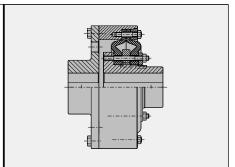
Highly Flexible Ring Couplings, Highly Flexible Rubber Tyre Couplings Highly Flexible Rubber Disk Couplings, Flexible Pin and Bush Couplings

ELPEX

Highly flexible ring couplings

Coupling without torsional backlash • can be used for large shaft misalignments • suitable for high dynamic loads, good damping properties

Nominal torque: 1 600 ... 90 000 Nm



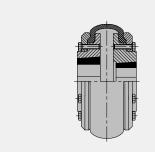
Brochure MD 10.1

ELPEX-B

Highly flexible rubber tyre couplings

Coupling without torsional backlash • compensating very large shaft misalignments • the rubber tyre can be easily replaced without the need to move the coupled machines • easy mounting on the shafts to be connected by means of Taper bushes

Nominal torque: 24 ... 14 500 Nm



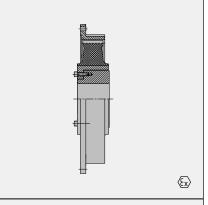
Brochure MD 10.1

ELPEX-S

Highly flexible rubber disk couplings

For connecting machines having a very nonuniform torque characteristic • very easy plug-in assembly • replacement of rubber disk element is possible without the need to move the coupled machines • flange with dimensions acc. to SAE J620d

Nominal torque: 330 ... 63 000 Nm



Brochure MD 10.1

RUPEX

Flexible pin and bush couplings

Fail-safe universal coupling for medium up to high torques, absorbing large shaft displacements • compact design, low weights and mass moments of inertia • suitable for plug-in assembly

Nominal torque: 200 ... 1 300 000 Nm

Brochure MD 10.1

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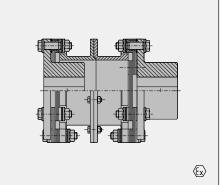
ARPEX - ARS (ARF / ARC / ARW)

All-steel couplings

Torsionally rigid coupling without clearance • compensates radial, angular and axial shaft displacements by means of two flexible disc packs • packs made out of stainless spring steel • easy assembly of coupling due to compact disc packs • modular system: many standard types by combination of standard components

Nominal torque: 92 ... 1 450 000 Nm

Brochure MD 10.1



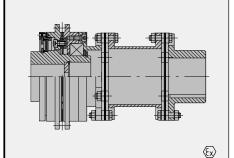
ARPEX - AKR

Torque limiters

On reaching the preset disconnecting torque, the torque limiter separates the coupled drive components both during slow and fast rising torques • after the disengagement process the coupling halves are out of contact, so that a wear-free running down can be realized

Nominal torque: 10 ... 75 000 Nm

Brochure MD 10.11



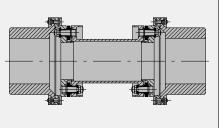
ARPEX - ART

High-speed couplings

Were designed for the energy and petrochemical industries and marine propulsion drives • are used for all high-speed purposes where reliable power transmission is required even with unavoidable shaft misalignment • meet the requirements of API 671

Nominal torque: 1 000 ... 535 000 Nm

Brochure MD10.9



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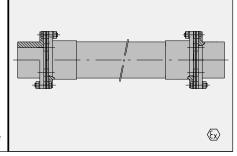
ARPEX - ARS Composite

Composite couplings

Corrosion-resistant, extreme light weight coupling for drives with great shaft distances (e.g. cooling tower fan) • up to 6 metres without centre bearing support • easy to handle and to install • maintenance-free and wear-free • reduced coupling vibrations

Nominal torque: 1 250 ... 7 600 Nm

Brochure MD 10.5



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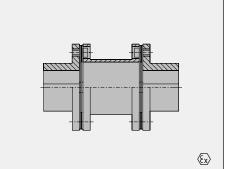
ARPEX - ARM

Miniature couplings

Designed for applications with very low torques
• fields of application: control systems, machine
tools, computer technology, tacho drives, measuring
and registering systems, printing and packaging
machines, stepping and servomotors, test stands

Nominal torque: 5 ... 25 Nm

Brochure MD10.10



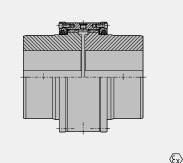
ZAPEX-ZW

Gear couplings

Double-jointed coupling compensating angular, parallel and axial misalignment of shafts • long-term lubrication is ensured by design measures and by using special seals • small dimensions; can be used for high shock loads • available in many types and variants

Nominal torque: 1 300 ... 7 200 000 Nm

Brochure MD 10.1



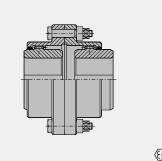
ZAPEX-ZI

Universal gear couplings

Double-jointed gear coupling with hobbed and crowned external gear teeth and low torsional backlash • largest possible bore range with grease lubricated gear teeth • mounting dimensions in metric and inch measures acc. to international standards

Nominal torque: 850 ... 125 000 Nm

Brochure MD10.1



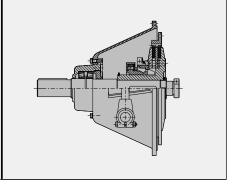
PLANOX

Multiple disk clutches

Constant torque transmission by means of contact pressure ensured by springs • many applications possible owing to mechanical, electrical, pneumatic or hydraulic disengaging devices • protects drives against overloading

Nominal torque: 10 ... 30 000 Nm

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Shaft Couplings

Fluid Couplings, Overrunning Clutches Torque Limiters

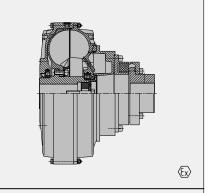
FLUDEX

Fluid couplings

Soft starting without shocks and acceleration of large masses during a load-relieved start of motor • torque limitation during starting and overload

- · excellent vibration separation and shock damping
- · torque transmission without wear

Nominal power ratings: 0.5 ... 2 500 kW



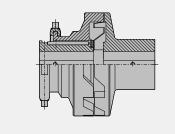
Brochure MD 10.1

UZWN

Overrunning clutches

Flender overrunning clutches allow to drive shafts and machines first by means of an auxiliary drive at low speed for startup and then by means of the main drive at higher speeds for full-load operation, the auxiliary drive then being shut off by overrunning.

Nominal torque: 9 000 ... 100 000 Nm



Dimensioned drawing M 495



Certified according to directive 94/9/EC (ATEX 95)
This coupling is particularly suitable for the use in hazardous locations

SECUREX

Torque limiters

With SECUREX, Flender provides a unique modular system of mechanical torque limiters. Owing to a variety of possibilities to combine standard components, the functions **Protection from overload** as well as **Compensation of shaft misalignment** can be fulfilled with just one compact unit.

With the development of SECUREX, Flender has concentrated its experiences gained over decades in the fields of both overload protection and compensation of shaft misalignments in one product line.

SECUREX is based on the wide range of Flender's standard couplings of different basic types and on standardized safety elements. With this combination, economical coupling solutions can be realized.

With the modular SECUREX system, Flender has focused on its core competence in the torque range of up to 1,500,000 Nm and benefits from its rich fund of knowledge and experience gained from application- and product-related R&D (e.g. sliding hubs in the wind energy industry, shear pin solutions in rolling mills, torque limiters in extruder applications, etc.).

Brochure K 440

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Couplings for pump drives

N-EUPEX

Flexible pin couplings

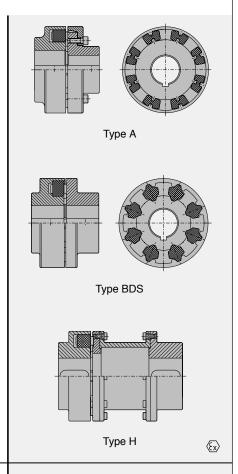
- Tried and tested drive element in millions of pump drives
- Good value for money, reliable, available worldwide
- Complete application-oriented assortment! In addition to the fail-safe standard design, a variant without fail-safe device is available especially developed for hazardous locations

Types B / BDS - in two parts

Types A / ADS - in three parts

Types H / HDS - with intermediate sleeve

Certified acc. to directive 94/9/EC (ATEX 95)



Katalog MD 10.1

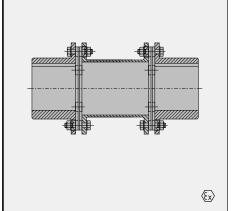
ARPEX - ARP

All-steel couplings

Were specially designed for pump drives

- Meet the requirements of API 610
- Design according to API 671, "NON-SPARKING" and certified acc. to directive 94/9/EC (ATEX 95) also available

Nominal torque: 100 ... 17 000 Nm



Katalog MD 10.1

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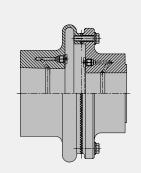
Coupling systems for railway vehicles

Input side couplings

Membrane coupling, Type MBG

- All-steel membrane coupling for the connection of motor and gear unit
- Without backlash; compensating relatively small shaft misalignments

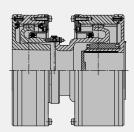
Max. nominal torque: 3 425 Nm Max. shaft diameter: 86 mm



Gear coupling, Type ZBG

- Double-jointed grease lubricated gear coupling between motor and gear unit
- Compensating extremely large shaft misalignments
- Split spacer with crowned gear teeth

Max. nominal torque: 15 000 Nm Max. shaft diameter: 100 mm



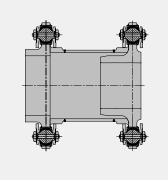
on request

Output side couplings

Articulated joint rubber coupling, Type GKG

- Double-jointed, flexible coupling without backlash, between axle drive and driving wheel shaft
- Low wear and low maintenance
- Compensating extremely large shaft misalignments, with low restoring forces

Max. nominal torque: 13 440 Nm Max. shaft diameter: 260 mm



on request

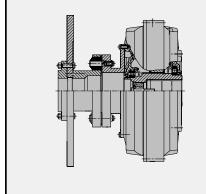
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Coupling systems for wind turbines

FLUDEX

Fluid couplings in combination with other couplings

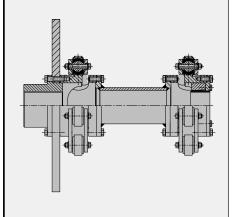
- Fluid coupling with slip between 2 and 3%.
 Peak torques caused by gusts of wind are compensated
- Combination with RUPEX coupling for small shaft misalignments
- Combination with articulated joint rubber coupling or ARPEX coupling for large shaft misalignments



on request

Articulated joint rubber couplings Type GKGW with brake disk

- Rubber-elastic ball bearings for extremely large shaft misalignments between gear unit and generator
- Very low restoring forces
- Electrically insulating and structure-borne noise absorbing
- Wearing parts and coupling can be removed without the need to move the generator
- Optional with torque-limiting slip hub

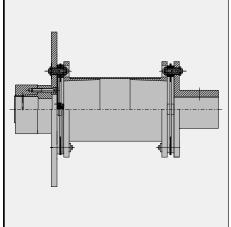


on request

ARPEX

All-steel couplings

- Design with hexagonal or square disc pack for very large shaft misalignments
- Optionally with slip hub for limiting the torque load in case of generator short-circuit
- Light spacer out of glass-fibre compound material for lightning insulation
- Conical bolt connection of disc packs for easy assembly



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а	m	Length of overhanging end
Α	m ²	Cross-sectional area
Α	m, rad	Amplitude of oscillation
A _D ; A _e		Damping energy; elastic energy
С	Nm/rad	Torsional stiffness
c'	N/m	Translational stiffness; bending stiffnes
d	m	Diameter
d _i	m	Inside diameter
da	m	Outside diameter
D	-	Attenuation ratio (Lehr's damping)
D _m	m	Mean coil diameter (coil spring)
e =	2.718	Euler's number
Е	N/m ²	Modulus of elasticity
f, f _e	Hz	Frequency; natural frequency
f	m	Deformation
F	N	Force
F (t)	N	Time-variable force
G	N/m ²	Shear modulus
i	-	Transmission ratio
İF	1	Number of windings (coil spring)
la	m ⁴	Second axial moment of area
Ip	m ⁴	Second polar moment of area
J, J _i	kgm ²	Mass moment of inertia
J*	kgm ²	Reduced mass moment of inertia of a two-mass vibration generating system
k	Nms/ rad	Viscous damping in case of torsional vibrations
k'	Ns/m	Viscous damping in case of translational and bending vibrations
I	m	Length; distance between bearings
m, m _i	kg	Mass
M (t)	Nm	Time-variable excitation moment
M_0	Nm	Amplitude of moment
M ₀ *	Nm	Reduced amplitude of moment of a two-mass vibration generating system
n _e	1/min	Natural frequency (vibrations per minute)
n ₁ ; n ₂	min ⁻¹	Input speed; output speed
q	_	Influence factor for taking into account the mass of the shaft when calculating the natural bending frequency
t	s	Time

	1	
Т	S	Period of a vibration
T	Nm	Torque
V	m ³	Volume
V	_	Magnification factor; Dynamic/ static load ratio
x	m	Displacement co-ordinate (translational, bending)
x̂	m	Displacement amplitude
α	rad	Phase angle
γ	rad	Phase angle with free vibration
δ	1/s	Damping constant
ε	rad	Phase displacement angle with forced vibration
η	_	Excitation frequency/natural frequency ratio
λ_{i}	_	Inherent value factor for i-th natural frequency
Λ	_	Logarithmic decrement
π =	3.14159	Peripheral/diameter ratio
6	kg/m ³	Specific density
ϕ,ϕ_i	rad	Angle of rotation
φ̂	rad	Angular amplitude of a vibration
φ	rad/s	Angular velocity (first time derivation of $\boldsymbol{\phi})$
φ	rad/s ²	Angular acceleration (second time derivation of $\boldsymbol{\phi})$
ϕ_{h}	rad	Vibratory angle of the free vibration (homogeneous solution)
ϕ_{p}	rad	Vibratory angle of the forced vibration (particular solution)
$\hat{\phi}_{\text{p}}$	rad	Angular amplitude of the forced vibration
$\hat{\phi}_{\text{stat}}$	rad	Angular amplitude of the forced vibration under load $(\phi=0)$
ψ	_	Damping coefficient acc. to DIN 740 /18/
ω	rad/s	Angular velocity, natural radian frequency of the damped vibration
ω_0	rad/s	Natural radian frequency of the undamped vibration
Ω	rad/s	Radian frequency of the excitation on vibration

Note: The unit "rad" (= radian) may be replaced with "1".

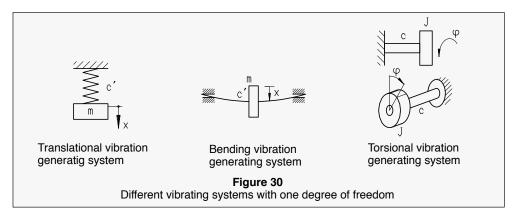
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3. Vibrations

3.1 General fundamental principles

Vibrations are more or less regularly occurring temporary variations of state variables. The state of a vibrating system can be described by suitable variables, such as displacement, angle, velocity, pressure, temperature, electric voltage/current, and the like.

The simplest form of a mechanical vibrating system consists of a mass and a spring with fixed ends, the mass acting as kinetic energy store and the spring as potential energy store, see figure 30. During vibration, a periodic conversion of potential energy to kinetic energy takes place, and vice versa, i.e. the kinetic energy of the mass and the energy stored in the spring are converted at certain intervals of time. Dependent on the mode of motion of the mass, a distinction is made between translational (bending) and torsional vibrating systems as well as coupled vibrating systems in which translational and torsional vibrations occur at the same time, influencing each other.

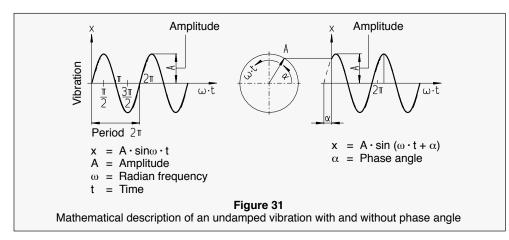


Further, a distinction is made between free vibrations and externally forced vibrations, and whether the vibration takes place without energy losses (undamped) or with energy losses (damped).

A vibration is free and undamped if energy is neither supplied nor removed by internal friction so that the existing energy content of the vibration is maintained. In this case the system carries out steady-state natural

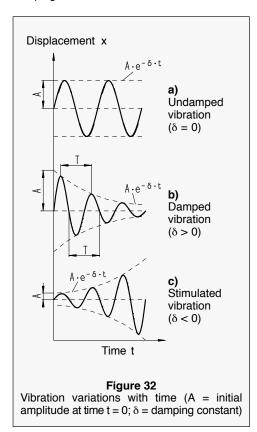
vibrations the frequency of which is determined only by the characteristics of the spring/mass system (natural frequency), figure 32 a.

The vibration variation with time x can be described by the constant amplitude of oscillation A and a harmonic function (sine, cosine) the arguments of which contain natural radian frequency $\omega = 2 \cdot \pi \cdot f$ (f = natural frequency in Hertz) and time, see figure 31.



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A damped vibration exists, if during each period of oscillation a certain amount of vibrational energy is removed from the vibration generating system by internal or external friction. If a constant viscous damping (Newton's friction) exists, the amplitudes of oscillation decrease in accordance with a geometric progression, figure 32 b. All technical vibration generating systems are subject to more or less strong damping effects.



If the vibrating system is excited by a periodic external force F(t) or moment M(t), this is a forced or stimulated vibration. With the periodic external excitation force, energy can be supplied to or removed from the vibrating system.

After a building-up period, a damped vibrating system does no longer vibrate with its natural frequency but with the frequency of the external excitation force.

Resonance exists, when the applied frequency is at the natural frequency of the system. Then, in undamped systems the amplitudes of oscillation grow at an unlimited degree, figure 32c. In damped systems, the amplitude of oscillation

grows until the energy supplied by the excitation force and the energy converted into heat by the damping energy are in equilibrium. Resonance points may lead to high loads in the components and therefore are to be avoided or to be quickly traversed (example: natural bending frequency in high-speed gear units).

The range of the occurring amplitudes of oscillation is divided by the resonance point (natural frequency = excitation frequency, critical vibrations) into the subcritical and supercritical oscillation range. As a rule, for technical vibrating systems (e.g. drives), a minimum frequency distance of 15% or larger from a resonance point is required.

Technical vibrating systems often consist of several masses which are connected with each other by spring or damping elements. Such systems have as many natural frequencies with the corresponding natural vibration modes as degrees of freedom of motion. A free, i.e. unfixed torsional vibration system with n masses, for instance, has n-1 natural frequencies. All these natural frequencies can be excited to vibrate by periodic external or internal forces, where mostly only the lower natural frequencies and especially the basic frequency (first harmonic) are of importance.

In technical drive systems, vibrations are excited by the following mechanisms:

a) From the input side:

Starting processes of electric motors, system short circuits, Diesel and Otto engines, turbines, unsteady processes, starting shock impulses, control actions.

b) From transmitting elements:

Meshing, unbalance, universal-joint shaft, alignment error, influences from bearings.

c) From the output side:

Principle of the driven machine, uniform, nonuniform, e.g. piston compressor, propeller.

As a rule, periodic excitation functions can be described by means of sine or cosine functions and the superpositions thereof. When analysing vibration processes, a Fourier analysis may often be helpful where periodic excitation processes are resolved into fundamental and harmonic oscillations and thus in comparison with the natural frequencies of a system show possible resonance points.

In case of simple vibrating systems with one or few (maximum 4) masses, analytic solutions for the natural frequencies and the vibration variation with time can be given for steady excitation. For unsteady loaded vibrating

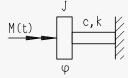
systems with one or more masses, however, solutions can be calculated only with the aid of numerical simulation programmes. This applies even more to vibrating systems with non-linear or periodic variable parameters (non-linear torsional stiffness of couplings; periodic meshing stiffnesses). With EDP programmes, loads with steady as well as unsteady excitation can be simulated for complex vibrating systems (linear, non-linear, parameter-excited) and the results be represented in the form of frequency analyses, load as a function of time, and overvoltages of resonance. Drive systems with torsionally flexi-

ble couplings can be designed dynamically in accordance with DIN 740 /18/. In this standard, simplified solution proposals for shockloaded and periodically loaded drives are made, the drive train having been reduced to a two-mass vibration generating system.

3.2 Solution proposal for simple torsional vibrators

Analytic solution for a periodically excited one-(fixed) or two-mass vibration generating system, figure 33.

Fixed one-mass vibration generating system



Free two-mass vibration generating system

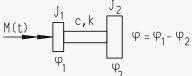


Figure 33 Torsional vibrators

 $J, J_1, J_2 = mass moment of inertia [kgm²]$ = torsional stiffness [Nm/rad] = viscous damping [Nms/rad]

M (t) = external excitation moment [Nm], time-variable

= angle of rotation [rad], $(\varphi = \varphi_1 - \varphi_2)$ for two-mass vibration generating systems

as relative angle)

= angular velocity [rad/s] (first time derivation of φ)

= angular acceleration [rad/s²] (second time derivation of φ)

Differential equation of motion:

One-mass vibration generating system:

$$\ddot{\phi} + \underbrace{\frac{k}{J}}_{2\delta} \dot{\phi} + \underbrace{\frac{c}{J}}_{\omega_0^2} \cdot \phi = \frac{M(t)}{J}$$
 (32)

Two-mass vibration generating system with relative coordinate:

$$\ddot{\varphi} + \underbrace{\frac{k}{J^{*}}}_{2\delta} \cdot \dot{\varphi} + \underbrace{\frac{c}{J^{*}}}_{\omega_{0}^{2}} \cdot \varphi = \frac{M(t)}{J_{1}}$$
(33)

with
$$\varphi = \varphi_1 - \varphi_2$$
 (34)

$$J^* = \frac{J_1 \cdot J_2}{J_1 + J_2} \tag{35}$$

Natural radian frequency (undamped): ω_0

$$\omega_0 = \sqrt{\frac{c}{I}}$$
 [rad/s] (36)

$$\omega_0 = \sqrt{c \cdot \frac{J_1 + J_2}{J_1 \cdot J_2}} \quad [rad/s] \tag{37}$$

Natural frequency:

$$f_{e} = \frac{\omega_{0}}{2\pi}$$
 [Hz] (38)

$$n_e = \frac{\omega_0 \cdot 30}{\pi}$$
 [1/min] (39)

(34)
$$\delta = \frac{k}{J} = \text{damping constant}$$
 [1/s] (40)

 ω_0 = natural radian frequency of the undamped vibration [rad/s]

f_e = natural frequency [Hertz]

n_e = natural frequency [1/min]

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(40)

Damped natural radian frequency:

$$\omega = \sqrt{\omega_0^2 - \delta^2} = \omega_0 \cdot \sqrt{1 - D^2} \tag{41}$$

Attenuation ratio (Lehr's damping): D

$$D = \frac{\delta}{\omega_0} = \frac{\mathbf{k} \cdot \omega_0}{2 \cdot \mathbf{c}} = \frac{\psi}{4\pi}$$
 (42)

 ψ = damping coefficient on torsionally flexible coupling, determined by a damping hysteresis of a period of oscillation acc. to DIN 740 /18/ and/or acc. to Flender brochure.

$$\psi = \frac{\text{damping energy}}{\text{elastic deformation energy}} = \frac{A_D}{A_e}$$

Reference values for some components:

D = 0.001...0.01 shafts (material damping of steel)
D = 0.04...0.08 gear teeth in gear units

D = 0.04...0.15 (0.2) torsionally flexible couplings

D = 0.01...0.04 gear couplings, all-steel couplings, universal joint shafts

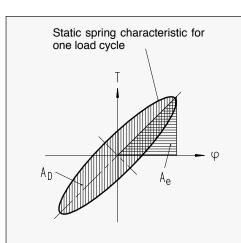


Figure 34
Damping hysteresis of a torsionally flexible component

3.3 Solution of the differential equation of motion

Periodic excitation moment

$$M(t) = M_0 \cdot \cos \Omega \cdot t \tag{43}$$

 M_0 = amplitude of moment [Nm] Ω = exciting circuit frequency [rad/s]

Total solution:

$$\varphi = \varphi_h + \varphi_p \tag{44}$$

a) Free vibration (homogeneous solution φ_h)

$$\varphi_h = A \cdot e^{-\delta \cdot t} \cdot \cos(\omega \cdot t - \gamma)$$
 (45)

Constants A and γ are determined by the starting conditions, e.g. by ϕ_h = 0 and $\dot{\phi}_h$ = 0 (initial-value problem).

In damped vibrating systems ($\delta > 0$) the free component of vibration disappears after a transient period.

b) Forced vibration (particular solution ϕ_{p})

$$\begin{split} \phi_p &= \frac{M_0^*}{c} \cdot \frac{1}{\sqrt{(1-\eta^2)^2 + 4D^2 \cdot \eta^2}} \\ &\cdot \cos{(\Omega \cdot t - \epsilon)} \end{split}$$

Phase angle:
$$\tan \varepsilon = \frac{2 \cdot D \cdot \eta}{1 - n^2}$$
 (47)

Frequency ratio:
$$\eta = \frac{\Omega}{\omega_0}$$
 (48)

One-mass vibration generating system:

$$\mathsf{M_0}^* = \mathsf{M_0} \tag{49}$$

Two-mass vibration generating system:

$$M_0^* = \frac{J_2}{J_1 + J_2} \cdot M_0 \tag{50}$$

c) Magnification factor

$$\varphi_{p} = \frac{M_{0}^{\star}}{c} \cdot V \cdot \cos (\Omega \cdot t - \epsilon)$$
 (51)

$$V = \frac{1}{\sqrt{(1 - \eta^2)^2 + 4D^2 \cdot \eta^2}} = \frac{\hat{\phi}_p}{\hat{\phi}_{stat}} = \frac{M}{M_0^*}$$
 (52)

(46)

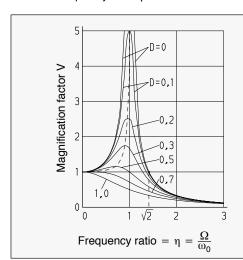
Vibrations

Solution of the Differential Equation of Motion Formulae for the Calculation of Vibrations

= vibration amplitude of forced vibration

 $\hat{\phi}_{\text{stat}} = \text{vibration}$ amplitude of forced vibration at a frequency ratio $\eta = 0$.

The magnification factor shows the ratio of the dynamic and static load and is a measure for the additional load caused by vibrations (figure 35).



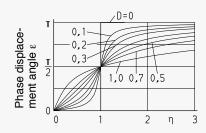


Figure 35

Magnification factors for forced, damped and undamped vibrations at periodic moment excitation (power excitation).

Magnification factors V and phase displacement angle ε.

3.4 Formulae for the calculation of vibra-

For the calculation of natural frequencies and vibrational loads, a general vibration generating system has to be converted to a calculable substitute system with point masses, spring and damping elements without mass.

3.4.1 Mass

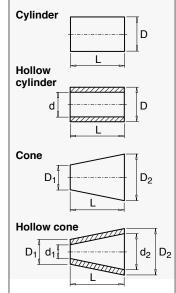
 $m = \varrho \cdot V$ [kg]

 $V = \text{volume } [m^3]$

 $o = \text{specific density } [kg/m^3]$

3.4.2 Mass moment of inertia

$$J = \int r^2 dm$$
: general integral formula



$$J = \frac{\varrho \cdot \pi \cdot L}{32} \cdot D^4$$

$$J = \frac{\varrho \cdot \pi \cdot L}{32} \cdot D^4$$

$$J = \frac{\varrho \cdot \pi \cdot L}{32} \cdot (D^4 - d^4) \qquad c = \frac{\pi \cdot G}{32 L} \cdot (D^4 - d^4)$$

$$J = \frac{Q^4 \pi^4 L}{32} \cdot (D^4 - d^4)$$

$$J = \frac{\varrho \cdot \pi \cdot L}{160} \cdot \frac{D_1^5 - D_2^5}{D_1 - D_2}$$

$$J = \frac{\varrho \cdot \pi \cdot L}{160} \cdot \left(\frac{D_1^5 - D_2^5}{D_1 - D_2} \right) c$$
$$- \frac{d_1^5 - d_2^5}{d_1 - d_2}$$

Torsional stiffness

$$c = \frac{\pi \cdot G}{32 L} \cdot D^4$$

$$c = \frac{\pi \cdot G}{32 I} \cdot (D^4 - d^4)$$

$$J = \left. \frac{\varrho \cdot \pi \cdot L}{160} \; \cdot \; \frac{D_1{}^5 - D_2{}^5}{D_1 - D_2} \; \right| \; c = \left. \frac{3 \cdot \pi \cdot G}{32 \; L} \cdot \frac{(D_1{}^3 \cdot D_2{}^3)}{(D_1{}^2 + D_1D_2 + D_2{}^2)} \right.$$

$$\begin{split} J &= \frac{\varrho \cdot \pi \cdot L}{160} \ \cdot \left(\frac{D_1{}^5 - D_2{}^5}{D_1 - D_2} \right) \ c &= \frac{3 \cdot \pi \cdot G}{32 \ L} \cdot \left[\frac{(D_1{}^3 \cdot D_2{}^3)}{(D_1{}^2 + D_1 D_2 + D_2{}^2)} \right. \\ &\left. - \frac{d_1{}^5 - d_2{}^5}{d_1 - d_2} \right) \\ &\left. - \frac{(d_1{}^3 \cdot d_2{}^3)}{(d_1{}^2 + d_1 d_2 + d_2{}^2)} \right] \end{split}$$

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Table 8 Symbols and units of translational and torsional vibrations					
Term	Quantity	Unit	Explanation		
Mass, Mass moment of inertia	m J	kg kg⋅m²	Translatory vibrating mass m; Torsionally vibrating mass with mass moment of inertia J		
Instantaneous value of vibration (displacement, angle)	χ φ	m rad *)	Instantaneous, time-dependent value of vibration amplitude		
Amplitude	$oldsymbol{x}_{ extsf{max},}\hat{oldsymbol{x}},oldsymbol{A}$ $\phi_{ extsf{max},}\hat{oldsymbol{\phi}},oldsymbol{A}$	m rad	Amplitude is the maximum instantaneous value (peak value) of a vibration.		
Oscillating velocity	x φ	m/s rad/s	Oscillating velocity; Velocity is the instantaneous value of the velocity of change in the direction of vibration.		
Inertia force, Moment of inertia forces	m·ẍ J·ÿ	N N·m	The d'Alembert's inertia force or the moment of inertia force acts in the opposite direction of the positive acceleration.		
Spring rate, Torsional spring rate	c' c	Nm N·m/rad	Linear springs		
Spring force, Spring moment	c'·x c·φ	N N·m	In case of linear springs, the spring recoil is proportional to deflection.		
Attenuation constant (Damping coefficient), Attenuation constant for rotary motion	k' k	N·s/m Nms/rad	In case of Newton's friction, the damping force is proportional to velocity and attenuation constant (linear damping).		
Damping factor (Decay coefficient)	$\delta = k'/(2 \cdot m)$ $\delta = k/(2 \cdot J)$	1/s 1/s	The damping factor is the damping coefficient referred to twice the mass.		
Attenuation ratio (Lehr's damping)	$D = \delta/\omega_0$	_	For D < 1, a damped vibration exists; for D \geq 1, an aperiodic case exists.		
Damping ratio	$\hat{x}_n / \hat{x}_{n+1} \\ \hat{\phi}_n / \hat{\phi}_{n+1}$	_	The damping ratio is the relation between two amplitudes, one cycle apart.		
Logarithmic damping decrement	$\Lambda = \frac{2 \cdot \pi \cdot D}{\sqrt{1 - D^2}}$	_	$\Lambda = \ln \left(\hat{\mathbf{x}}_{n} / \hat{\mathbf{x}}_{n+1} \right)$ $\Lambda = \ln \left(\hat{\mathbf{\phi}}_{n} / \hat{\mathbf{\phi}}_{n+1} \right)$		
Time	t	S	Coordinate of running time		
Phase angle	α	rad	In case of a positive value, it is a lead angle.		
Phase displacement angle	$\varepsilon = \alpha_1 - \alpha_2$	rad	Difference between phase angles of two vibration processes with same radian frequency.		
Period of a vibration	$T = 2 \cdot \pi / \omega_0$	s	Time during which a single vibration occurs.		
Frequency of natural vibration	$f = 1/T = \omega_0/(2 \cdot \pi)$	Hz	Frequency is the reciprocal value to a period of vibrations; vibrations per sec.		
Radian frequency of natural vibration	$\omega_0 = 2 \cdot \pi \cdot f$	rad/s	Radian frequency is the number of vibrations in $2\cdot\pi$ seconds.		
Natural radian frequency (Natural frequency)	$\omega_0 = \sqrt{c/m}$ $\omega_0 = \sqrt{c/J}$	rad/s rad/s	Vibration frequency of the natural vibration (undamped) of the system.		
Natural radian frequency when damped	$\omega_{\text{d}} = \sqrt{\omega_0^2 - \delta^2}$	rad/s	For a very small attenuation ratio $D < 1$ becomes $\omega_d \approx \omega_0$.		
Excitation frequency	Ω	rad/s	Radian frequency of excitation		
Radian frequency ratio	$\eta = \Omega/\omega_0$	_	Resonance exists at $\eta = 1$.		

^{*)} The unit "rad" may be replaced with "1".

3.4.3 Determination of stiffness

Table 9 Calculation of stiffness (examples)				
Example	Stiffness Symbols			
Coil spring	$c' = \frac{G \cdot d^4}{8 \cdot D_m^3 \cdot i_F} \left[\frac{N}{m} \right]$	 i_F = number of windings G = shear modulus ¹⁾ d = diameter of wire D_m = mean coil diameter 		
Torsion bar	$c = \frac{G \cdot I_p}{I} \left[\frac{\text{Nm}}{\text{rad}} \right]$ Shaft: $I_p = \frac{\pi \cdot d^4}{32}$ Hollow shaft: $I_p = \frac{\pi}{32} \left(d_a^4 - d_i^4 \right)$	I _p = second polar moment of area I = length d, d _i , d _a = diameters of shafts		
Tension bar F	$c' = \frac{E \cdot A}{I} \left[\frac{N}{m} \right]$	E = modulus of elasticity ¹⁾ A = cross-sectional area		
Cantilever beam	$c' = \frac{F}{f} = \frac{3 \cdot E \cdot I_a}{I^3} \left[\frac{N}{m} \right]$ Shaft: $I_a = \frac{\pi \cdot d^4}{64}$ Hollow shaft: $I_a = \frac{\pi}{64} (d_a^4 - d_i^4)$	F = force f = deformation at centre of mass under force F I _a = second axial moment of area		
Transverse beam (single load in the middle)	$c' = \frac{F}{f} = \frac{48 \cdot E \cdot I_a}{I^3} \left[\frac{N}{m} \right]$			
Transverse beam with overhanging end	$c' = \frac{F}{f} = \frac{3 \cdot E \cdot I_a}{a^2 \cdot (I + a)} \left[\frac{N}{m} \right]$	I = distance between bearings a = length of overhang- ing end		

1) For steel: $E = 21 \cdot 10^{10} \text{ N/m}^2$; $G = 8.1 \cdot 10^{10} \text{ N/m}^2$

Measuring the stiffness:

In a test, stiffness can be determined by measuring the deformation. This is particularly helpful if the geometric structure is very complex and very difficult to acquire.

Translation:

$$c' = \frac{F}{f} \quad [N/m] \tag{53}$$

F = applied force [N]

f = measured deformation [m]

Torsion:

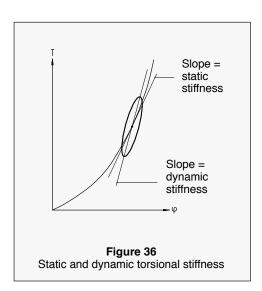
$$c = \frac{T}{\omega} \quad [Nm/rad] \tag{54}$$

T = applied torsion torque [Nm]

 φ = measured torsion angle [rad]

Measurements of stiffness are furthermore required if the material properties of the spring material are very complex and it is difficult to rate them exactly. This applies, for instance, to rubber materials of which the resilient properties are dependent on temperature, load frequency, load, and mode of stress (tension, compression, shearing). Examples of application are torsionally flexible couplings and resilient buffers for vibration isolation of machines and internal combustion engines.

These components often have non-linear progressive stiffness characteristics, dependent on the direction of load of the rubber material.



For couplings the dynamic stiffness is given, as a rule, which is measured at a vibrational

frequency of 10 Hz (vibrational amplitude = 25% of the nominal coupling torque). The dynamic torsional stiffness is greater than the static torsional stiffness, see figure 36.

3.4.4 Overlaying of different stiffnesses

To determine resulting stiffnesses, single stiffnesses are to be added where arrangements in series connection or parallel connection are possible.

Series connection:

Rule: The individual springs in a series connection carry the same load, however, they are subjected to different deformations.

$$\frac{1}{c_{\text{ges}}} = \frac{1}{c_1} + \frac{1}{c_2} + \frac{1}{c_3} + \dots + \frac{1}{c_n}$$
 (55)

Parallel connection:

Rule: The individual springs in a parallel connection are always subject to the same deformation.

$$c_{ges} = c_1 + c_2 + c_3 + ... + c_n$$
 (56)

3.4.5 Conversions

If drives or shafts with different speeds are combined in one vibration generating system, the stiffnesses and masses are to be converted to a reference speed (input or output).

Conversion is carried out as a square of the transmission ratio:

Transmission ratio:

$$i = \frac{n_1}{n_2} = \frac{\text{reference speed}}{\text{speed}}$$
 (57)

Conversion of stiffnesses c_{n2} and masses J_{n2} with speed n_2 to the respective values c_{n1} and J_{n1} with reference speed n_1 :

$$c_{n1} = c_{n2}/i^2$$
 (58)

$$J_{n1} = J_{n2}/i^2 (59)$$

Before combining stiffnesses and masses with different inherent speeds, conversion to the common reference speed has to be carried out first.

3.4.6 Natural frequencies

 a) Formulae for the calculation of the natural frequencies of a fixed one-mass vibration generating system and a free two-mass vibration generating system.

Natural frequency f_e in Hertz (1/s):

One-mass vibration generating system:

Two-mass vibration generating system:

Torsion:
$$f_e = \frac{1}{2\pi} \sqrt{\frac{c}{J}}$$

(60)
$$f_{e} = \frac{1}{2\pi} \sqrt{c} \frac{J_{1} + J_{2}}{J_{1} \cdot J_{2}}$$
 (61)

c = torsional stiffness [Nm/rad] $J, J_i = mass moments of inertia [kgm²]$

Translation, Bending :
$$f_e = \frac{1}{2\pi} \sqrt{\frac{c'}{m}}$$
 (62) $f_e = \frac{1}{2\pi} \sqrt{c' \frac{m_1 + m_2}{m_1 \cdot m_2}}$

$$f_{e} = \frac{1}{2\pi} \sqrt{c' \frac{m_1 + m_2}{m_1 \cdot m_2}}$$
 (63)

c' = translational stiffness (bending stiffness) [N/m] $m, m_i = masses [kg]$

b) Natural bending frequencies of shafts supported at both ends with applied masses with known deformation f due to the dead weight.

$$f_{e} = \frac{q}{2\pi} \sqrt{\frac{g}{f}} \qquad [Hz] \tag{64} \label{eq:fe}$$

 $q = 9.81 \text{ m/s}^2 \text{ gravity}$

f = deformation due to dead weight [m]

q = factor reflecting the effect of the shaft masses on the applied mass

q = 1 shaft mass is neglected compared with the applied mass

q = 1.03 ... 1.09 common values when considering the shaft masses

q = 1.13 solid shaft without pulley

 Natural bending frequencies for shafts, taking into account dead weights (continuum); general formula for the natural frequency in the order f_{e,i}.

$$f_{e,i} = \frac{1}{2\pi} \cdot \left(\frac{\lambda_i}{I}\right)^2 \cdot \sqrt{\frac{I \, E}{\varrho \cdot A}} \, \left[Hz \right] \tag{65}$$

 λ_i = inherent value factor for the i-th natural frequency

l = length of shaft [m]

E = modulus of elasticity [N/m²]

I = moment of area [m⁴]

 $o = density [kg/m^3]$

A = cross-sectional area [m²]

d = diameter of solid shaft [m]

Table 10 λ-values for the first three natural frequencies, dependent on mode of fixing

Bearing application	λ ₁	λ_2	λ3
	1.875	4.694	7.855
	4.730	7.853	10.966
	π	2π	3π
	3.927	7.069	10.210

For the solid shaft with free bearing support on both sides, equation (65) is simplified to:

$$f_{e,i} = \frac{\pi \cdot d}{8} \left(\frac{i}{I} \right)^2 \cdot \sqrt{\frac{E}{Q}} \quad [Hz]$$
 (66)

i = 1st, 2nd, 3rd ... order of natural bending frequencies.

3.5 Evaluation of vibrations

The dynamic load of machines can be determined by means of different measurement methods. Torsional vibration loads in drives, for example, can be measured directly on the shafts by means of wire strain gauges. This requires, however, much time for fixing the strain gauges, for calibration, signal transmission and evaluation. Since torques in shafts are generated via bearing pressure in gear units, belt drives, etc., in case of dynamic loads, structure-borne noise is generated which can be acquired by sensing elements at the bearing points in different directions (axial, horizontal, vertical). Dependent on the requirements, the amplitudes of vibration displacement, velocity and acceleration can be recorded and evaluated in a sum (effective vibration

velocity) or frequency-selective. The structure-borne noise signal reflects besides the torque load in the shafts also unbalances, alignment errors, meshing impulses, bearing noises, and possibly developing machine damages.

To evaluate the actual state of a machine, VDI guideline 2056¹⁾ or DIN ISO 10816-1 /19, 20/ is consulted for the effective vibration velocity, as a rule, taking into account structure-borne noise in the frequency range between 10 and 1,000 Hertz. Dependent on the machine support structure (resilient or rigid foundation) and power transmitted, a distinction is made between four machine groups (table 11). Dependent on the vibration velocity, the vibrational state of a machine is judged to be "good", "acceptable", "still permissible", and "non-permis-

sible". If vibration velocities are in the "non-permissible" range, measures to improve the vibrational state of the machine (balancing, improving the alignment, replacing defective machine parts, displacing the resonance) are required, as a rule, or it has to be verified in detail that the vibrational state does not impair the service life of the machine (experience, verification by calculation).

Structure-borne noise is emitted from the machine surface in the form of airborne noise and has an impact on the environment by the generated noises. For the evaluation of noise, sound pressure level and sound intensity are measured. Gear unit noises are evaluated according to VDI guideline 2159 or DIN 45635 /17, 16/, see subsection 1.5.

Table 11 Boundary limits acc. to VDI guideline 2056 1) for four machine groups					
Machine	Including gear units and machines with input power	Range classification acc. to VDI 2056 ("Effective value of the vibration velocity" in mm/s)			
groups	ratings of	Good	Acceptable	Still permissible	Non- permissible
К	up to approx. 15 kW with- out special foundation.	up to 0.7	0.7 1,8	1.8 4.5	from 4.5 up
М	from approx. 15 up to 75 kW without special foundation from approx. 75 up to 300 kW and installation on highly tuned, rigid or heavy foundations.	up to 1.1	1.1 2.8	2.8 7.1	from 7.1 up
G	over 300 kW and installation on highly tuned, rigid or heavy foundations.	up to 1.8	1.8 4.5	4.5 11	from 11 up
т	over 75 kW and installation on broadly tuned resilient foundations (especially also steel foundations designed according to light-construc- tion guidelines).	up to 2.8	2.8 7	7 18	from 18 up

^{1) 08/97} withdrawn without replacement; see /20/

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